

# The Radial Acceleration Relation: Linking baryons and DM in Galaxies

Federico Lelli



Main Collaborators:

**Stacy McGaugh** (Case Western Reserve)

**James Schombert** (U of Oregon)

**Marcel Pawlowski** (U of California - Irvine)



# Outline:

## I. Introduction: Dynamics of Galaxies

Rotation curves, mass models, scaling relations.

## II. The SPARC Galaxy Database

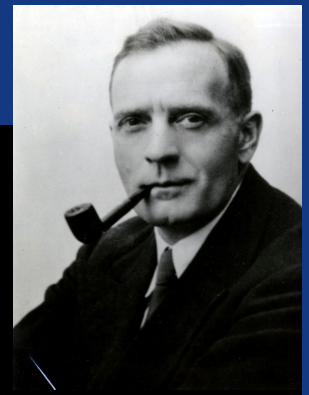
Largest compilation of galaxy mass models to date.

## III. The Radial Acceleration Relation

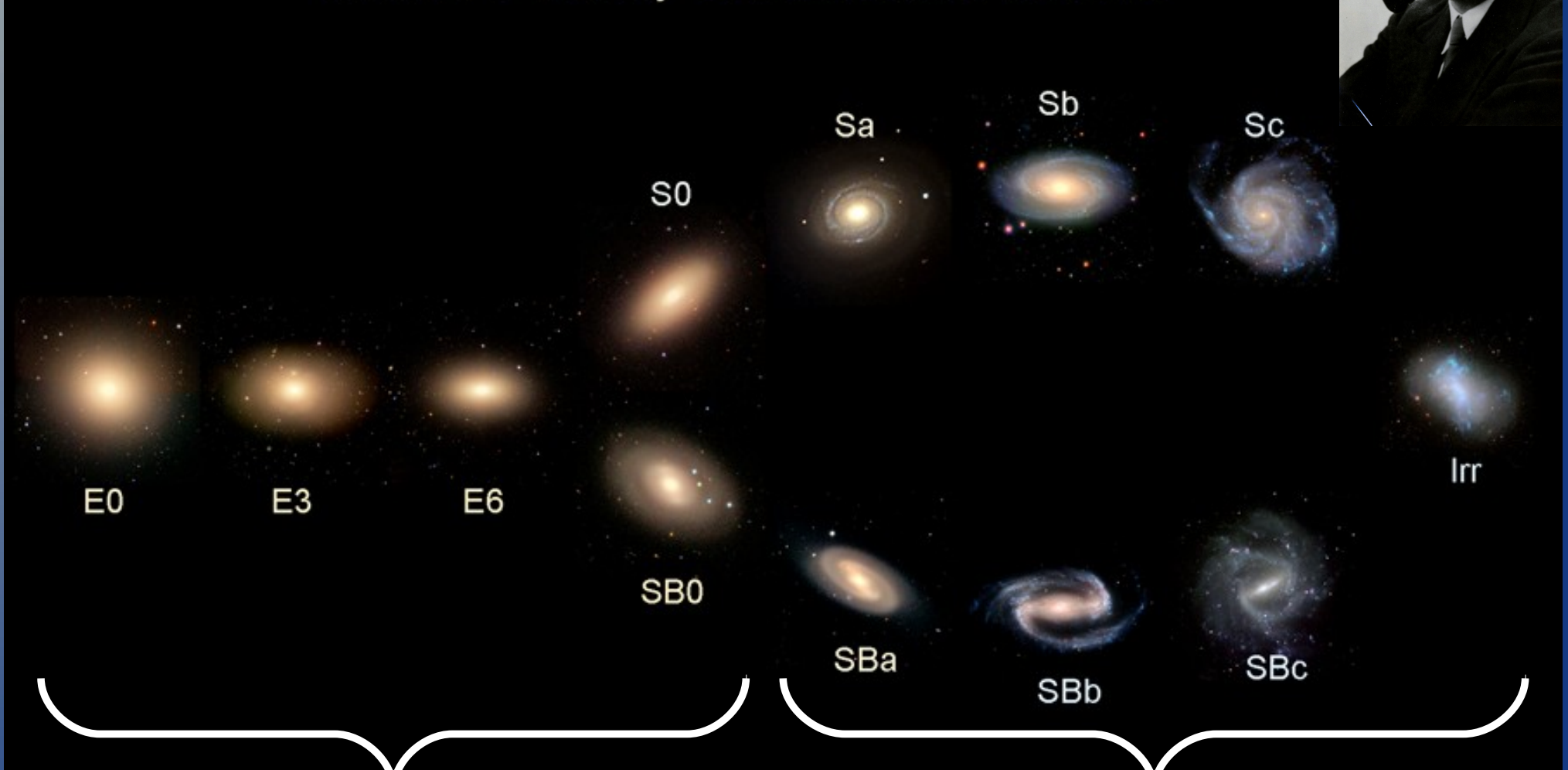
Local link between baryons and dark matter in galaxies.

# I. Introduction: Dynamics of Galaxies

# Galaxies: "Island Universes"



## Hubble's Galaxy Classification Scheme



**Early-Type Galaxies (ETGs): E and S0**

Little Cold Gas → No Star Formation  
→ Dominated by Old Stars

**Late-Type Galaxies (LTGs): S and Irr**

Disk of Cold Gas → Star Formation  
→ Both Young & Old Stars



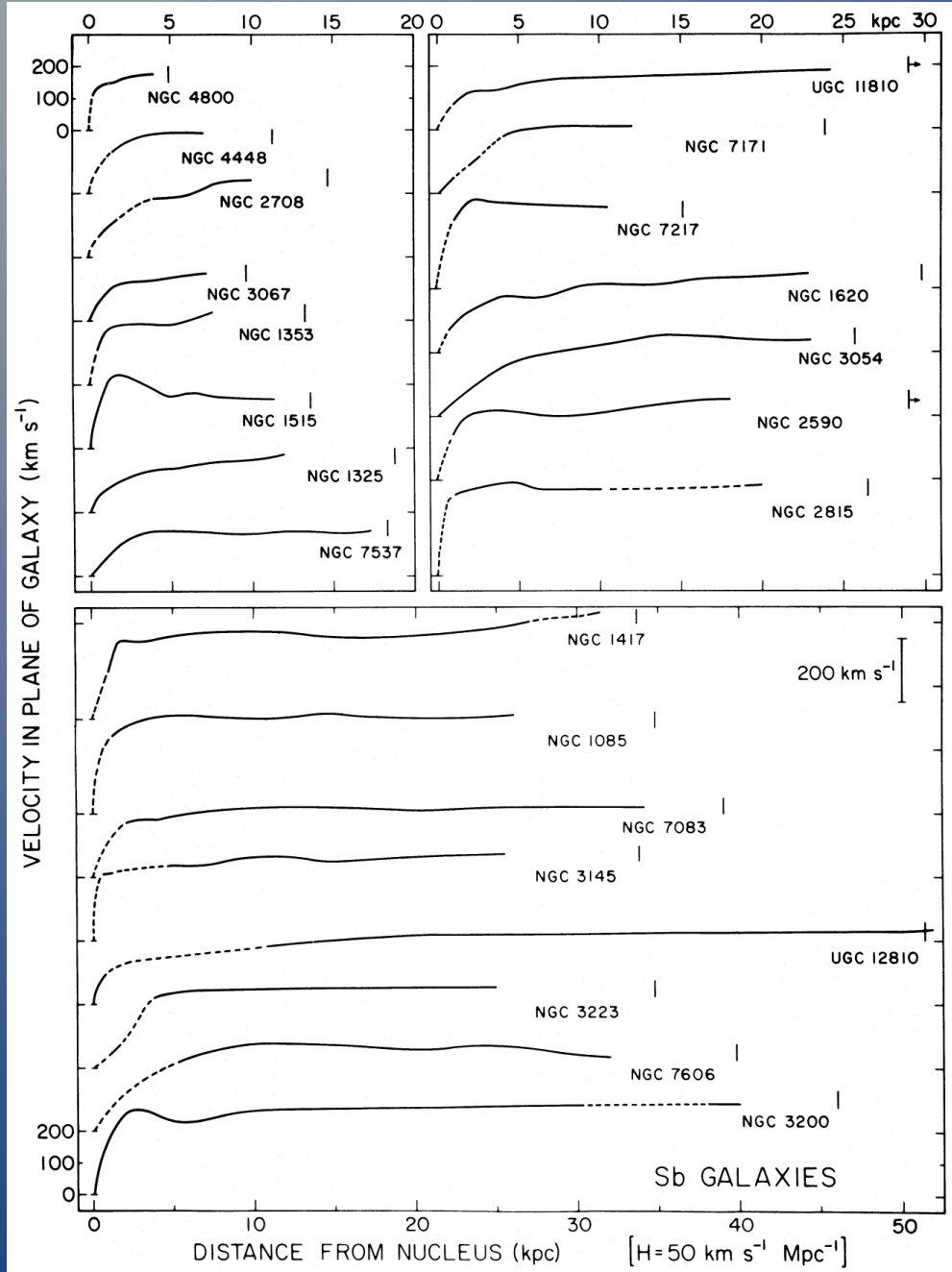
# Galaxy Rotation Curves are Flat at Large Radii

Historical Evidence for  
Mass Discrepancies

$$V = \text{const}$$

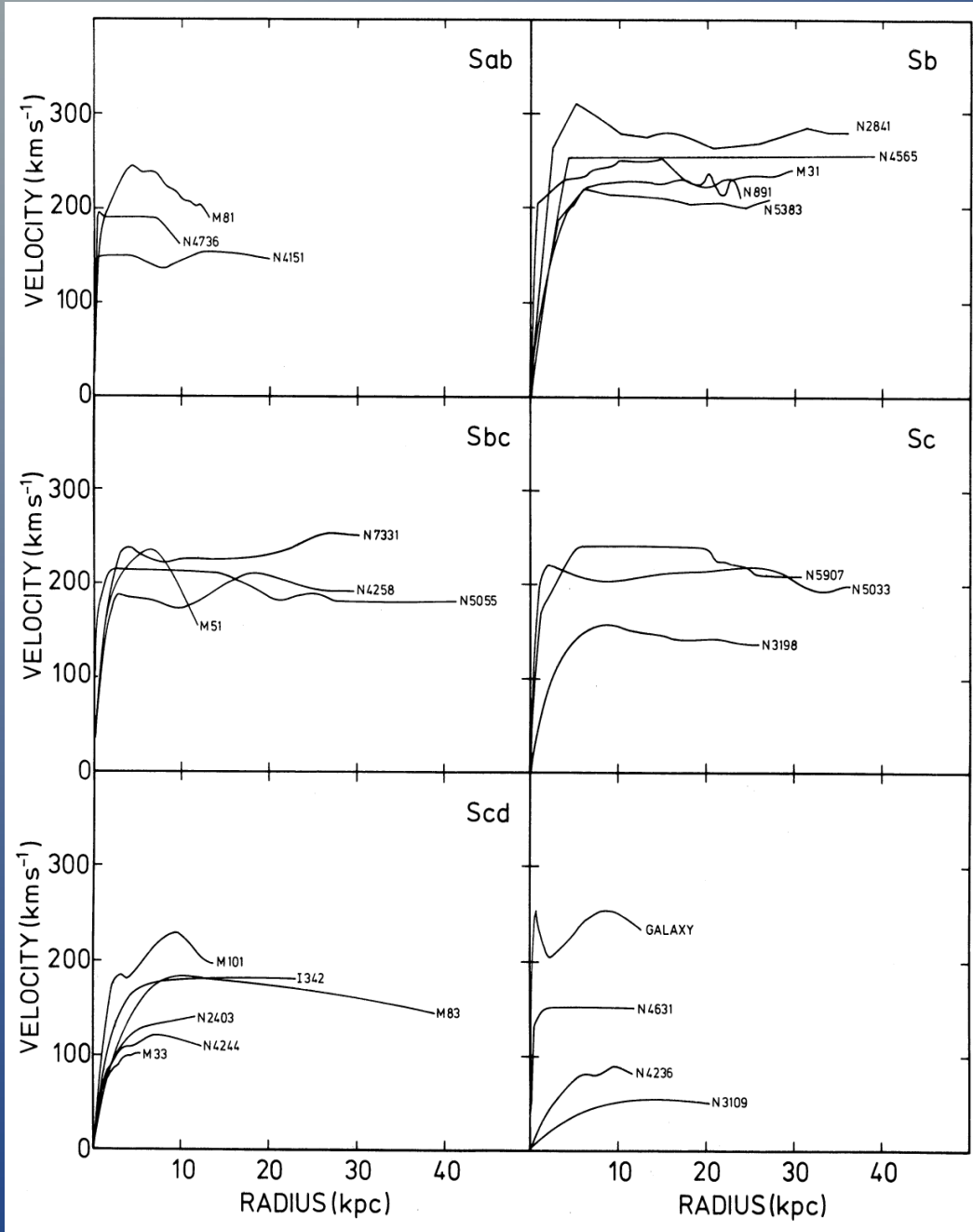
$$M_{\text{tot}} \propto r$$

$$\rho_{\text{tot}} \propto r^{-2}$$



Optical Observations of Ionized Gas  
V. Rubin et al. (1978, 1982)

# Galaxy Rotation Curves are Flat at Large Radii



Historical Evidence for  
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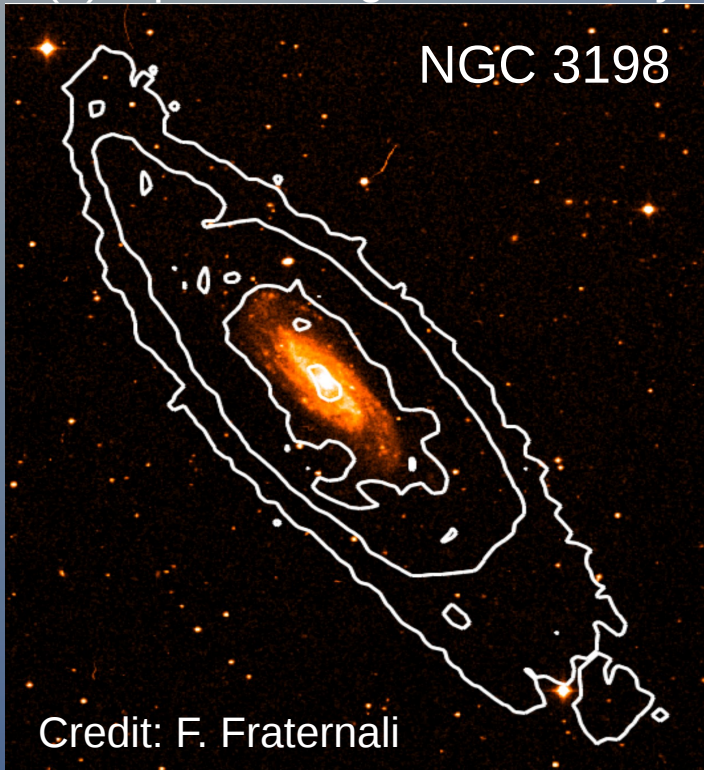


Radio Observations of Neutral Gas  
A. Bosma (1978, 1981)

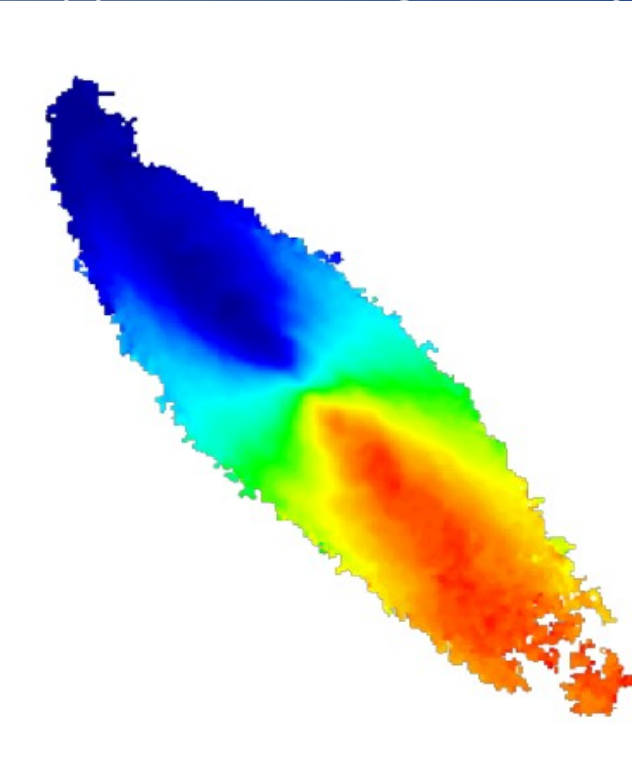


# Atomic Hydrogen (HI): Radio Data at 21 cm

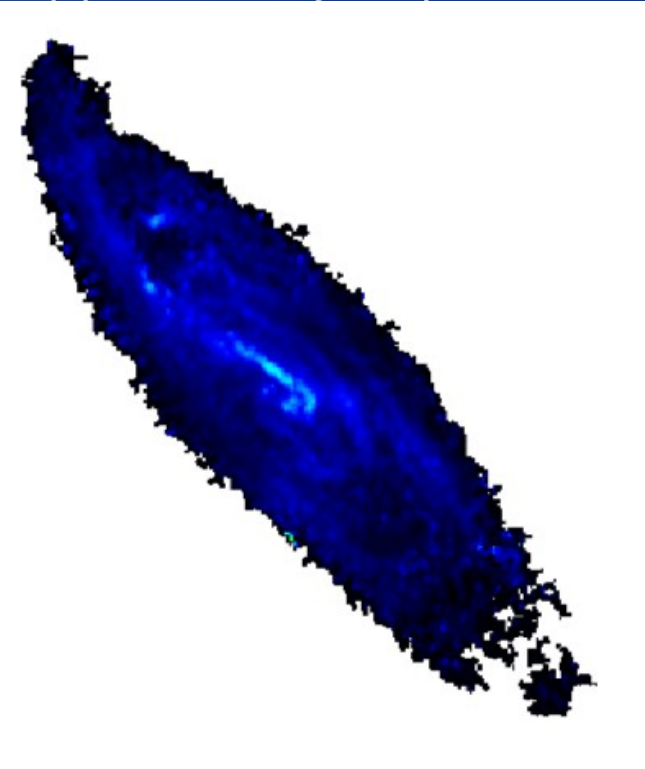
(1) Optical Image + HI density



(2) HI Line-of-Sight Velocity



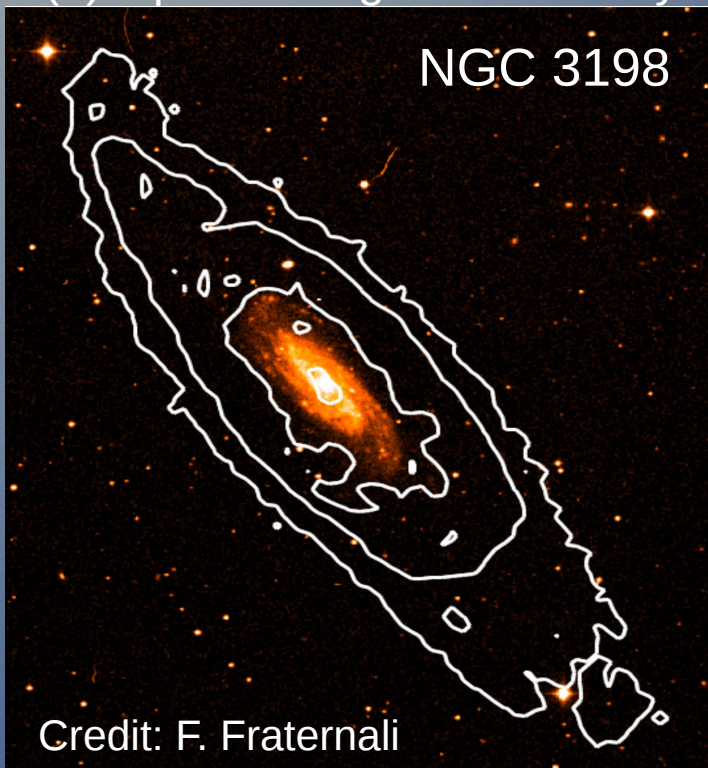
(3) HI Velocity Dispersion



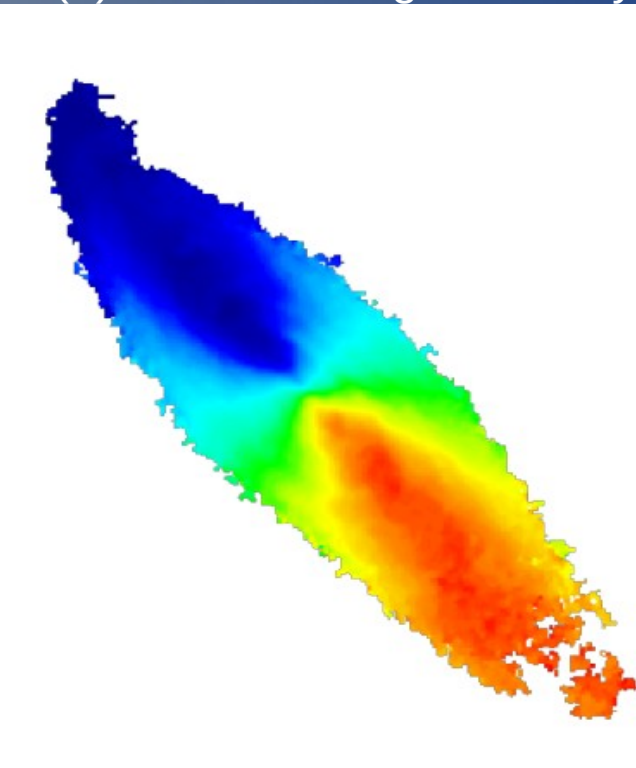
Good tracer of the **total** gravitational potential:  $\frac{V_{rot}^2}{R} = -\frac{\partial \Phi_{tot}}{\partial R}$

# Atomic Hydrogen (HI): Radio Data at 21 cm

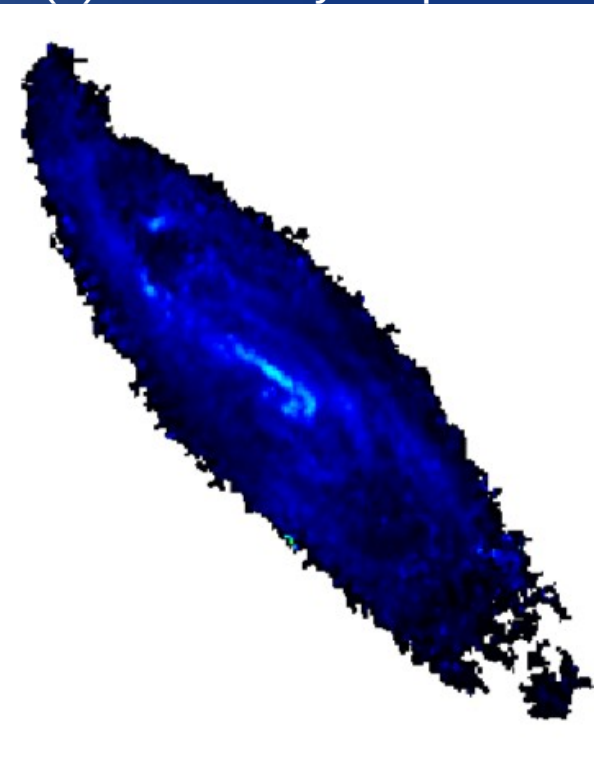
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(2) HI Line-of-Sight Velocity



(3) HI Velocity Dispersion



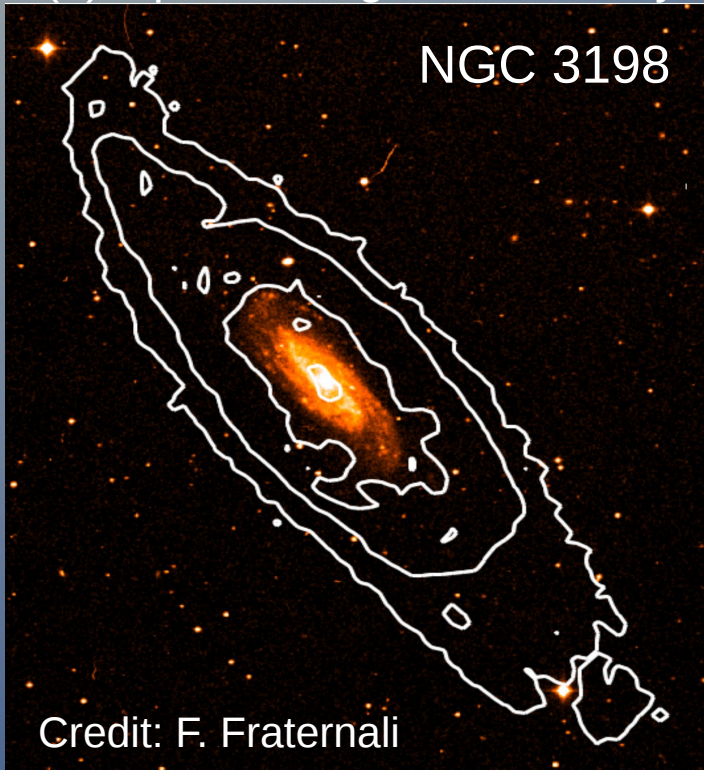
Good tracer of the **total** gravitational potential:  $\frac{V_{rot}^2}{R} = -\frac{\partial \Phi_{tot}}{\partial R}$

- (1) **HI is more extended than the stars** → trace the kinematics out to large R
- (2) **HI is in a rotating disk** → deviations from circular orbits are small (~10 km/s)
- (3) **HI velocity dispersion is small** (~10 km/s) → pressure support is negligible

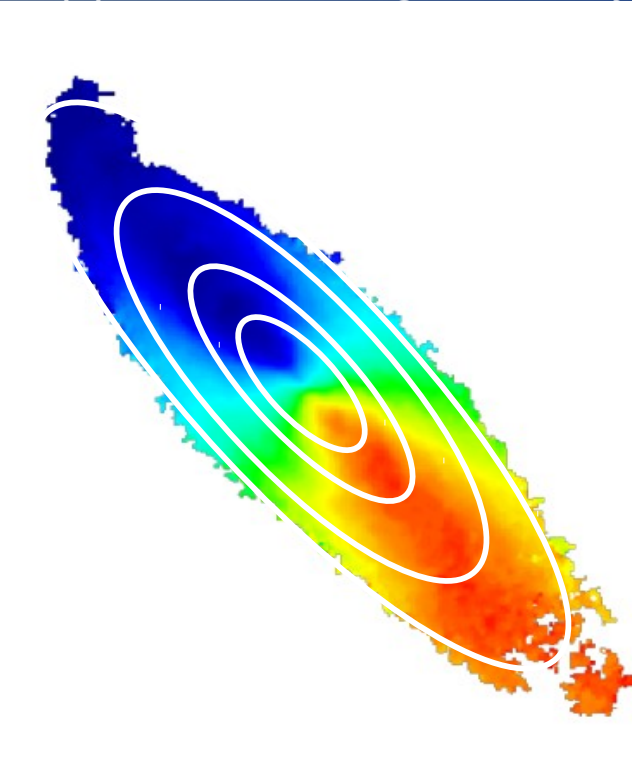


# Atomic Hydrogen (HI): Radio Data at 21 cm

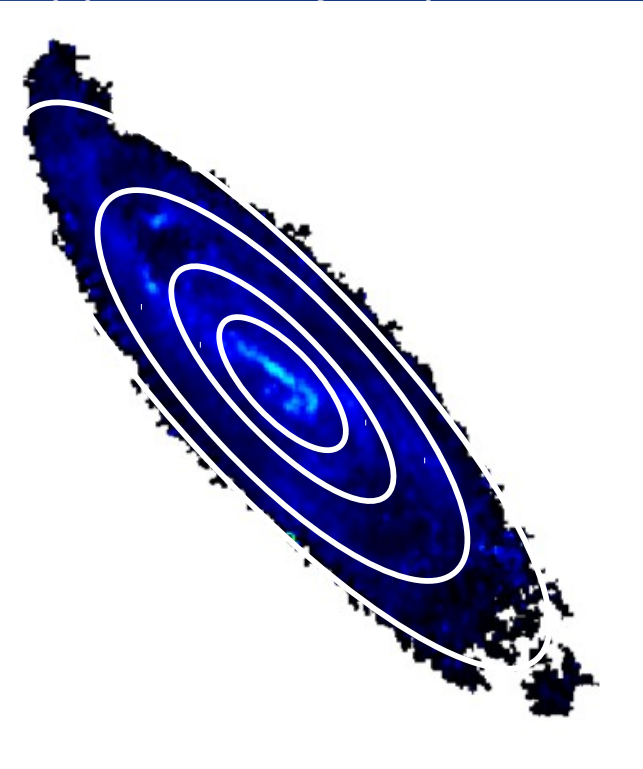
(1) Optical Image + HI density



(2) HI Line-of-Sight Velocity



(3) HI Velocity Dispersion



Deprojection from **sky plane** to **galaxy plane**:

$$V_{\text{l.o.s.}} = V_{\text{sys}} + V_{\text{rot}} \sin(i) \cos(\theta)$$

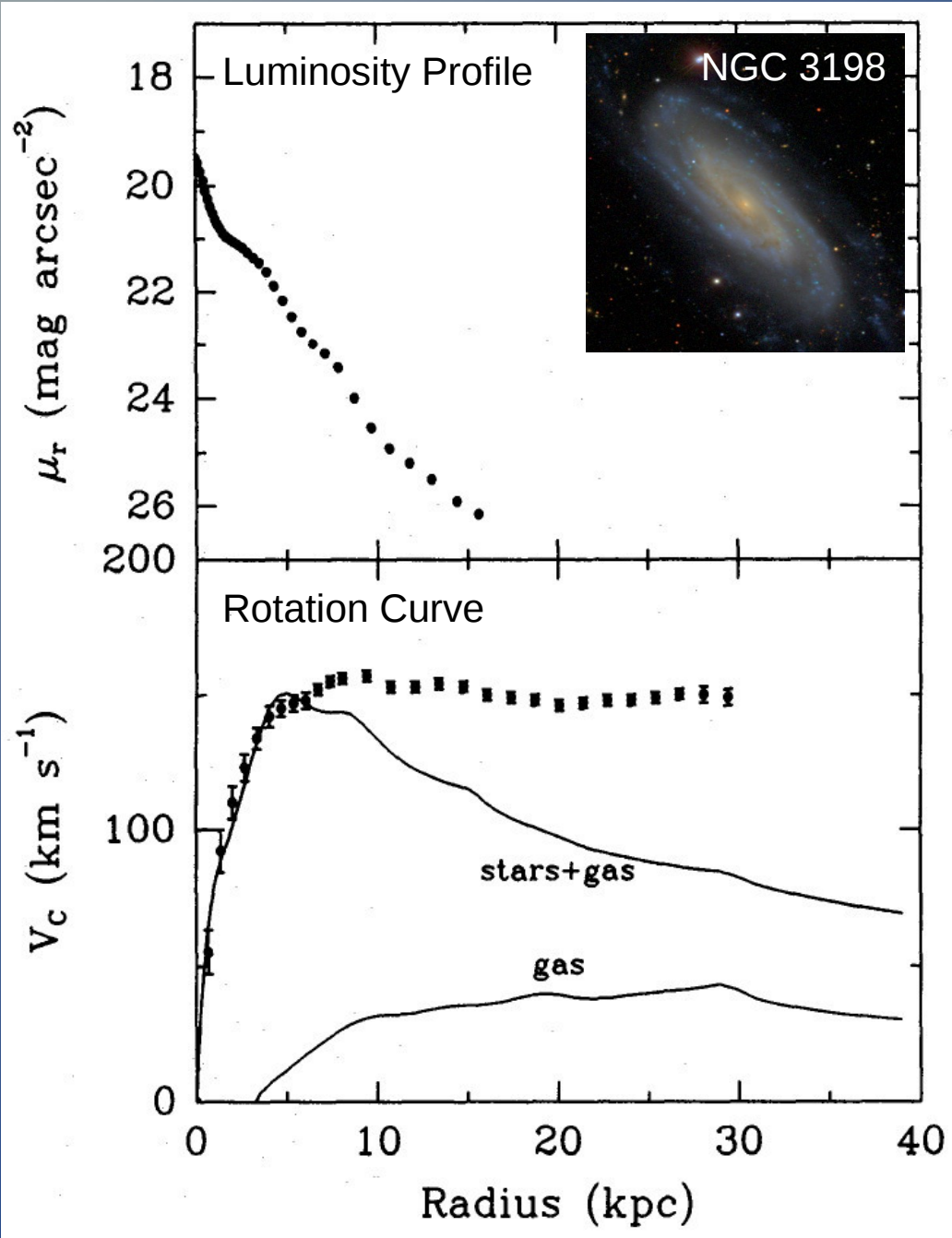
$$\cos(\theta) = \text{fnc}(\text{center}, \text{position angle})$$

$i$  = disk inclination angle

$\theta$  = azimuthal angle

$V_{\text{sys}}$  = recession velocity

# Mass Models for Late-Type Galaxies



Solve Poisson's Equation for each baryonic component ( $i = \text{stars, gas}$ )

$$\nabla^2 \Phi_i(R, z) = 4\pi G \rho_i(R, z)$$

Assume nominal disk thickness

$$\rho_i(R, z) = \mu_i(R) \nu_i(z)$$

Find expected circular velocity

$$\frac{V_i^2(R, z=0)}{R} = - \frac{\partial \Phi_i(R, z=0)}{\partial R}$$

Sum over all baryonic contributions

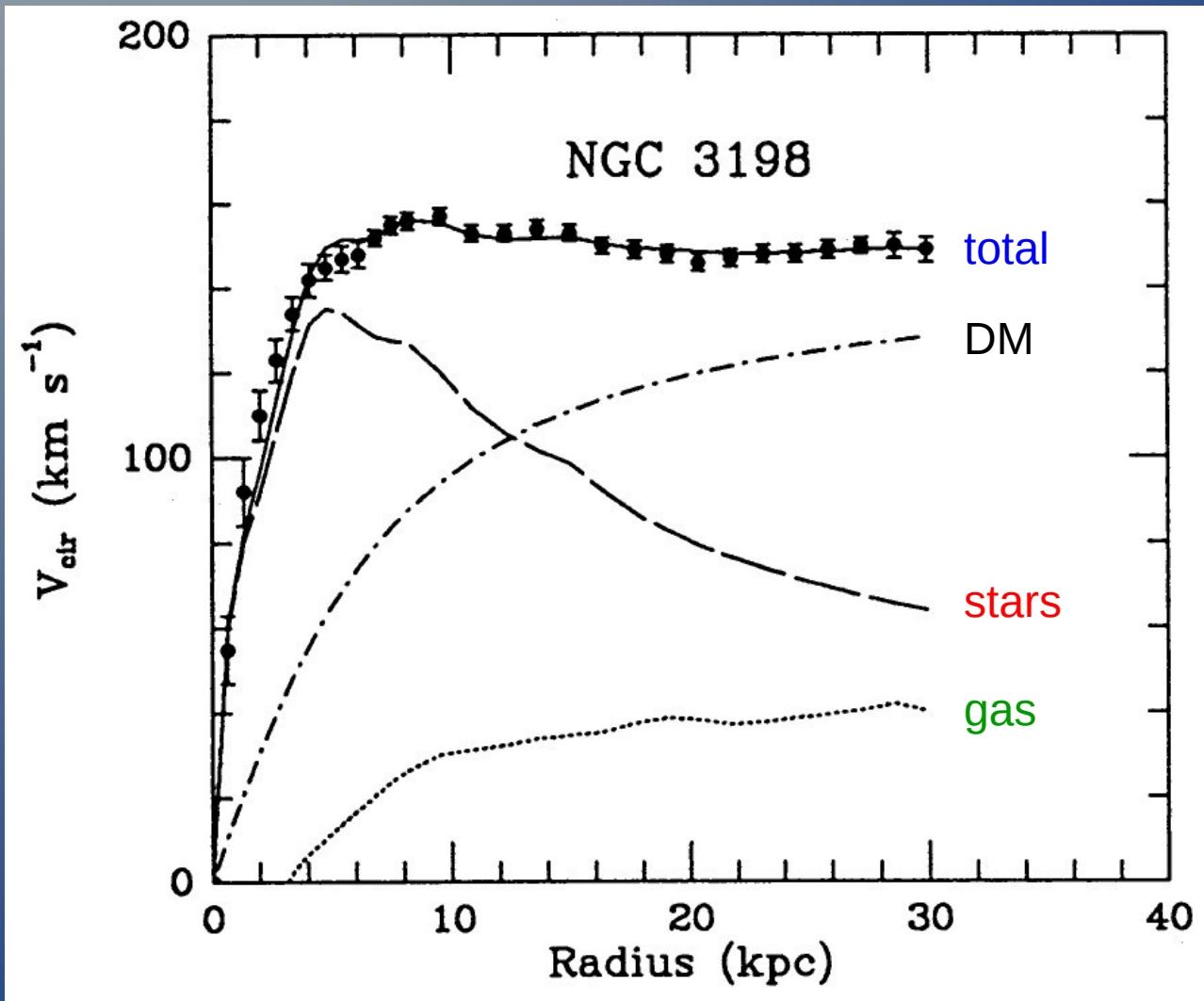
$$V_b^2(R) = \sum_i V_i^2(R)$$

Casertano 1983; van Albada+1985; Begeman 1987



# Mass Models with a Dark Matter Halo

$$V_{\text{total}}^2 = \Upsilon_* \cdot V_{\text{stars}}^2 + V_{\text{gas}}^2 + V_{\text{DM}}^2(\rho_0, r_s)$$



Van Albada et al. (1985); Begeman (1987)

## Mass Model with 3 Free Parameters:

- $\rho_0$  and  $r_s$  for DM halo
- $\Upsilon_*$  = mass-to-light ratio for stars.

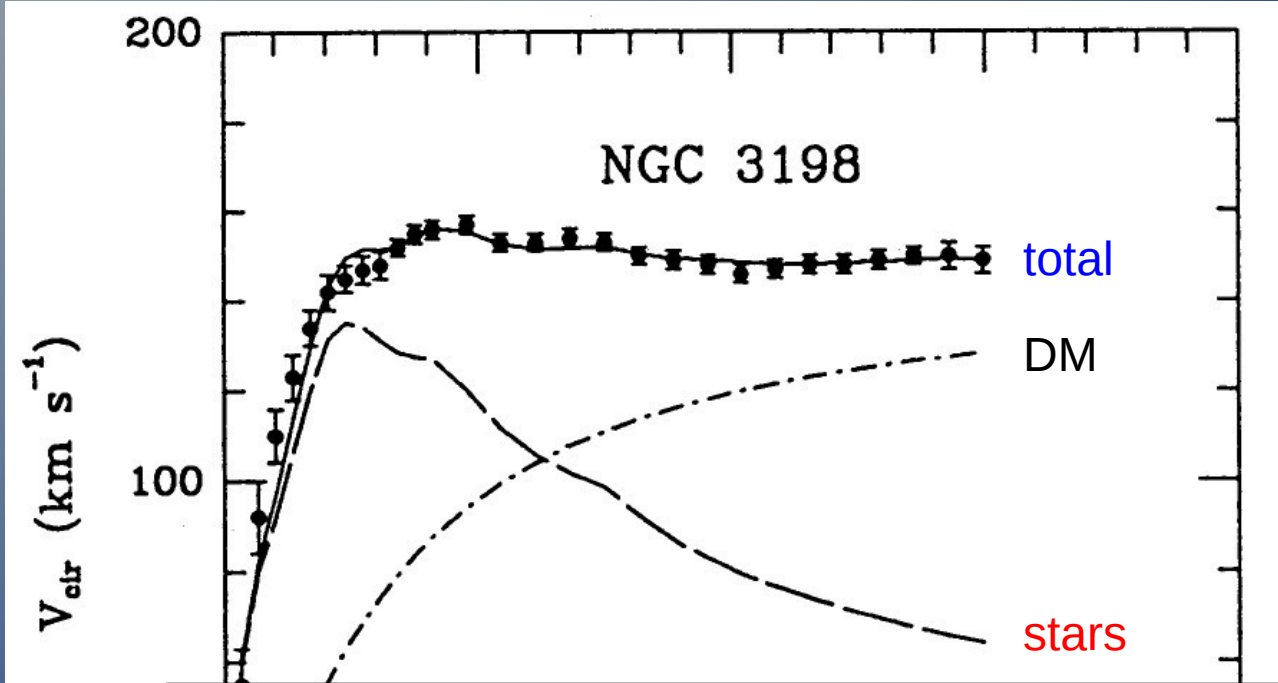
$\Upsilon_*$  depends on the stellar populations in the galaxy.

## Not needed for the gas:

Conversion from 21cm flux to gas mass is known from atomic physics of H + correction for He (BBN)

# Mass Models with a Dark Matter Halo

$$V_{\text{total}}^2 = \Upsilon_* \cdot V_{\text{stars}}^2 + V_{\text{gas}}^2 + V_{\text{DM}}^2(\rho_0, r_s)$$



## Mass Model with 3 Free Parameters:

- $\rho_0$  and  $r_s$  for DM halo
  - $\Upsilon_* =$  mass-to-light ratio for stars.
- $\Upsilon_*$  depends on the stellar populations in the galaxy.

### Disk-Halo Conspiracy:

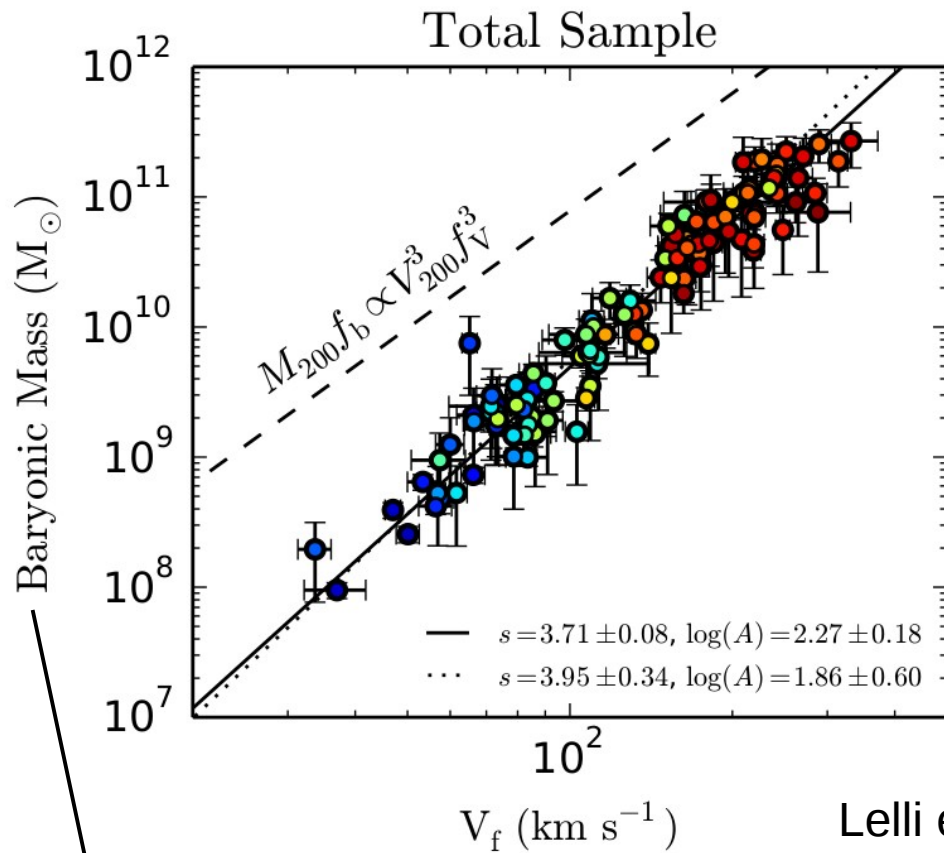
"Luminous matter and dark matter seem to conspire to produce the flat observed rotation curves in the outer region."

(van Albada & Sancisi 1986)

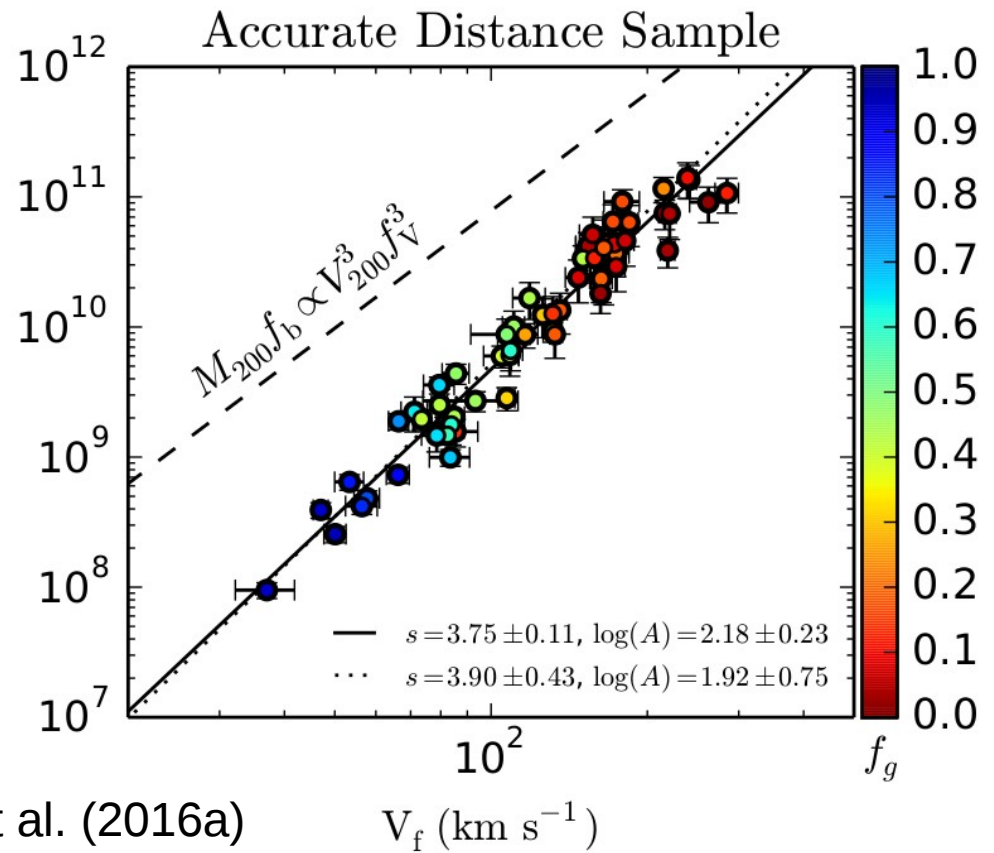




# Baryonic Tully-Fisher Relation (BTFR)



Lelli et al. (2016a)

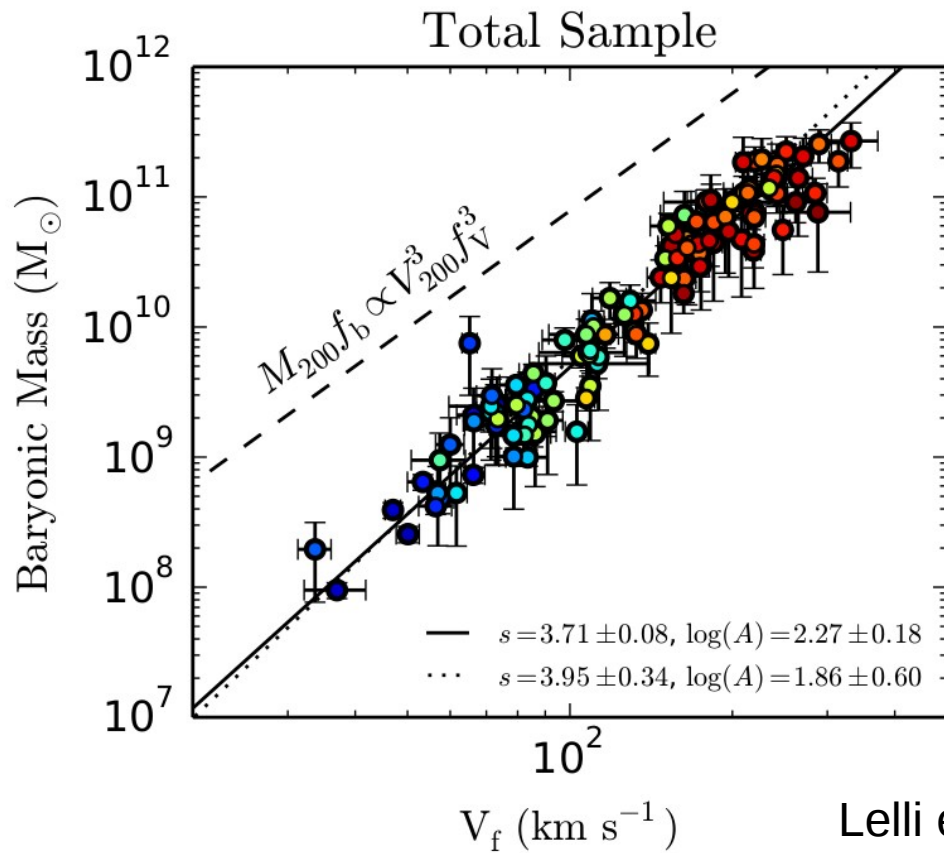


$$M_* + M_{\text{gas}} \propto D^2$$

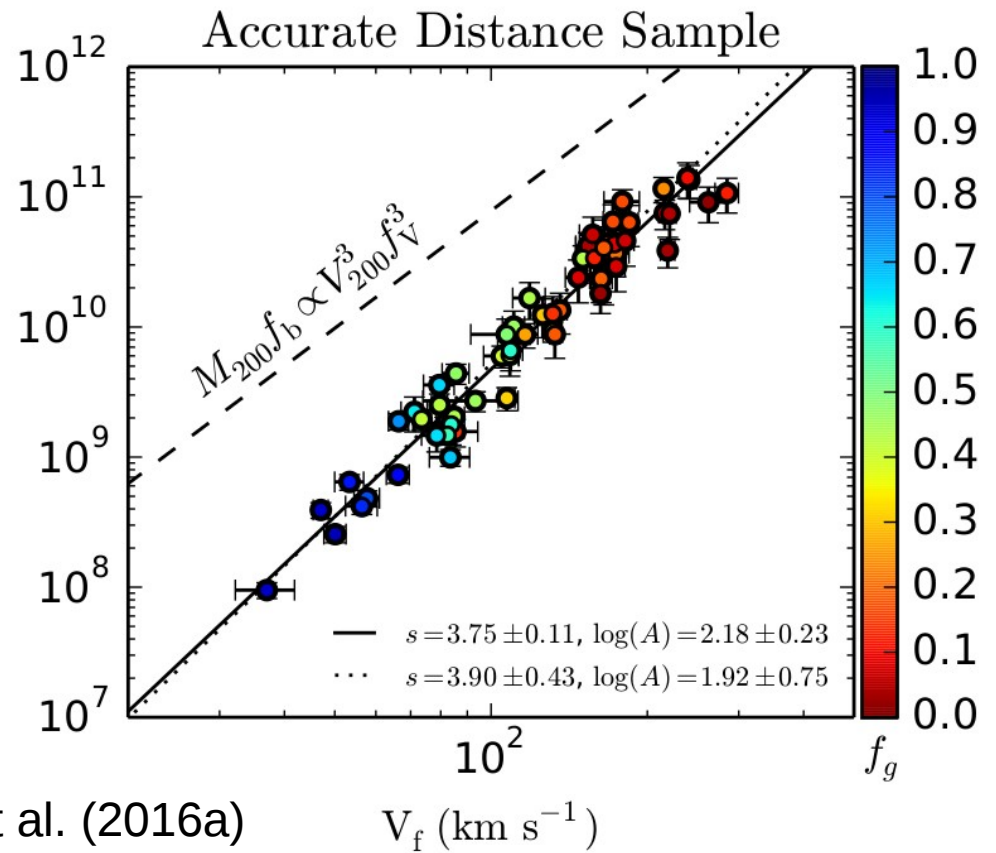
As the data quality increases, the scatter decreases!

**Some BTFR studies:** Freeman 1999; Walker 1999; McGaugh+2000, 2005, 2012; Verhejen 2001; Bell & de Jong 2001; Geha+2006; Noordermeer & Verheijen+2007; Begum+2008; Avila-Reese+2008; Stark+2009; Trachternach+2010; Gurovich+2010; Catinella+2012; Zaritsky+2014; Papastergis+2016

# Baryonic Tully-Fisher Relation (BTFR)

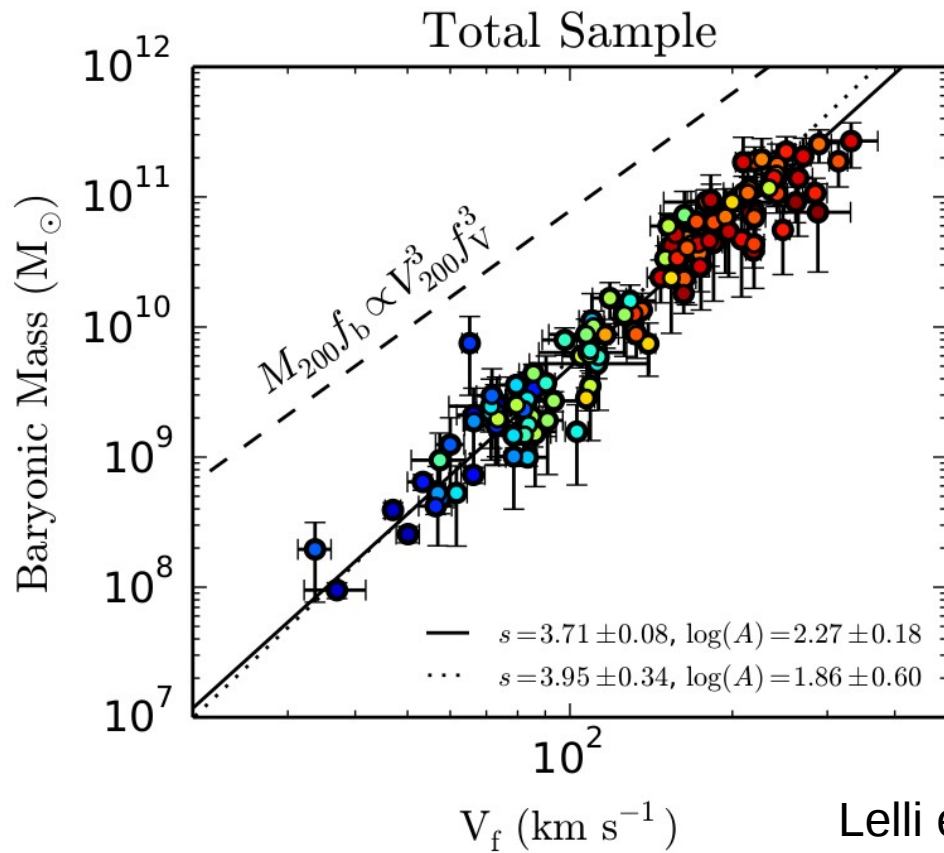


Lelli et al. (2016a)

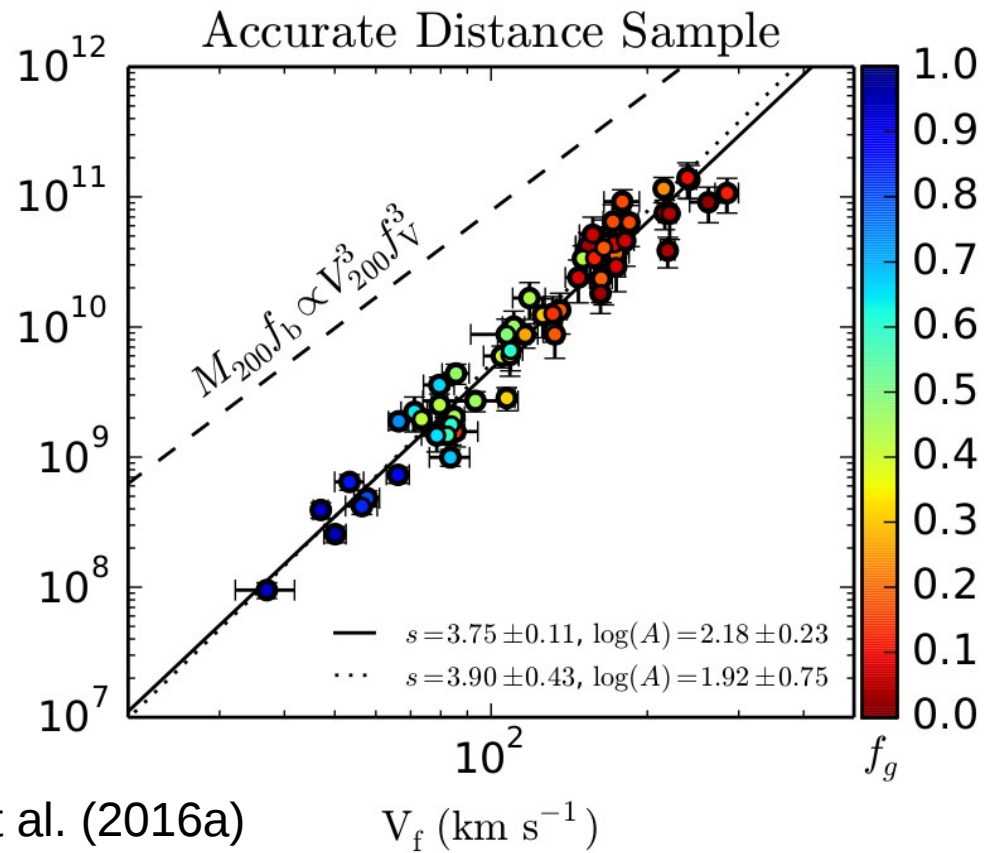


In  $\Lambda$ CDM:  $M_{200} = (10GH_0)^{-1} V_{200}^3$

# Baryonic Tully-Fisher Relation (BTFR)



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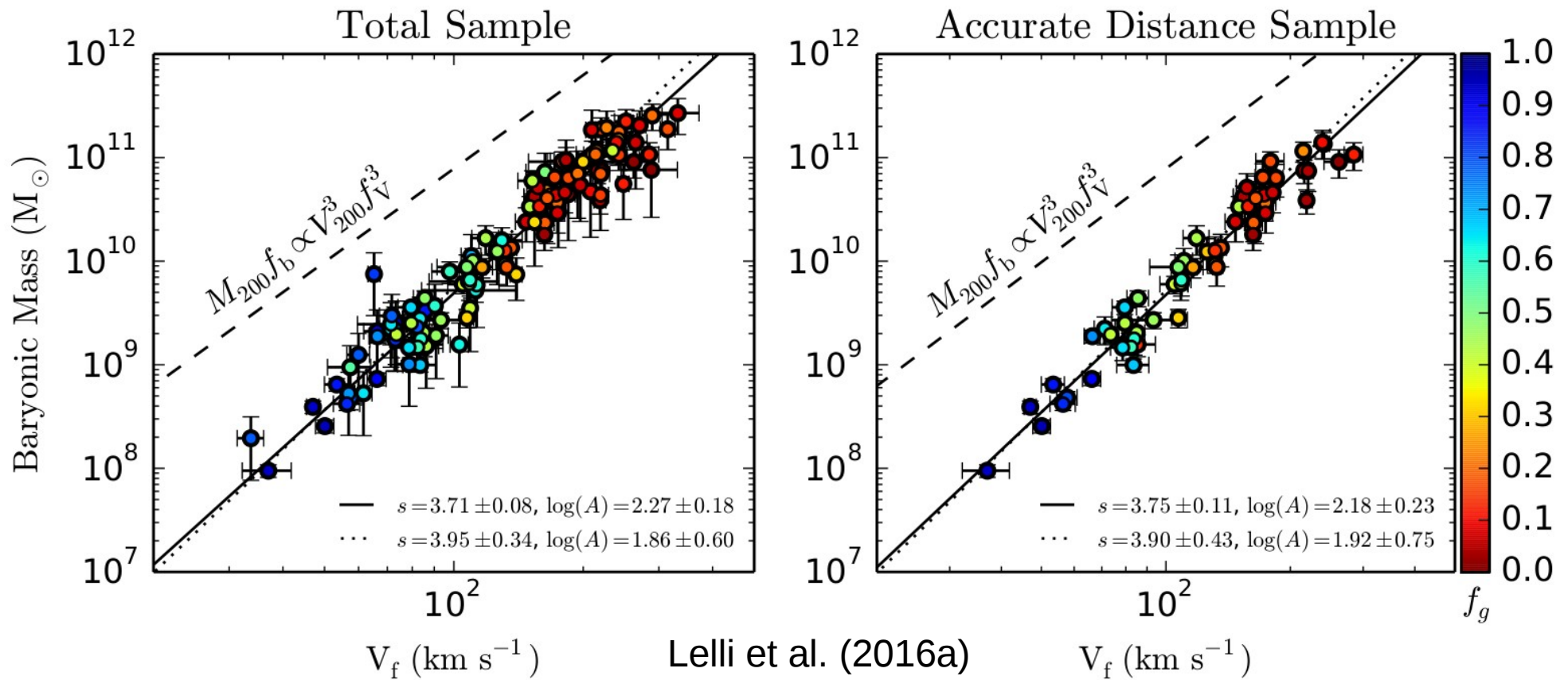


**In  $\Lambda$ CDM:**  $M_{200} = (10GH_0)^{-1} V_{200}^3$

$$f_b = M_b / M_{200} \quad f_V = V_f / V_{200} \quad \rightarrow \quad M_b = (10GH_0)^{-1} (f_b / f_V^3) V_f^3$$



# Baryonic Tully-Fisher Relation (BTFR)

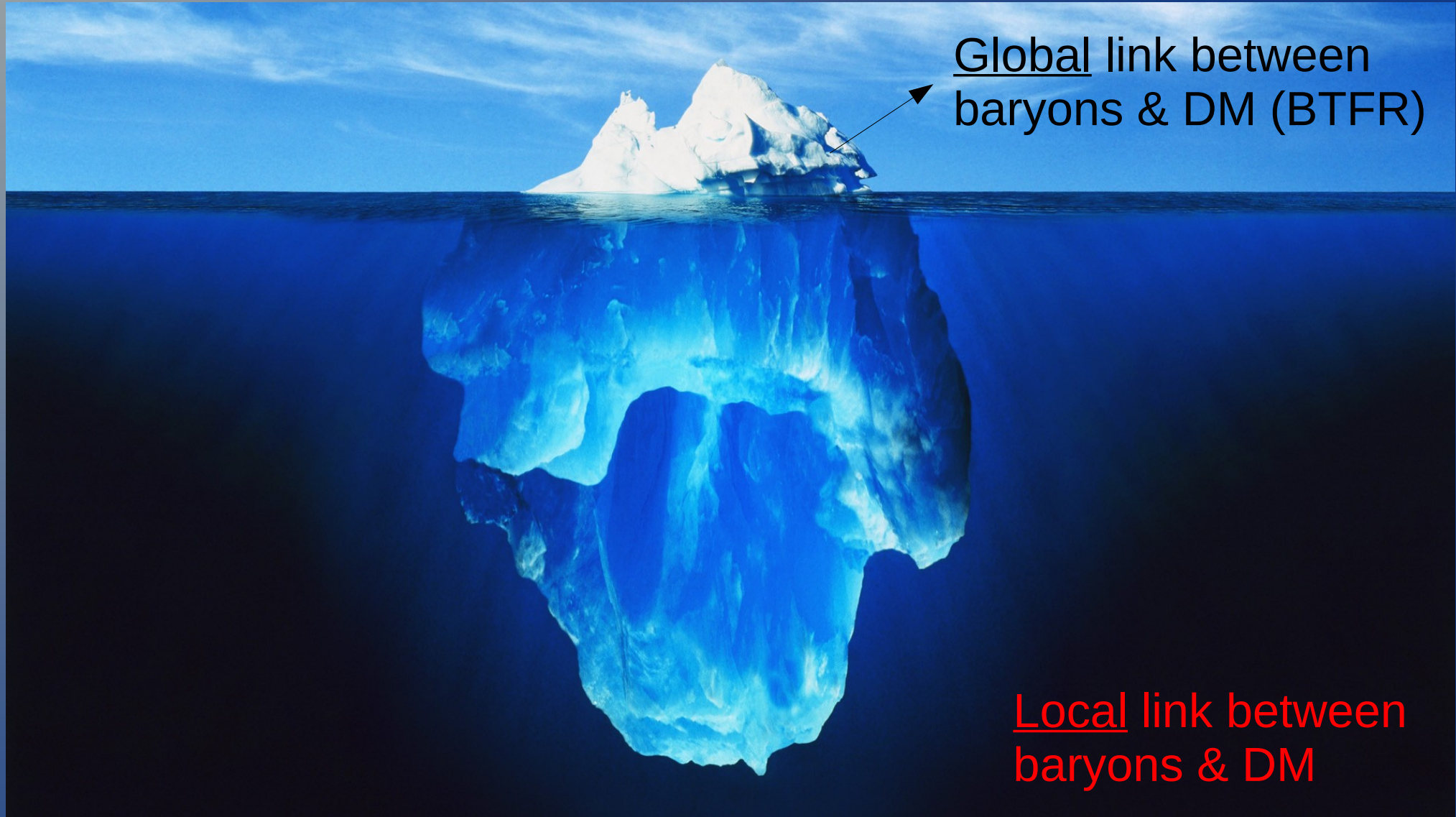


In  $\Lambda$ CDM:  $M_{200} = (10GH_0)^{-1} V_{200}^3$

$f_b = M_b/M_{200}$      $f_V = V_f/V_{200}$      $\rightarrow$      $M_b = (10GH_0)^{-1} (f_b/f_V^3) V_f^3$

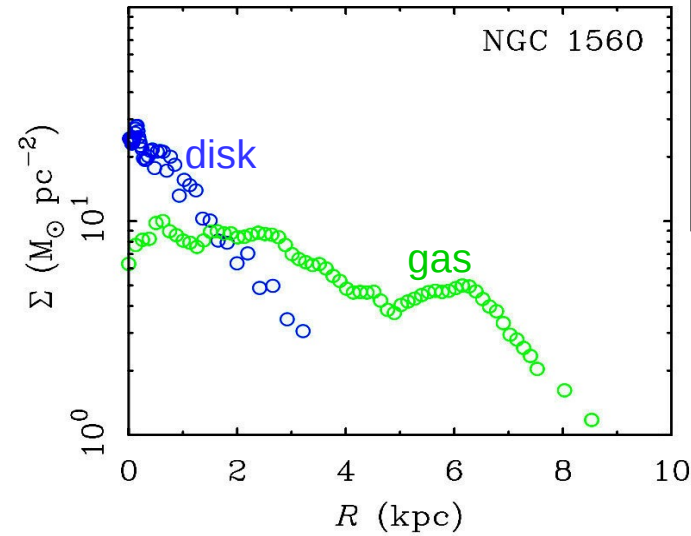
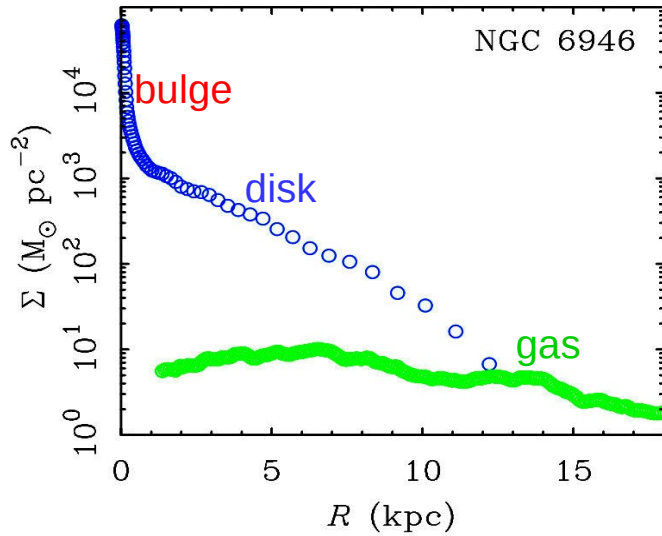
Assuming  $f_V=1$  and  $f_b=f_{\text{CMB}}$   $\rightarrow$  normalization and slope wrong!

# BTFR is only the tip of the Iceberg!

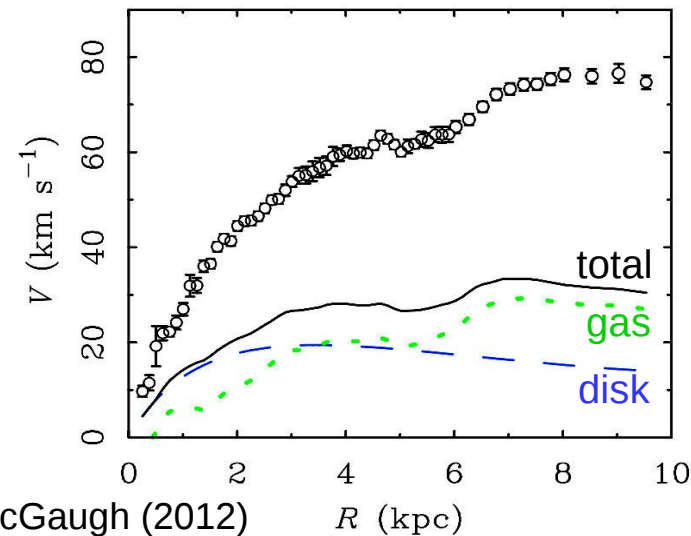
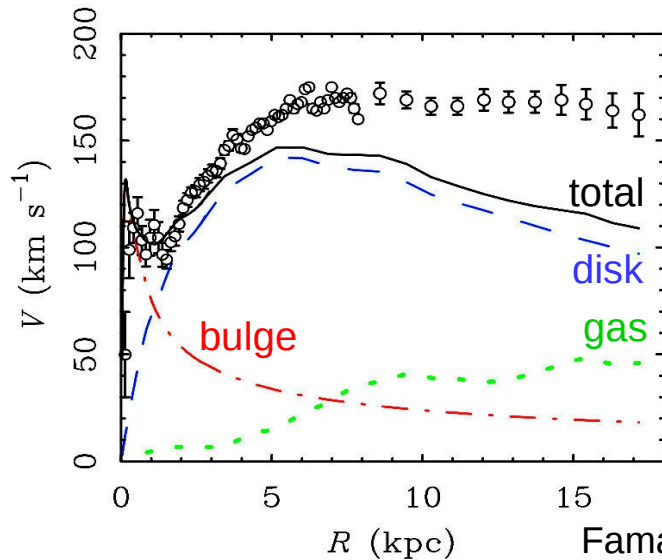


There is much more information in the shape of the rotation curve!

# Renzo's Rule



"For any feature in the **luminosity profile** of a galaxy there is a corresponding feature in the **rotation curve** and vice versa" (Sancisi 2004)



Famaey & McGaugh (2012)

R (kpc)

**Confirmed over the years:** Kent 1987; Corradi & Capaccioli 1991; Casertano & van Gorkom 1991; Broeils 1992; McGaugh & de Blok 1998; McGaugh 2004, 2005; Noordermeer+2007; Swaters+2009, 2012; Lelli+2010, 2012a,b



Can we quantify this Baryon-Dark Matter coupling with some empirical scaling law?

# SPARC

**Spitzer Photometry & Accurate Rotation Curves**



Database for 175 LTGs (spirals and irregulars):

[www.astroweb.cwru.edu/SPARC](http://www.astroweb.cwru.edu/SPARC)

Lelli, McGaugh, Schombert 2016b, AJ, 152, 157

- HI Rotation Curves for 175 galaxies
  - 30 years of interferometric HI observations
  - PhD theses from the University of Groningen
    - Begeman 1987; Broeils 1992; Verheijen 1997; de Blok 1997;
    - Swaters 1999; Noordermeer 2005; Lelli 2013 + other studies
  - Hybrid H $\alpha$ /HI rotation curves for ~30% sample





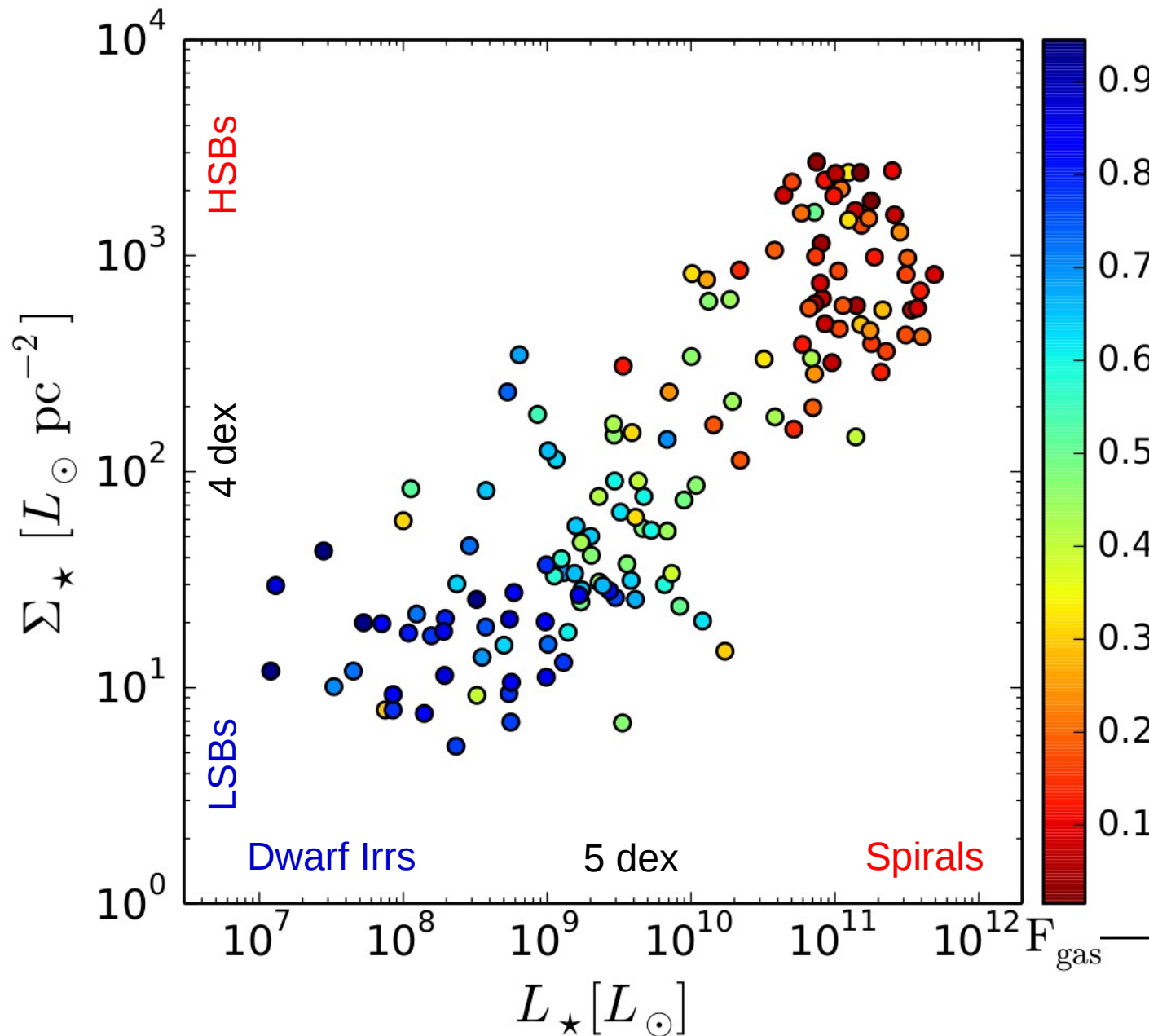
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  - Hybrid H $\alpha$ /HI rotation curves for ~30% sample



- Homogeneous Photometry at 3.6  $\mu\text{m}$ 
  - Optimal tracer of the stellar mass:  $M_* = Y_* L$
  - $Y_*$  is roughly constant in the NIR (~0.1 dex)
    - Bell & de Jong 2001; Bell+2003; Portinari+2004; Meidt+2014; Schombert & McGaugh 2014; McGaugh & Schombert 2014



# Widest possible range of disk properties



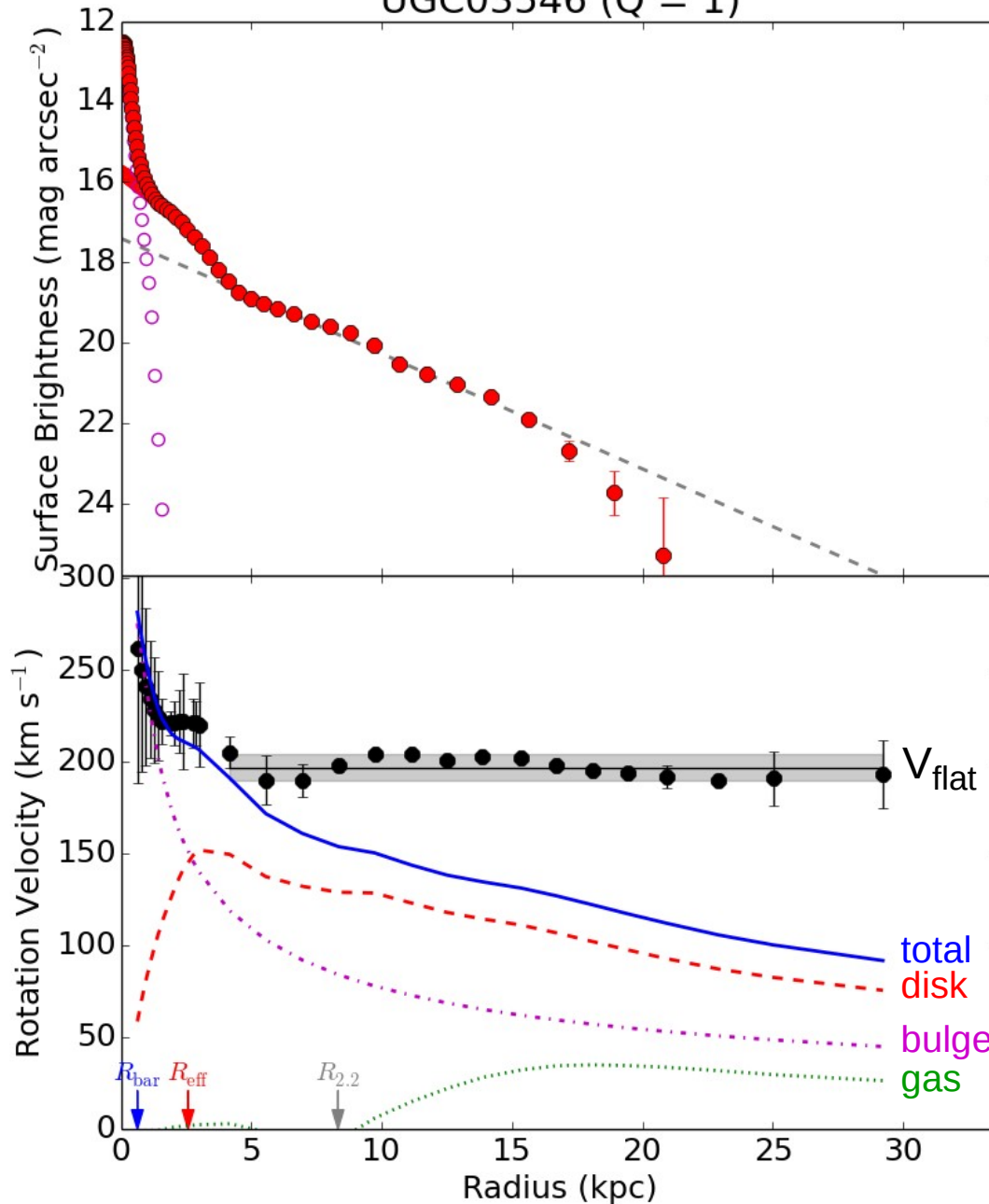
Basically any known galaxy type with a rotating HI disk.



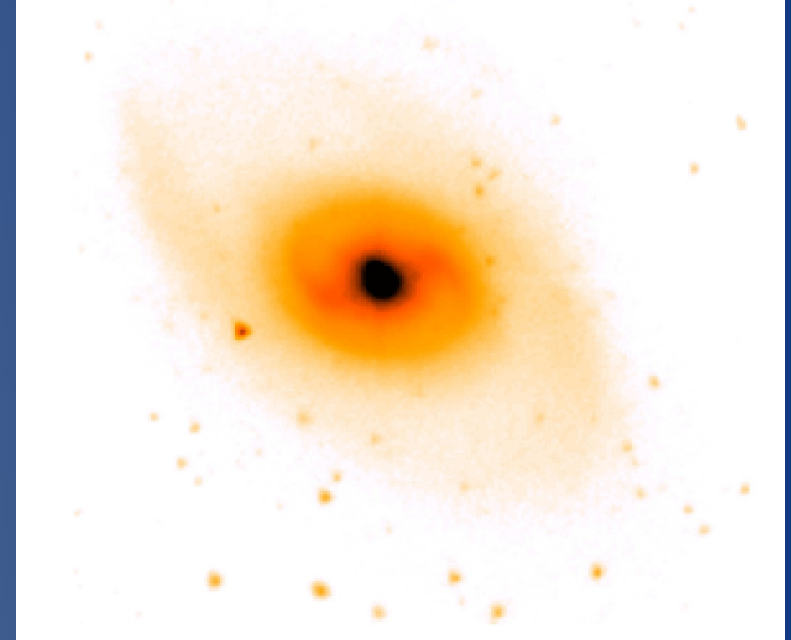
$M_{\text{gas}}/M_{\text{bar}}$

# Example: High-Mass HSB Spiral

UGC03546 (Q = 1)



Spitzer 3.6  $\mu\text{m}$



$$\nabla^2 \Phi_{\text{bar}}(R, z) = 4\pi G \rho_{\text{bar}}(R, z)$$

- Vertical Structure:

Disks:  $\exp(-z/h_z)$  with  $h_z \propto h_R$

Bulges: spherical symmetry

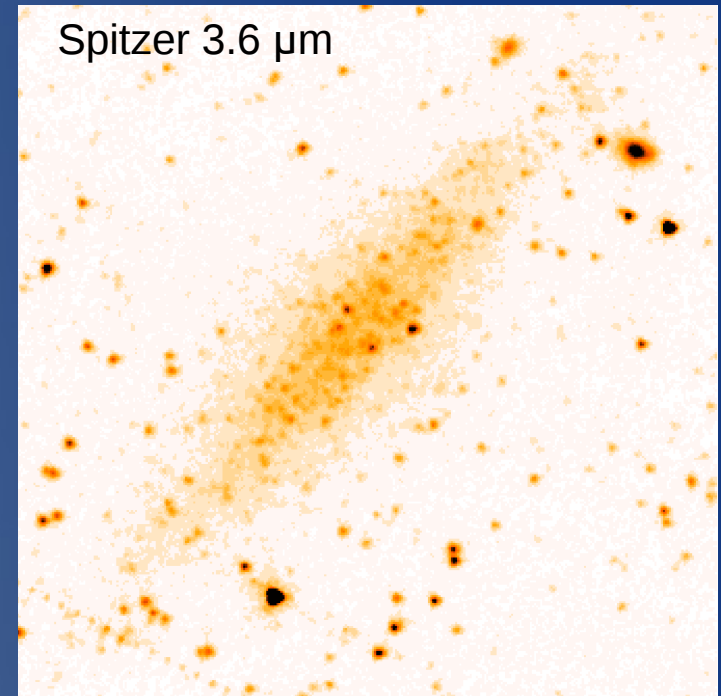
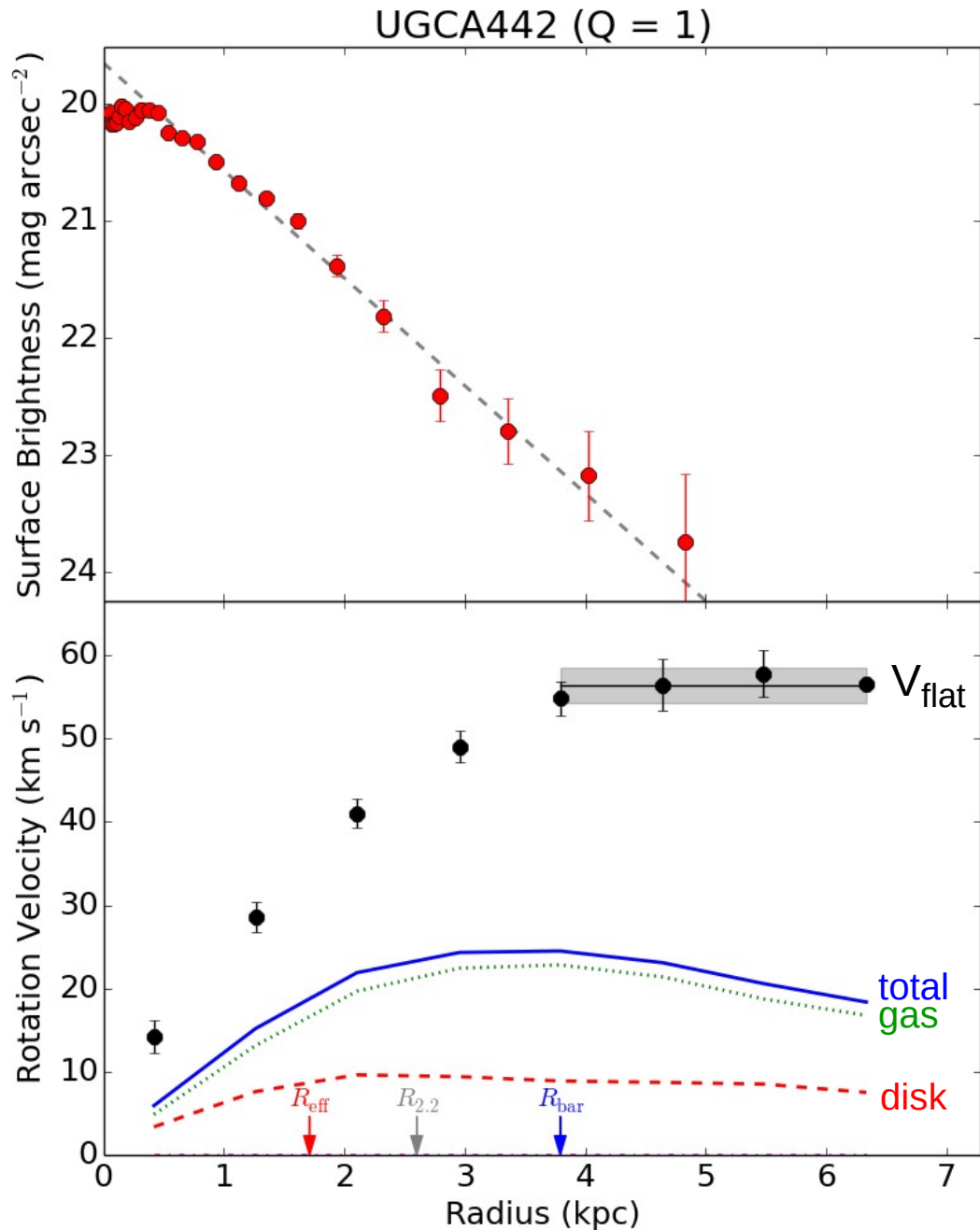
- Stellar mass-to-light ratio:

$\Upsilon_* = 0.5 M_\odot/L_\odot$  for disks

$\Upsilon_* = 0.7 M_\odot/L_\odot$  for bulges



# Example: Low-Mass LSB Dwarf



$$\nabla^2 \Phi_{\text{bar}}(R, z) = 4\pi G \rho_{\text{bar}}(R, z)$$

- Vertical Structure:

Disks:  $\exp(-z/h_z)$  with  $h_z \propto h_R$

Bulges: spherical symmetry

- Stellar mass-to-light ratio:

$\Upsilon_* = 0.5 M_{\odot}/L_{\odot}$  for disks

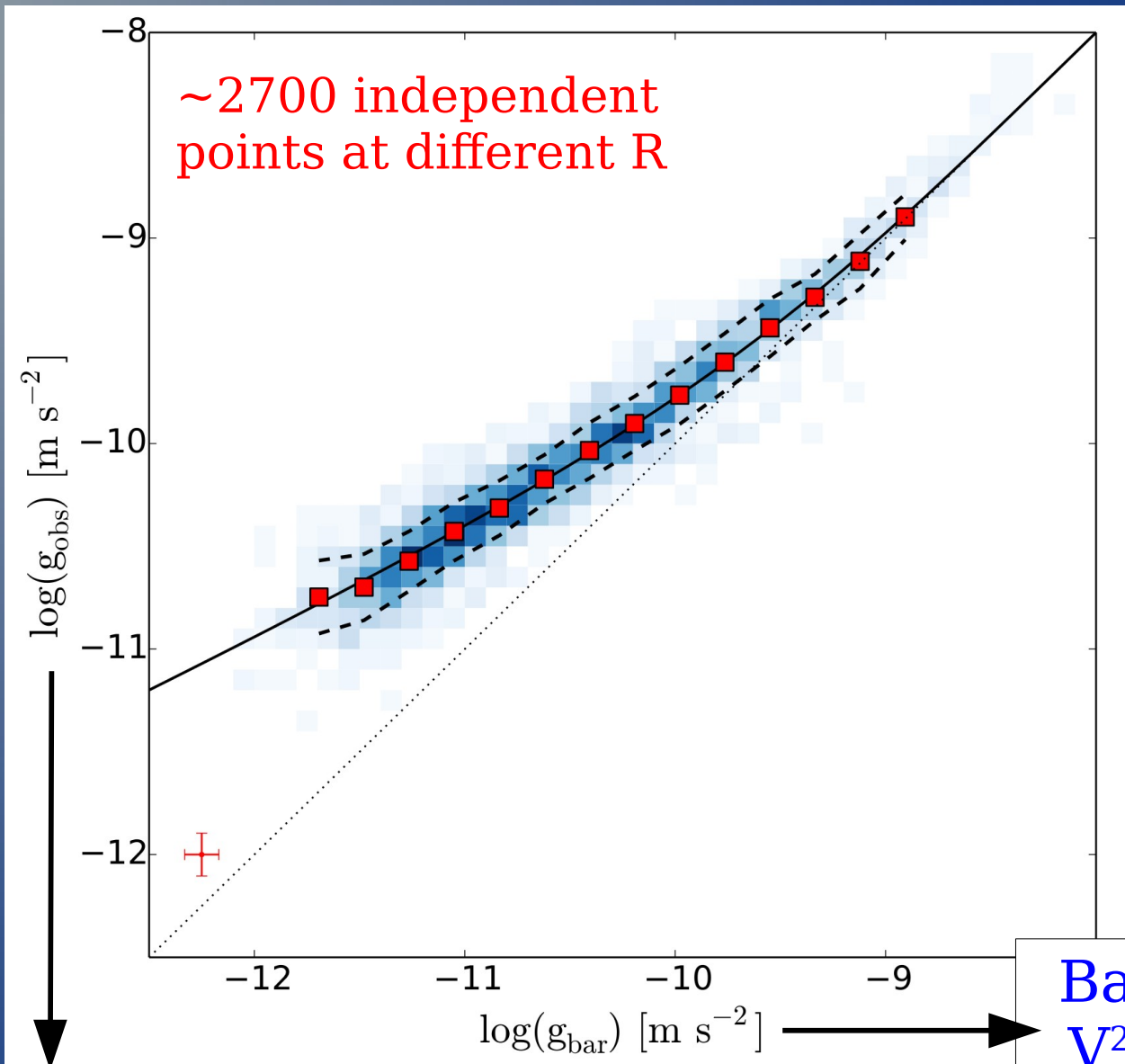
$\Upsilon_* = 0.7 M_{\odot}/L_{\odot}$  for bulges

# III. Radial Acceleration Relation

McGaugh, Lelli, Schombert 2016, PRL, 117, 201101

Lelli, McGaugh, Schombert, Pawlowski 2016d, submitted to ApJ

# Local link between baryons and DM



~2700 independent points at different R

For all galaxies:

$$\Upsilon_{\text{disk}} = 0.5 M_{\odot}/L_{\odot}$$

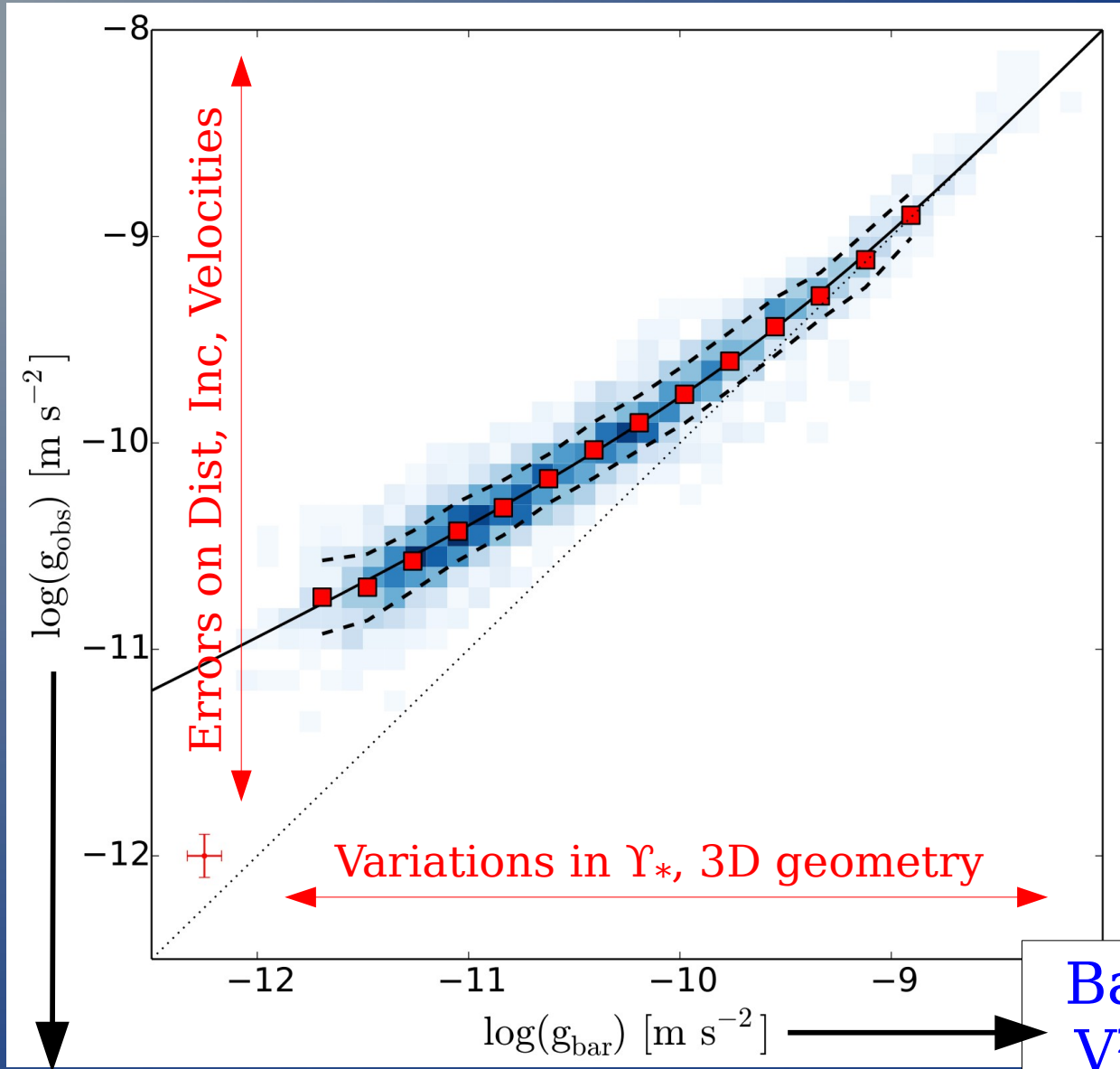
$$\Upsilon_{\text{bulge}} = 0.7 M_{\odot}/L_{\odot}$$

Total Acceleration:  $V_{\text{obs}}^2/R = -\nabla\Phi_{\text{tot}}$

Baryonic Force:  
 $V_{\text{bar}}^2/R = -\nabla\Phi_{\text{bar}}$   
 $\nabla^2\Phi_{\text{bar}} = 4\pi G \rho_{\text{bar}}$



# Local link between baryons and DM



For all galaxies:

$$\Upsilon_{\text{disk}} = 0.5 M_{\odot}/L_{\odot}$$

$$\Upsilon_{\text{bulge}} = 0.7 M_{\odot}/L_{\odot}$$

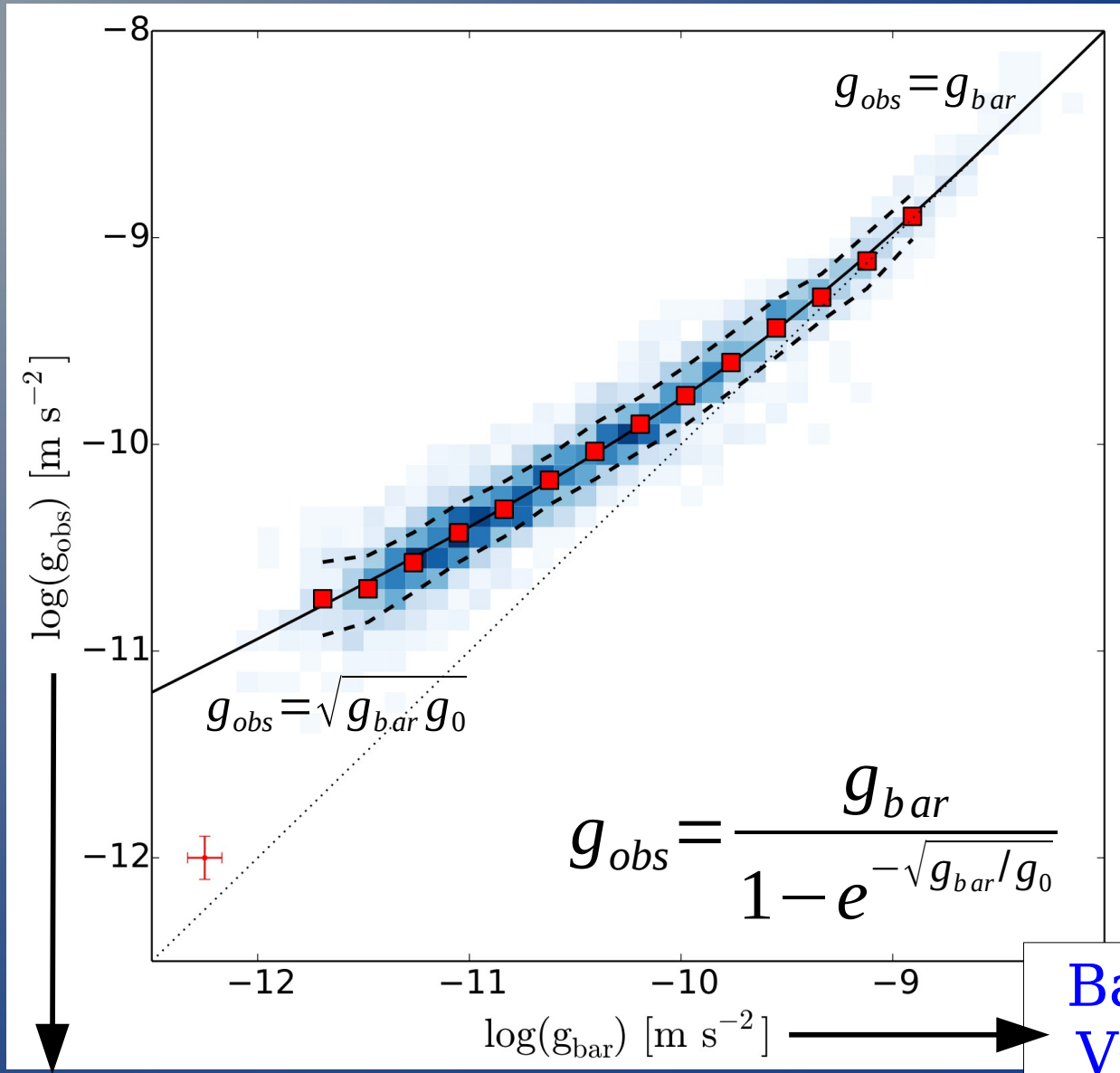
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# Local link between baryons and DM



For all galaxies:

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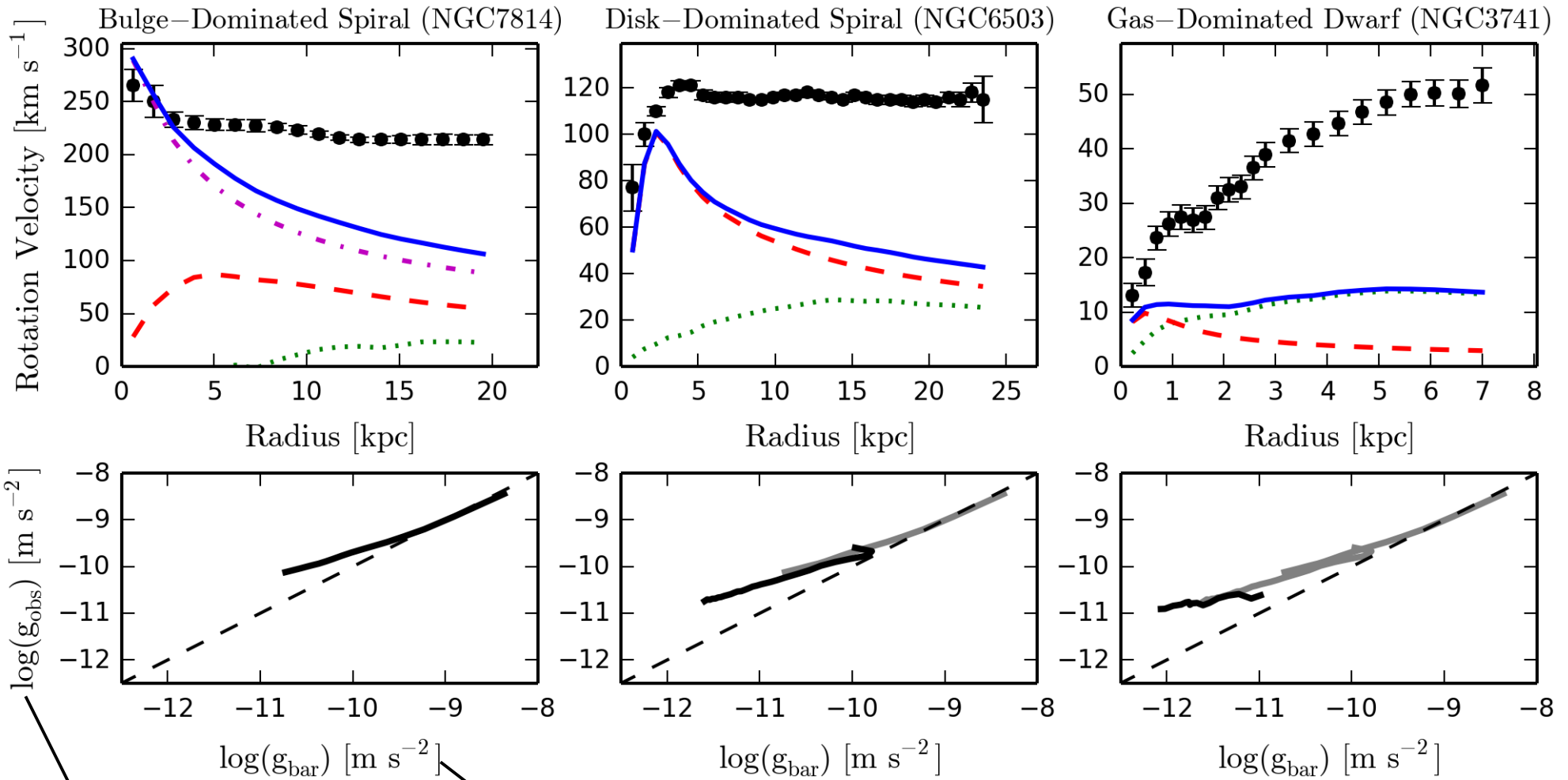
Total Acceleration:  $V_{obs}^2/R = -\nabla\Phi_{tot}$

Baryonic Force:

$$V_{bar}^2/R = -\nabla\Phi_{bar}$$

$$\nabla^2\Phi_{bar} = 4\pi G \rho_{bar}$$

# Very different galaxies but ONE relation



$$V_{\text{obs}}^2 / R = -\nabla\Phi_{\text{tot}}$$

$$V_{\text{bar}}^2 / R = -\nabla\Phi_{\text{bar}}$$

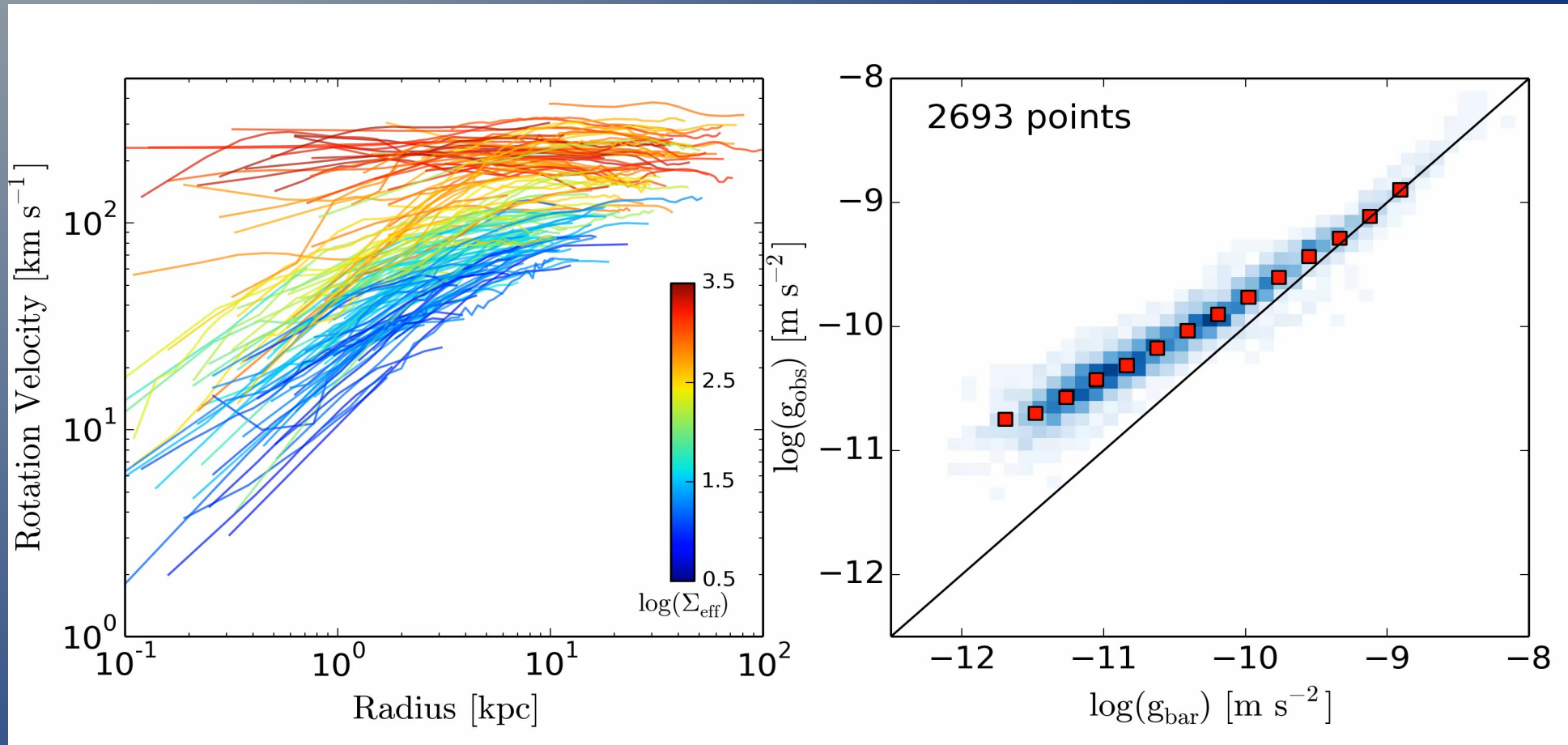
$$\nabla^2\Phi_{\text{bar}} = 4\pi G \rho_{\text{bar}}$$

McGaugh, Lelli, Schombert (2016)

# Building up the Radial Acceleration Relation

Large Diversity in Rotation Curves

Regularity in Acceleration Plane

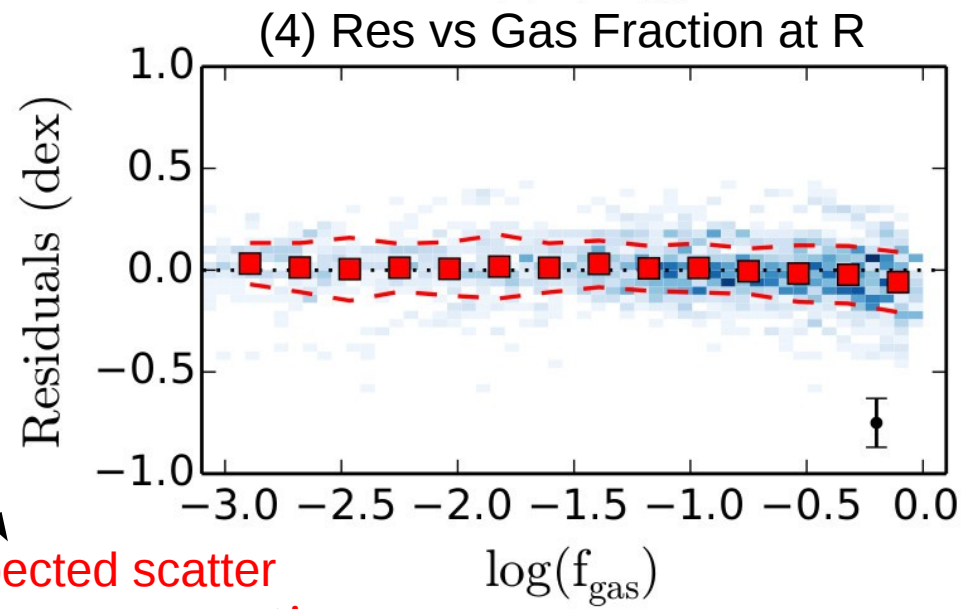
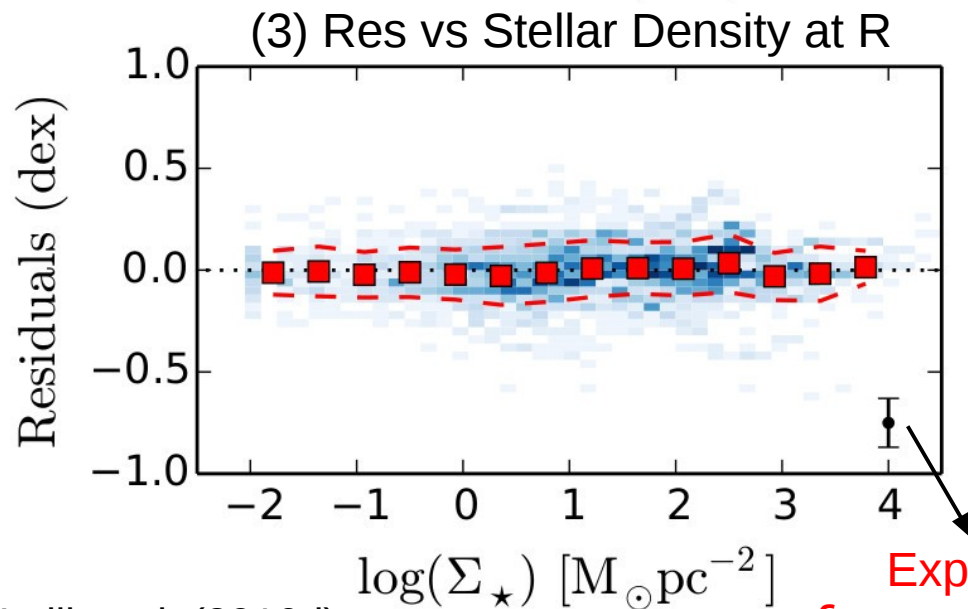
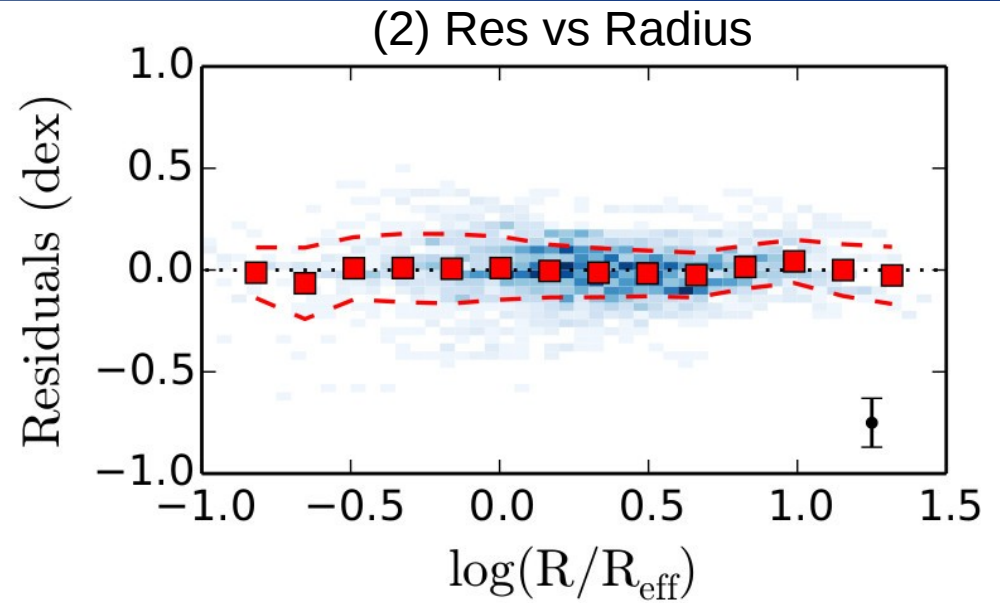
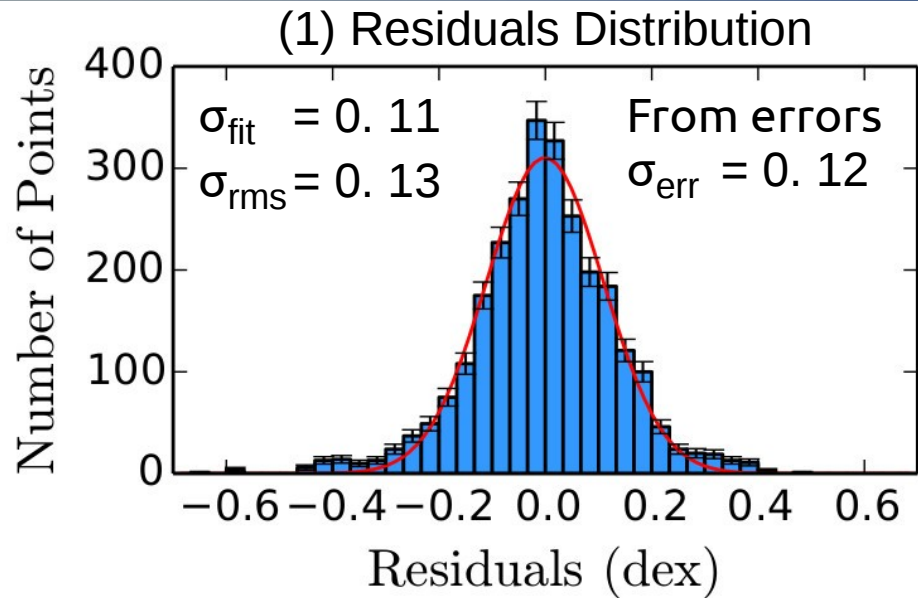


Lelli et al. 2016d, submitted to AJ

Video available at [astroweb.cwru.edu/SPARC/](http://astroweb.cwru.edu/SPARC/)



# Scatter and Residuals around the RAR



Lelli et al. (2016d)

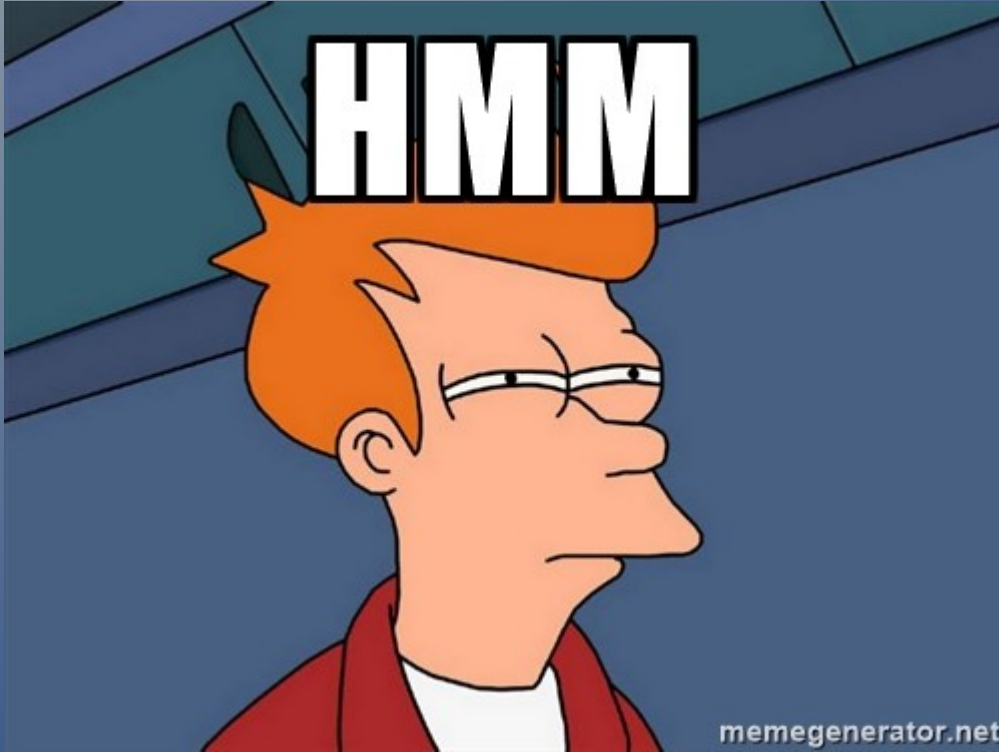
Expected scatter  
from error propagation

# We can infer the DM distribution from $g_{bar}$ !

From the observations:  $g_{DM} = g_{tot} - g_{bar} = F(g_{bar}) - g_{bar}$

For a spherical DM halo:  $M_{DM}(R) = \frac{R^2}{G} [F(g_{bar}) - g_{bar}]$

For our fiducial fitting F:  $M_{DM}(R) = \frac{R^2}{G} \frac{g_{bar}}{\exp(\sqrt{g_{bar}/g_0}) - 1}$

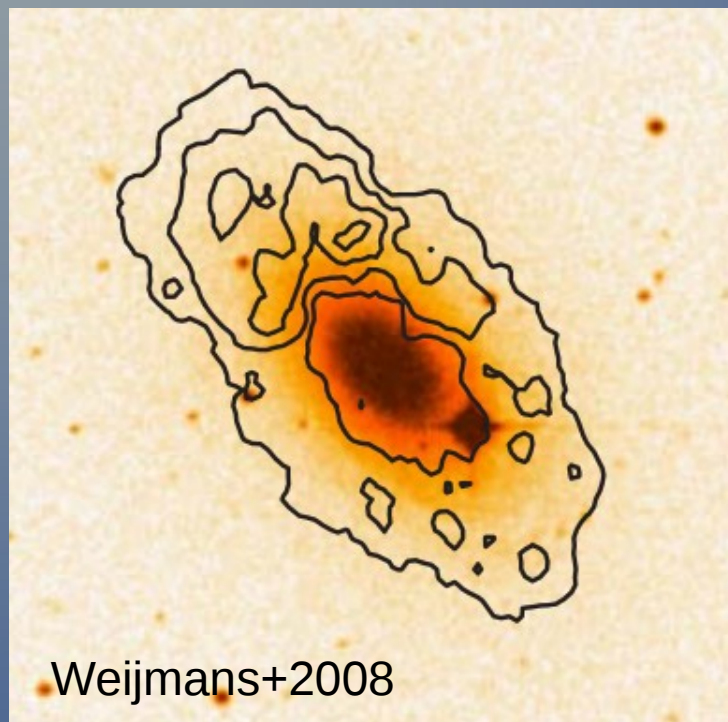


**OK. This works for  
LTGs, but...  
what about ETGs?**

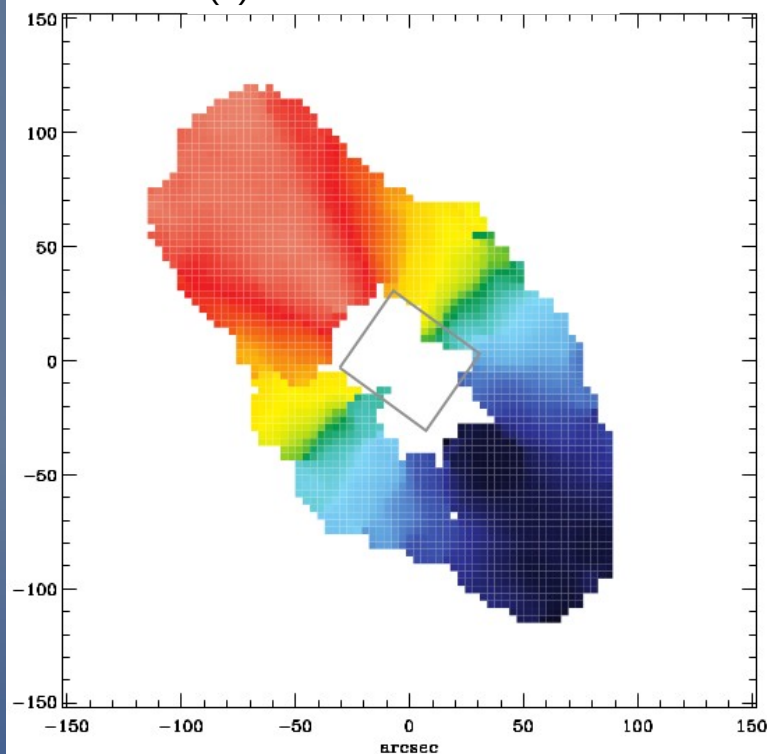


# Early-Type Galaxies with outer HI rings/disks

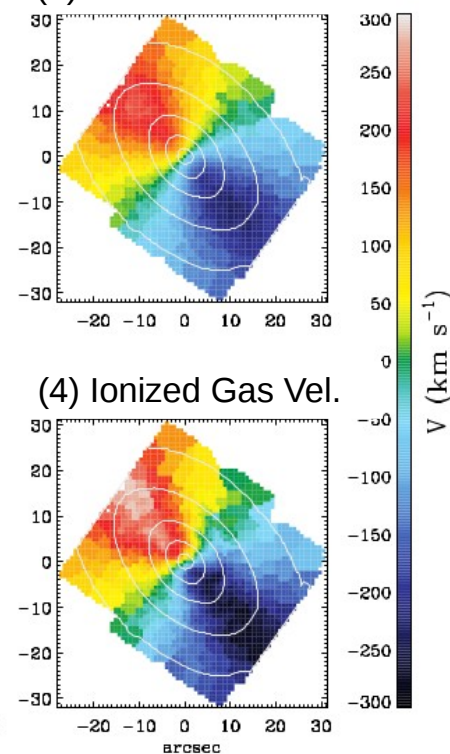
(1) Stars + Neutral Gas Map



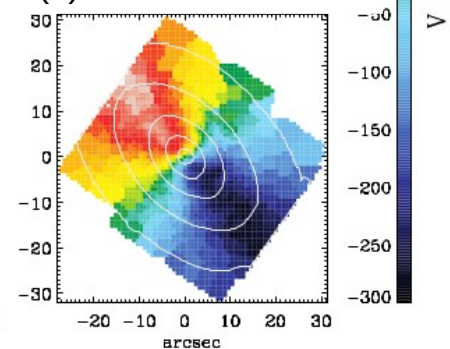
(2) Neutral Gas Velocities



(3) Stellar Velocities



(4) Ionized Gas Vel.



Key results from Atlas<sup>3D</sup> Survey (Cappellari+2010; Serra+2011)

- 85% of ETGs have rotating stellar components (but  $V_*/\sigma_* < 1$ )
- 20% of ETGs have rotating, low-density HI disks or rings

**Our Sample:** 16 ETGs with both stellar rotation and outer HI disks

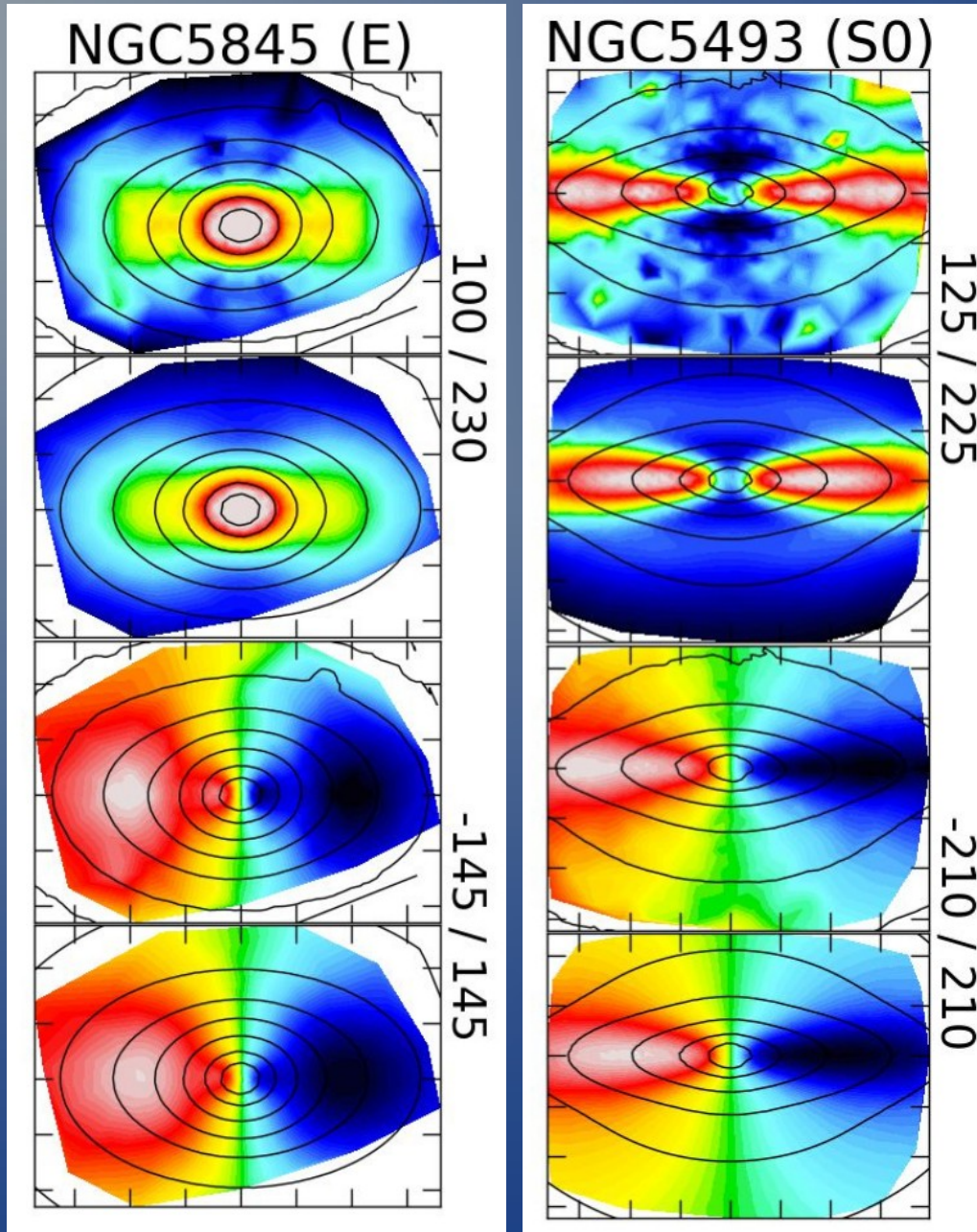
# Jeans Axisymmetric Models (JAM)

Observed  
 $\sqrt{(V^2 + \sigma^2)}$

Model  
 $\sqrt{(V^2 + \sigma^2)}$

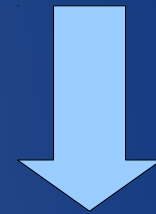
Observed  
Velocities

Model  
Velocities



## Assumptions:

- Axial Symmetry
- $\sigma_\theta = \sigma_R > \sigma_z$
- Mass follows light
- M/L constant with R

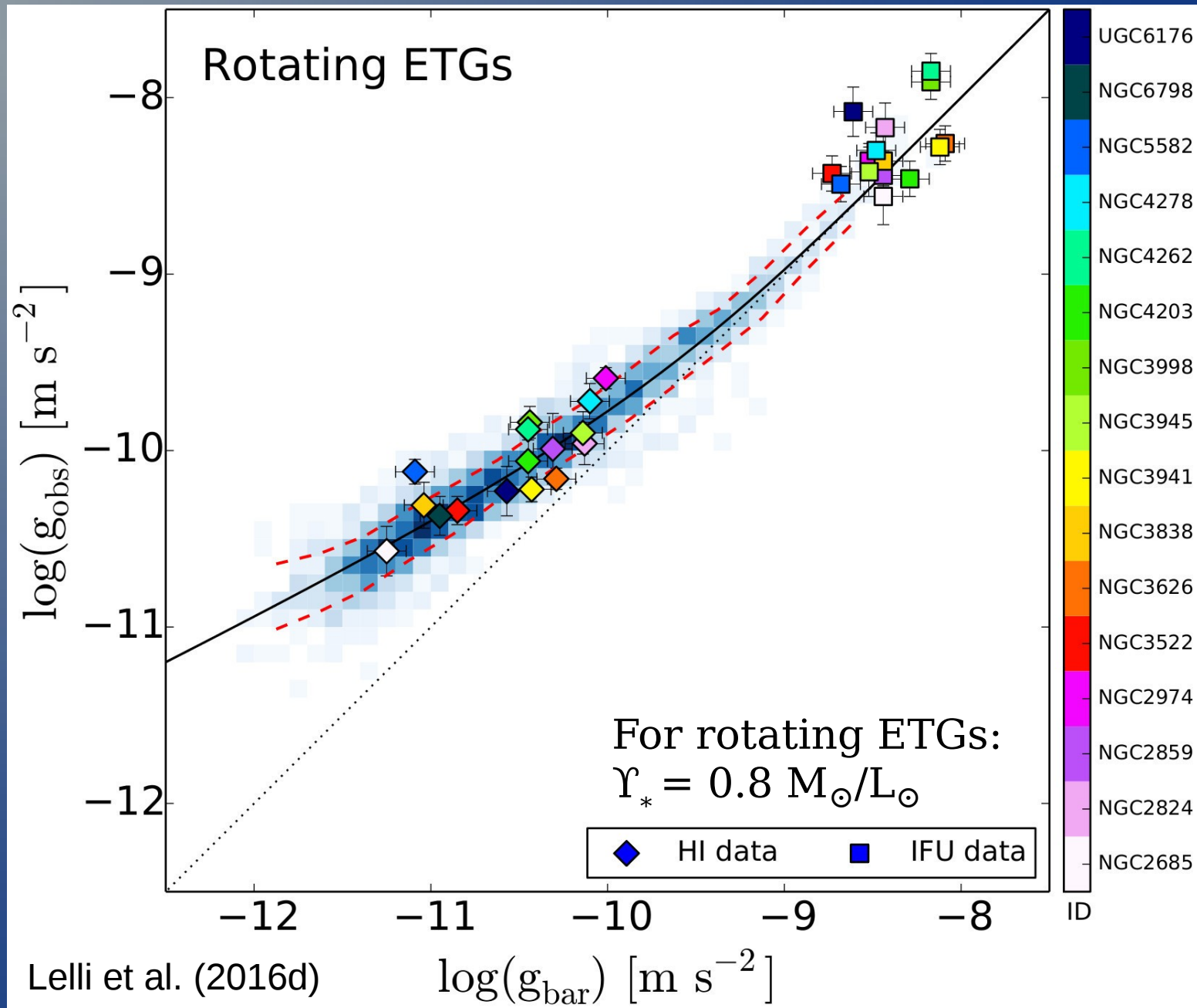


$$V_{\max} = \max \text{ circular } V$$

$$g_{\text{obs}} = V_{\max}^2 / R_{\max}$$

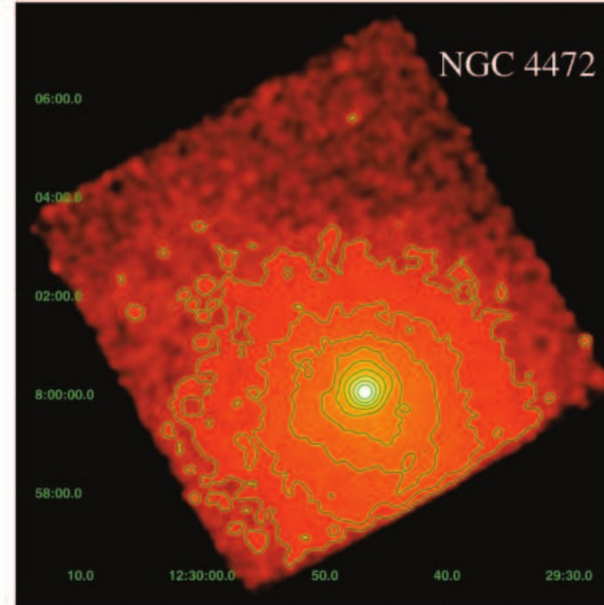
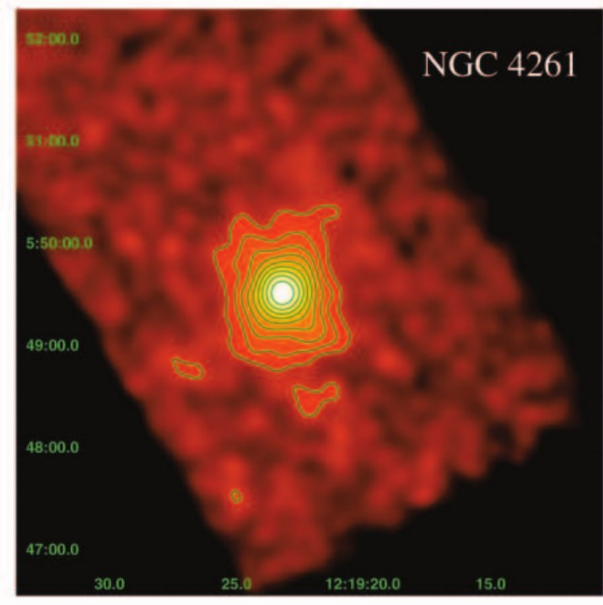
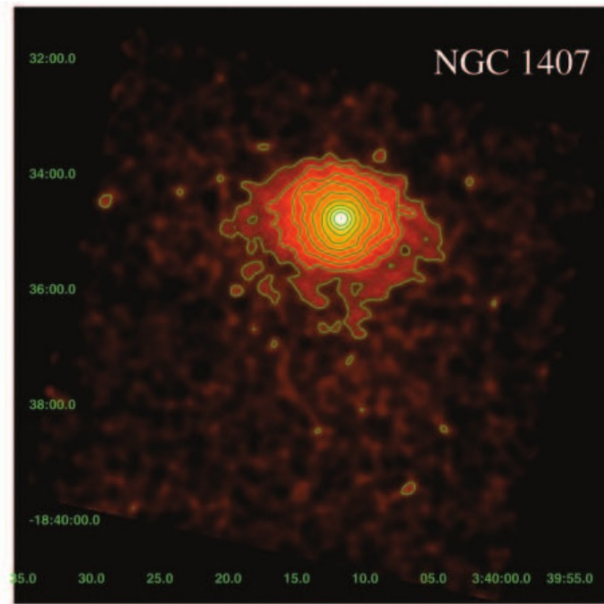
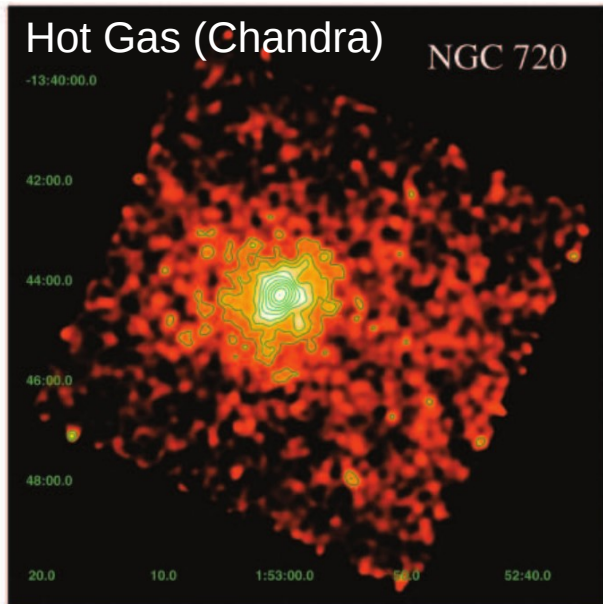
Cappellari+(2013, 2016)

# Rotating ETGs follow the same RAR as LTGs



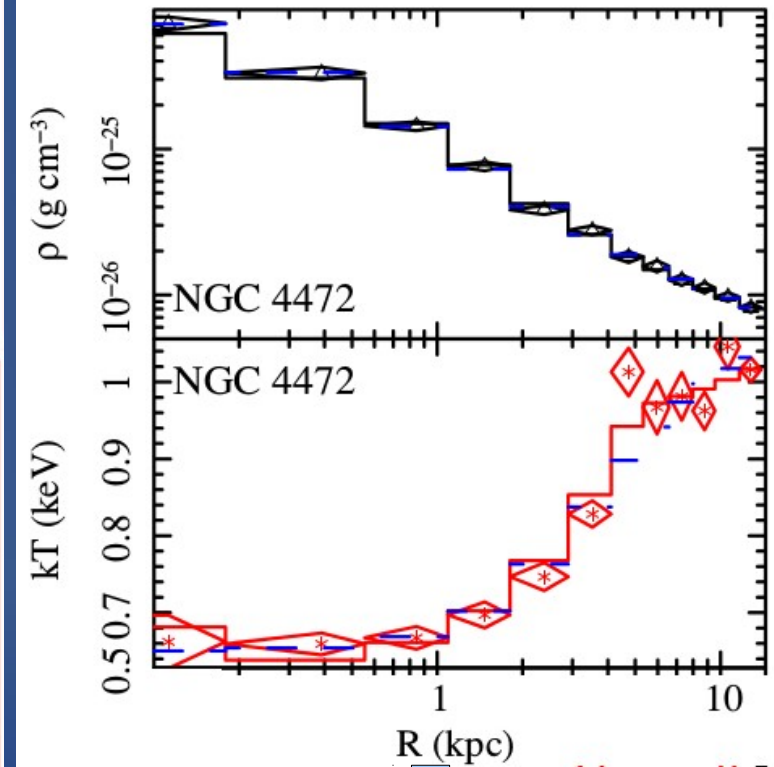


# Non-rotating Massive Ellipticals: X-ray haloes



Hydrostatic equilibrium:

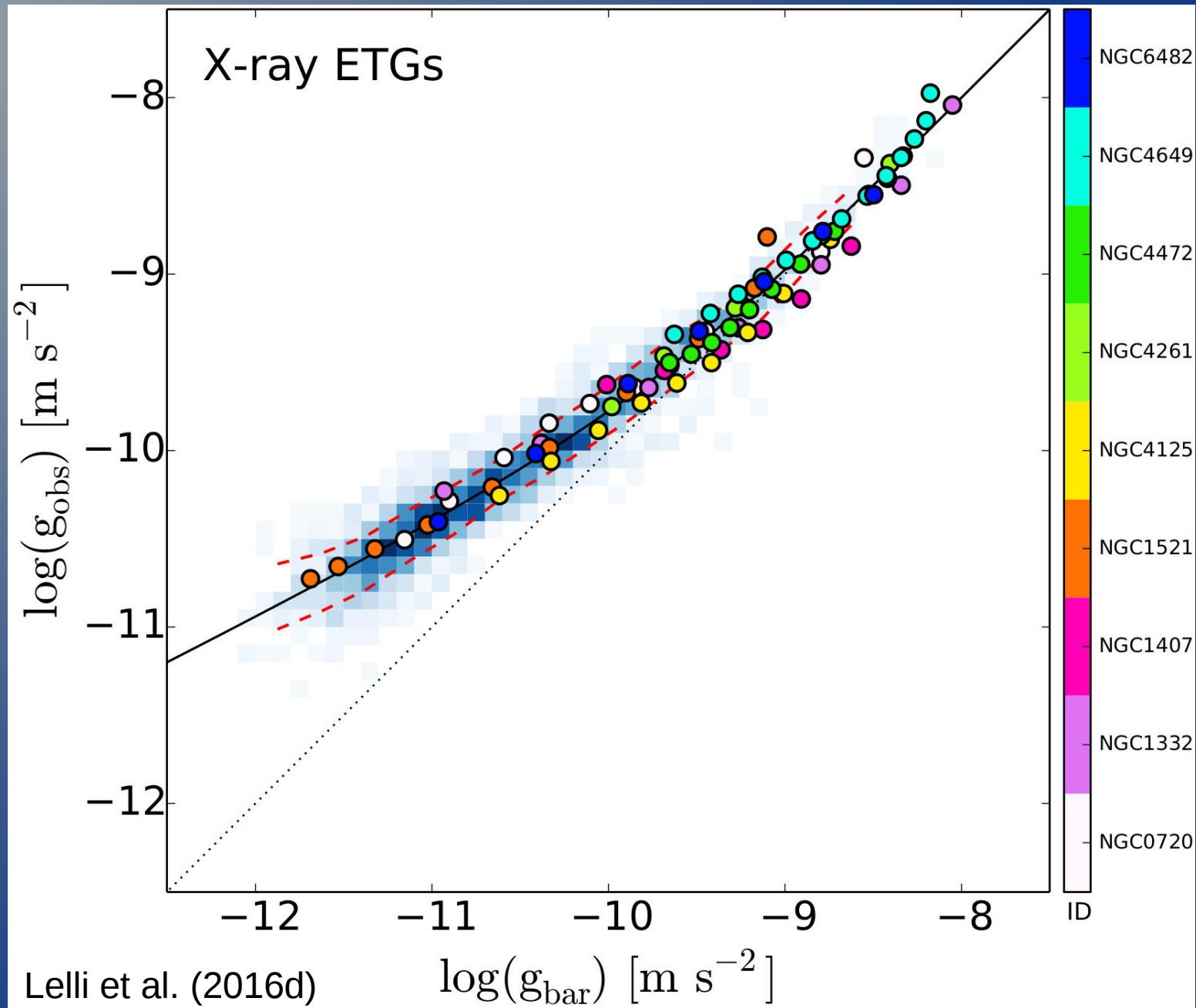
$$M(< r) = - \left[ \frac{rk_B T}{\mu m_a G} \right] \left[ \frac{d \ln \rho_{\text{gas}}}{d \ln r} + \frac{d \ln T}{d \ln r} \right]$$



$$g_{\text{obs}}(r) = -\nabla \Phi_{\text{tot}}(r) = \frac{GM_{\text{tot}}(< r)}{r^2}$$

Our sample: 9 X-ray ETGs from Humphrey+(2006, 2009, 2011, 2012)

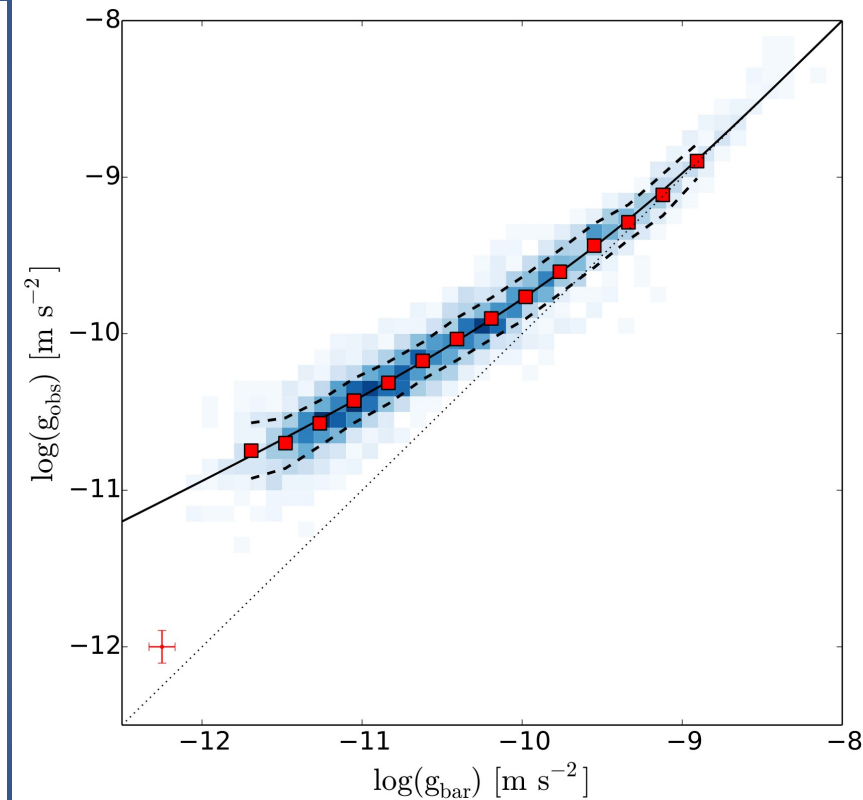
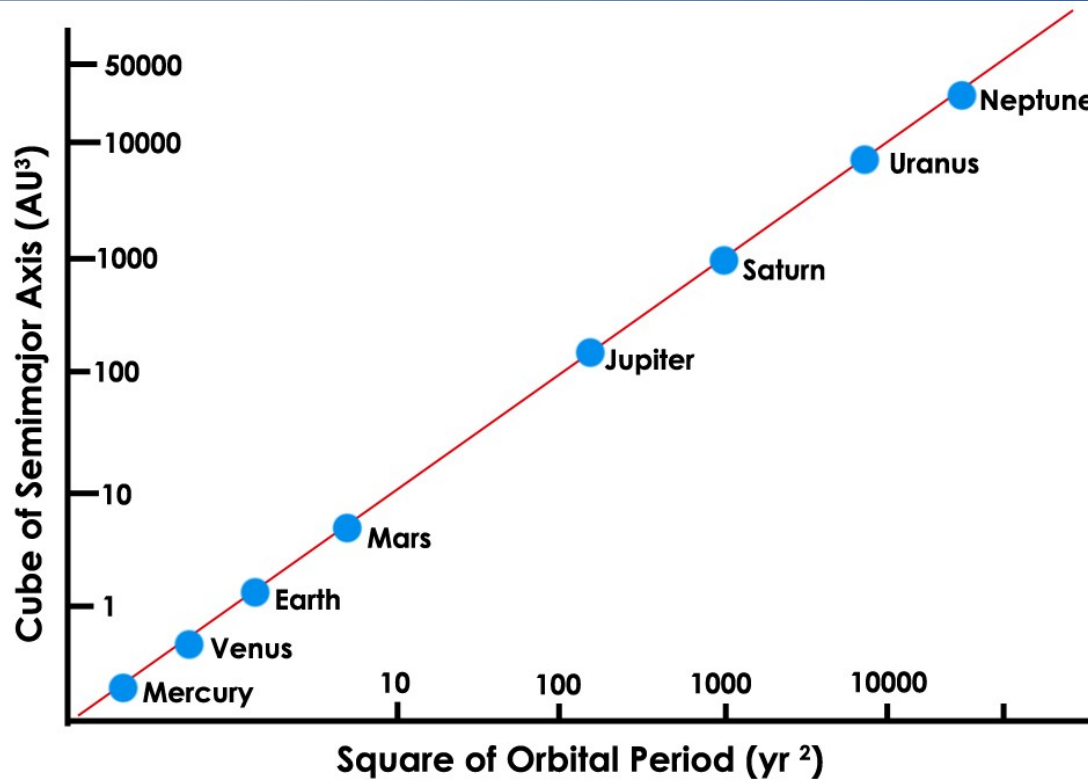
# X-ray ETGs follow the same RAR as LTGs



# A "Kepler" Law for Galaxies?

3rd Law of Kepler:  $a \leftrightarrow P$

RAR:  $g_{\text{bar}} \leftrightarrow g_{\text{obs}}$



The RAR follows with a **minimum set of assumptions**:

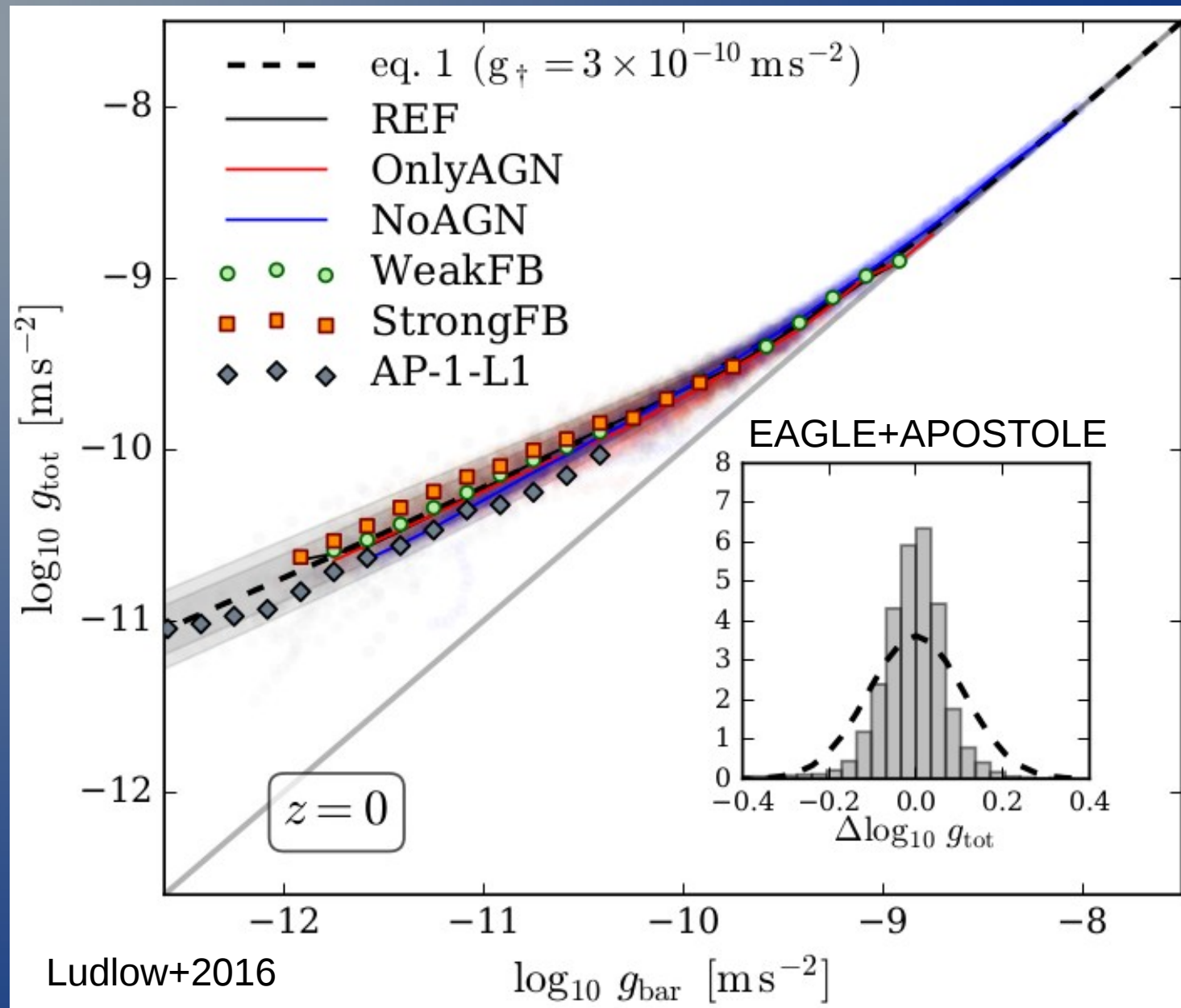
Poisson's Equation + stellar mass-to-light ratio

# Possible Interpretations:

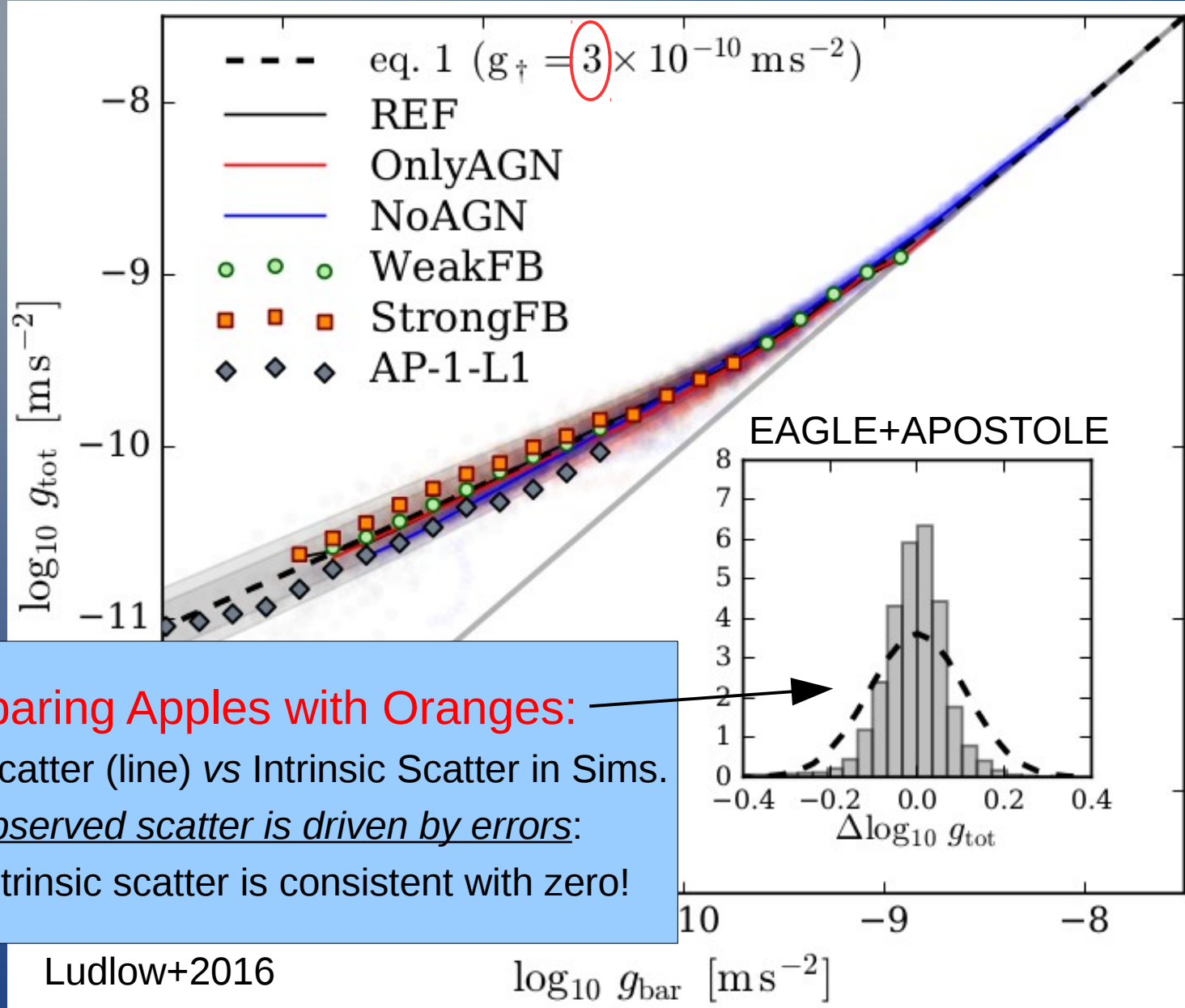
1. End product of galaxy formation in  $\Lambda$ CDM
2. New Dynamical Laws instead of DM
3. New Physics in the Dark Sector / Dark Forces



# RAR from Cosmological Simulations?



# RAR from Cosmological Simulations?



## Comparing Apples with Oranges:

Observed Scatter (line) vs Intrinsic Scatter in Sims.

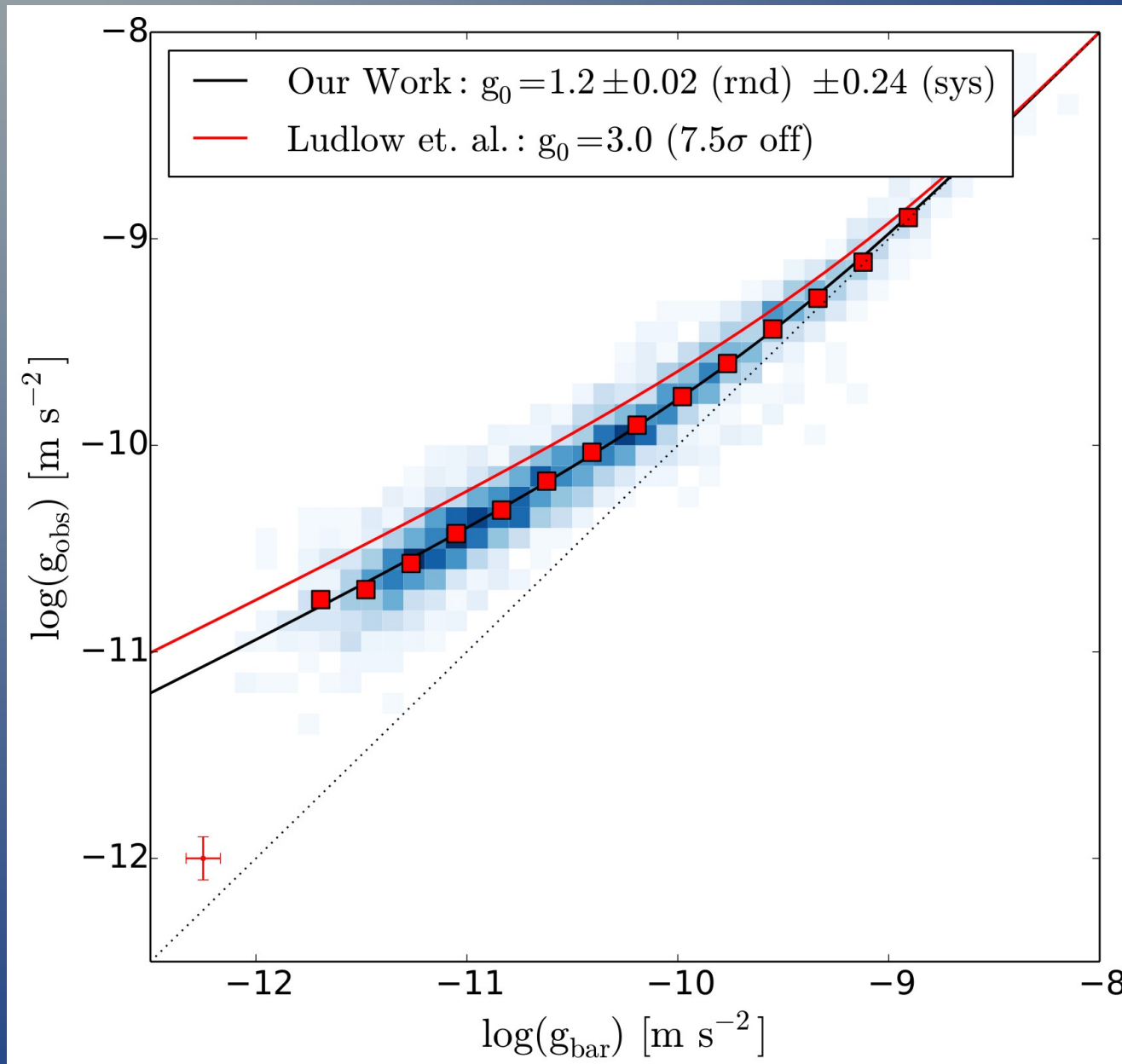
BUT observed scatter is driven by errors:

the real intrinsic scatter is consistent with zero!

Ludlow+2016

$\log_{10} g_{\text{bar}} [\text{ms}^{-2}]$

# Actual Comparison with the data



Persistent issue for sims:

Too much DM in galaxies!  
e.g. Cusp-Core Problem,  
Too-Big-Too-Fail Problem

Other conceptual issues:

Why an acceleration scale?  
Why the outer slope is 0.5?  
Correlations with residuals?

# Possible Interpretations:

1. End product of galaxy formation in  $\Lambda$ CDM

**NB:** "cusp-core", "too-big-to-fail" are symptoms of a more serious illness.

**Issues:** Stochastic and complex process. Why is scatter so small (if any)?

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**NB:** MOND predicted the RAR before the data existed (Milgrom 1983)

**Issues:** CMB? Large-scale structure of the Universe? Galaxy clusters?

## 3. New Physics in the Dark Sector / Dark Forces

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## 3. New Physics in the Dark Sector / Dark Forces

Dipolar DM (Blanchet & Le Tiec 2008, 2009) }  
Dark Superfluid (Khoury 2015) } Hybrids ( $\Lambda$ CDM + MOND)

**Issues:** Adding new free parameters to  $\Lambda$ CDM is somewhat uncomfortable.

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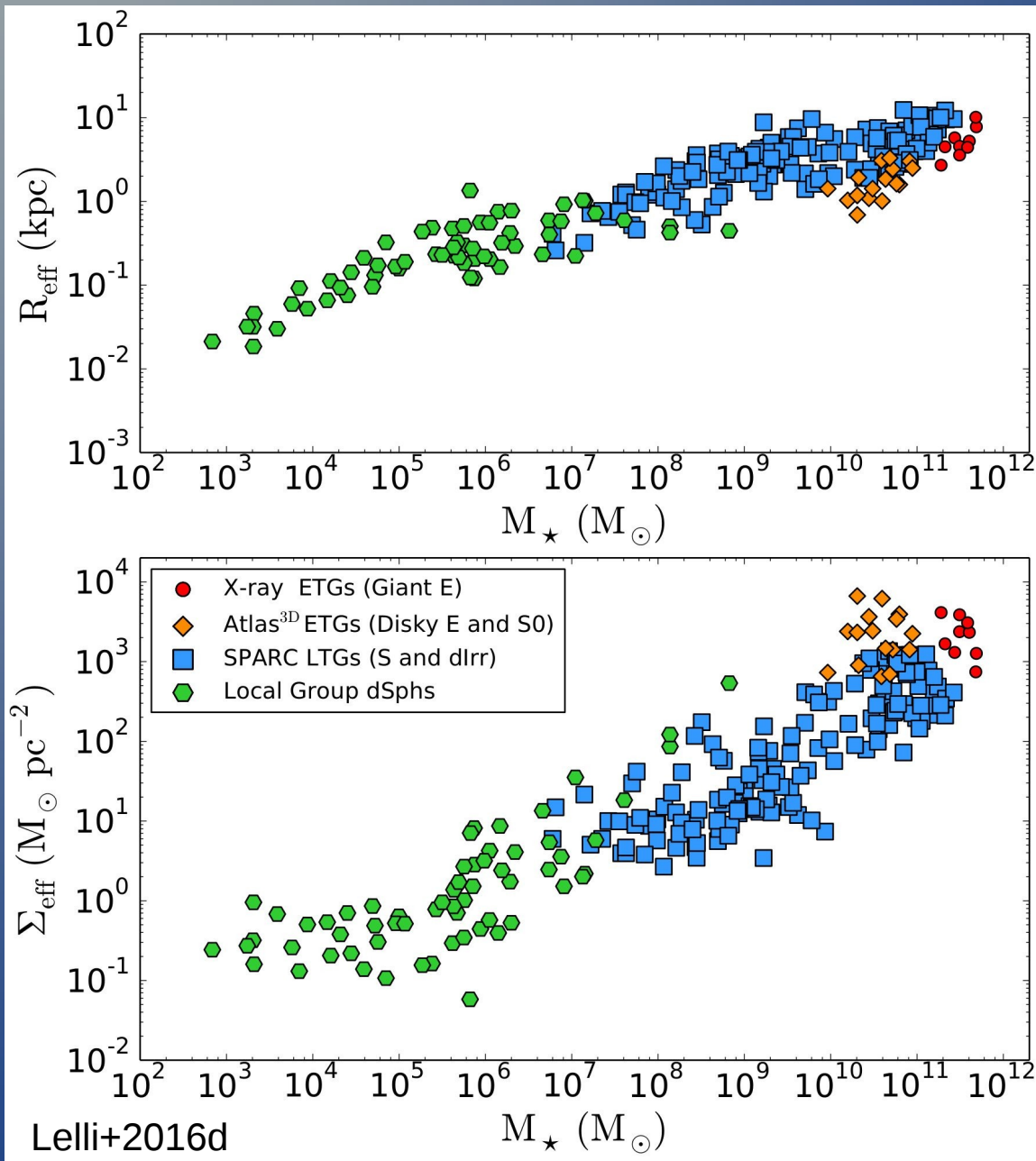


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# Additional Slides

# Dwarf Spheroidal (dSphs) in the Local Group



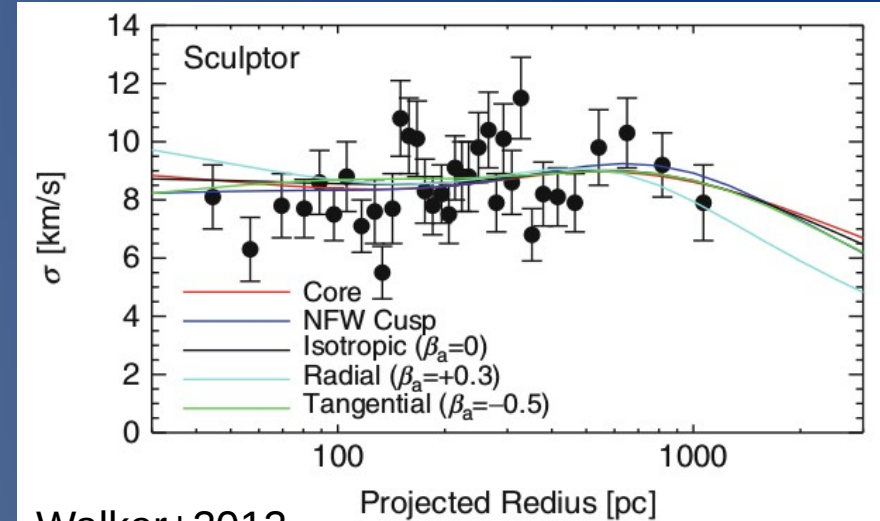
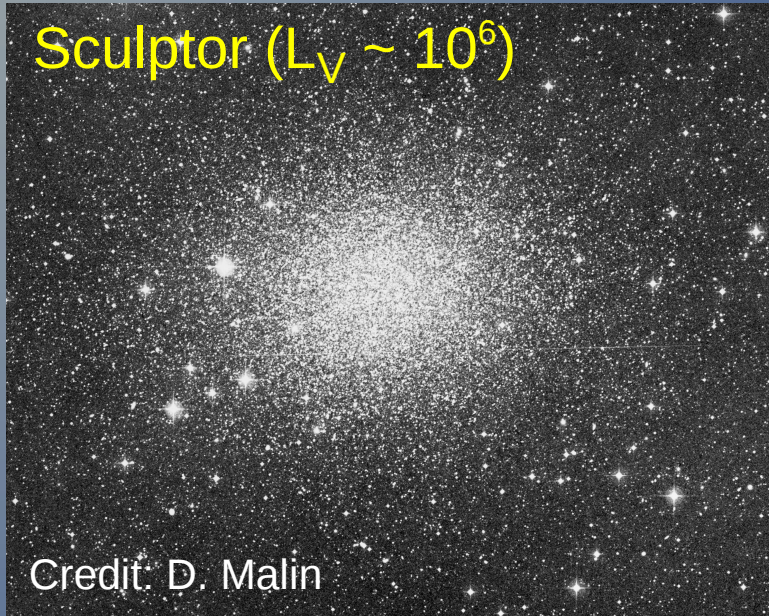
Satellites of MW and M31:  
extremely low masses, sizes,  
densities, and accelerations!

"Classical" dSphs discovered  
between the '40 and the '80.

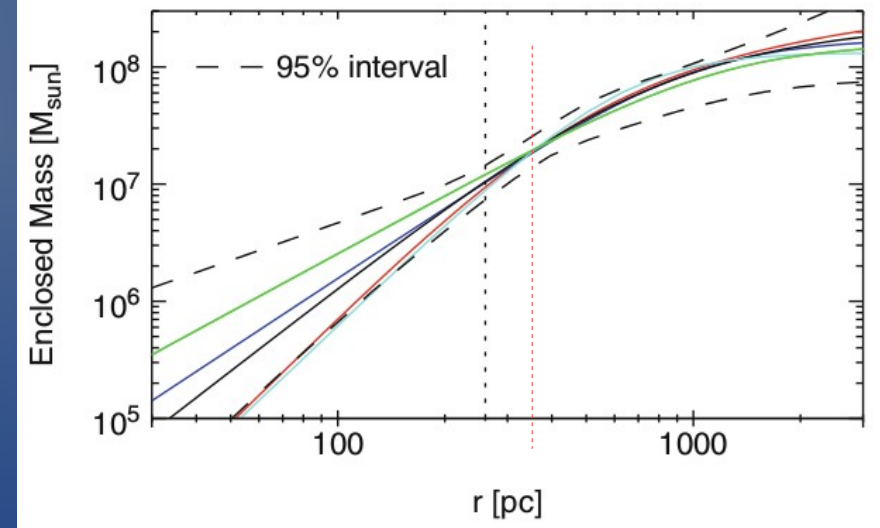
→ well-studied properties

"Ultrafaint" dSphs discovered  
during the past ~10 years with  
SDSS, DES and other surveys  
→ properties remain uncertain

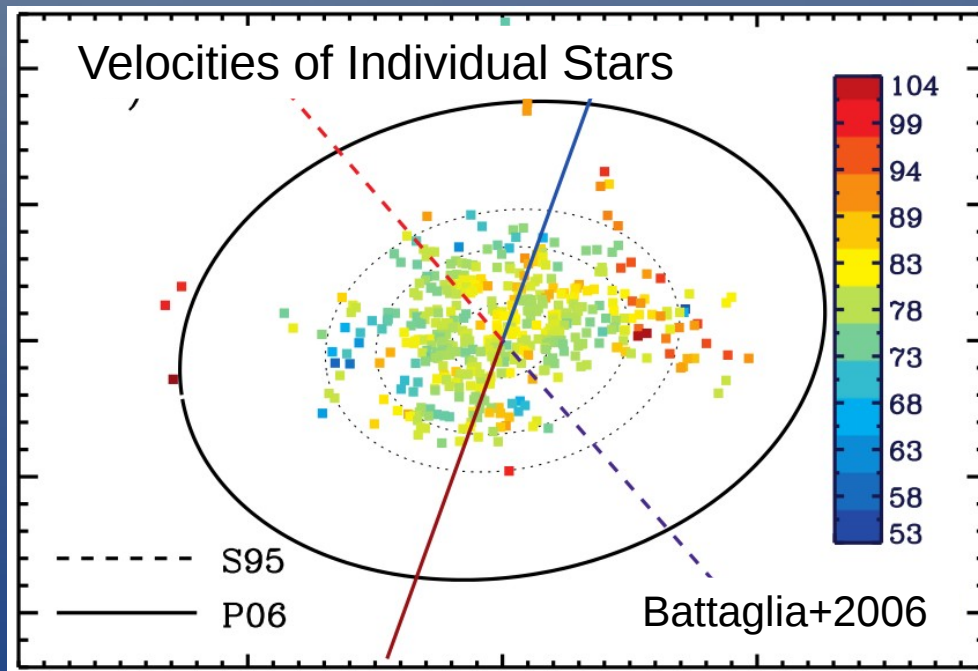
# Stellar kinematics in "classical" dSphs



Walker+2012

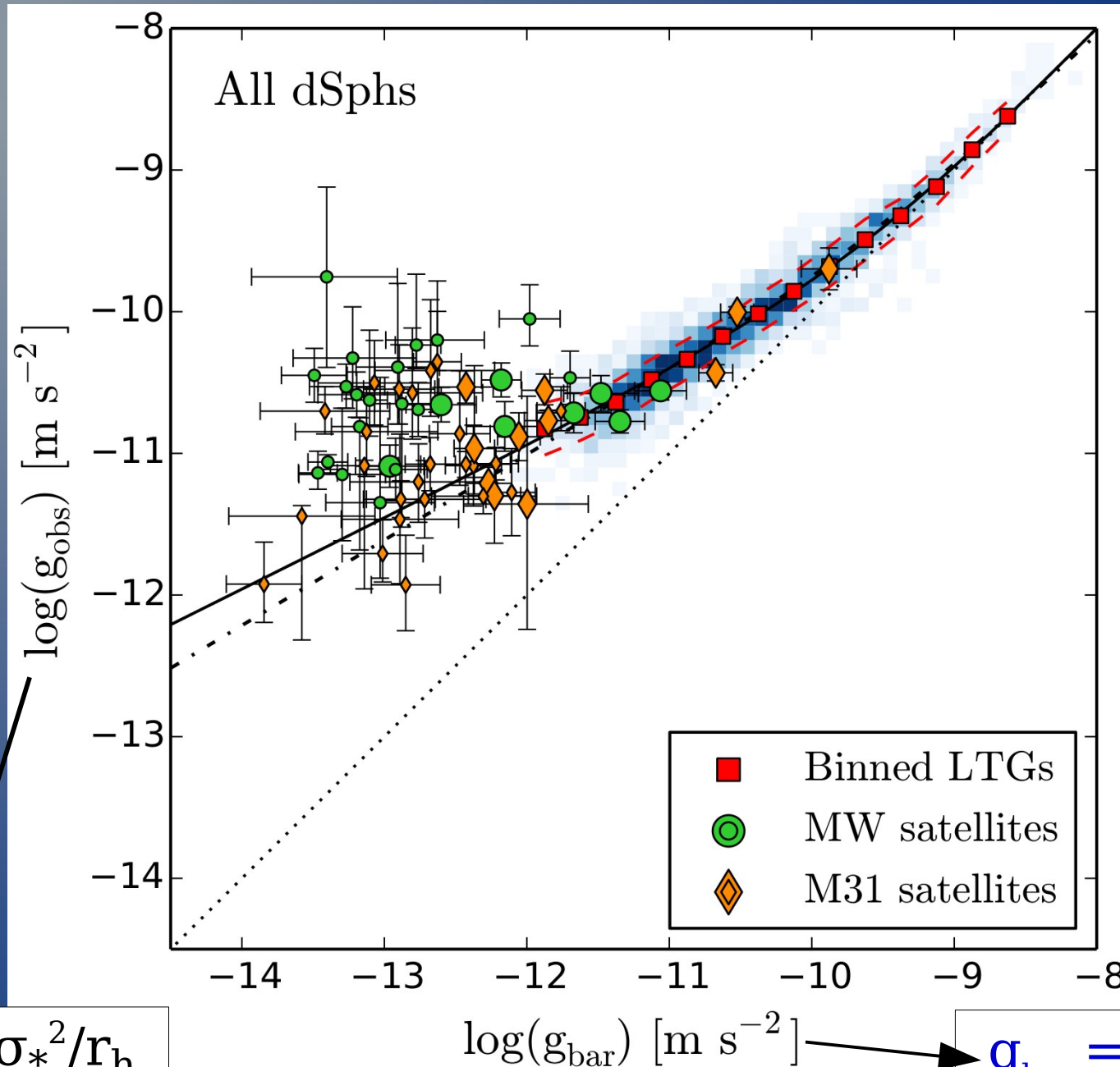


**Mass-Anisotropy Degeneracy:**  
 $M_{\text{tot}}$  can be robustly estimated only  
 at  $r_h = 4/3R_h$  (Walker+2009, Wolf+2010)





# Radial Acceleration Relation for dSphs



**dSphs:**  
1 point per galaxy at the half-light radius  $r_h$ .

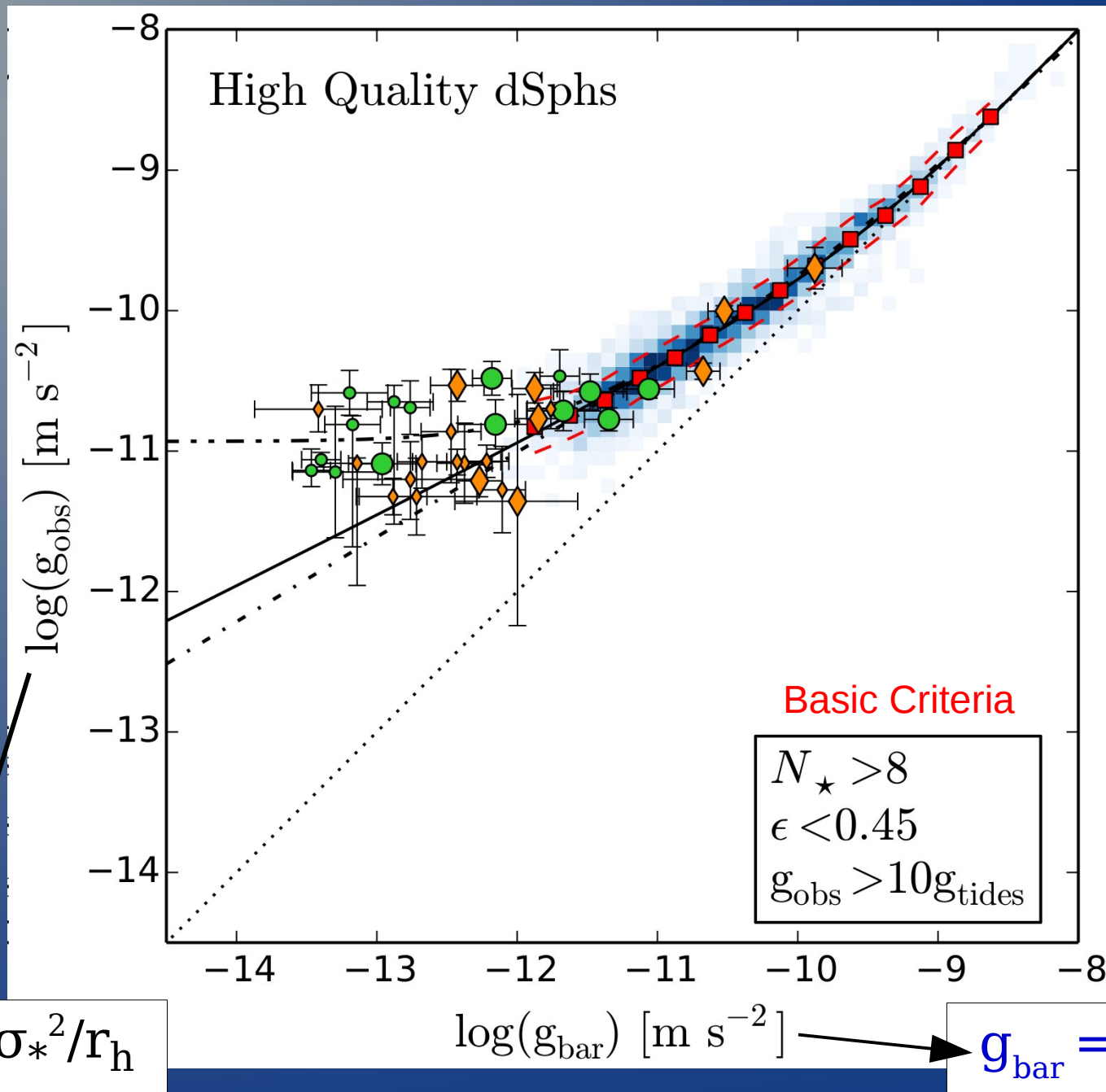
**Large symbols:**  
Classical dSphs

**Small symbols:**  
Ultrafaint dSphs

$$g_{\text{obs}} = 3\sigma_*^2/r_h$$

$$g_{\text{bar}} = GM_{\text{bar}}/r_h^2$$

# Radial Acceleration Relation for dSphs



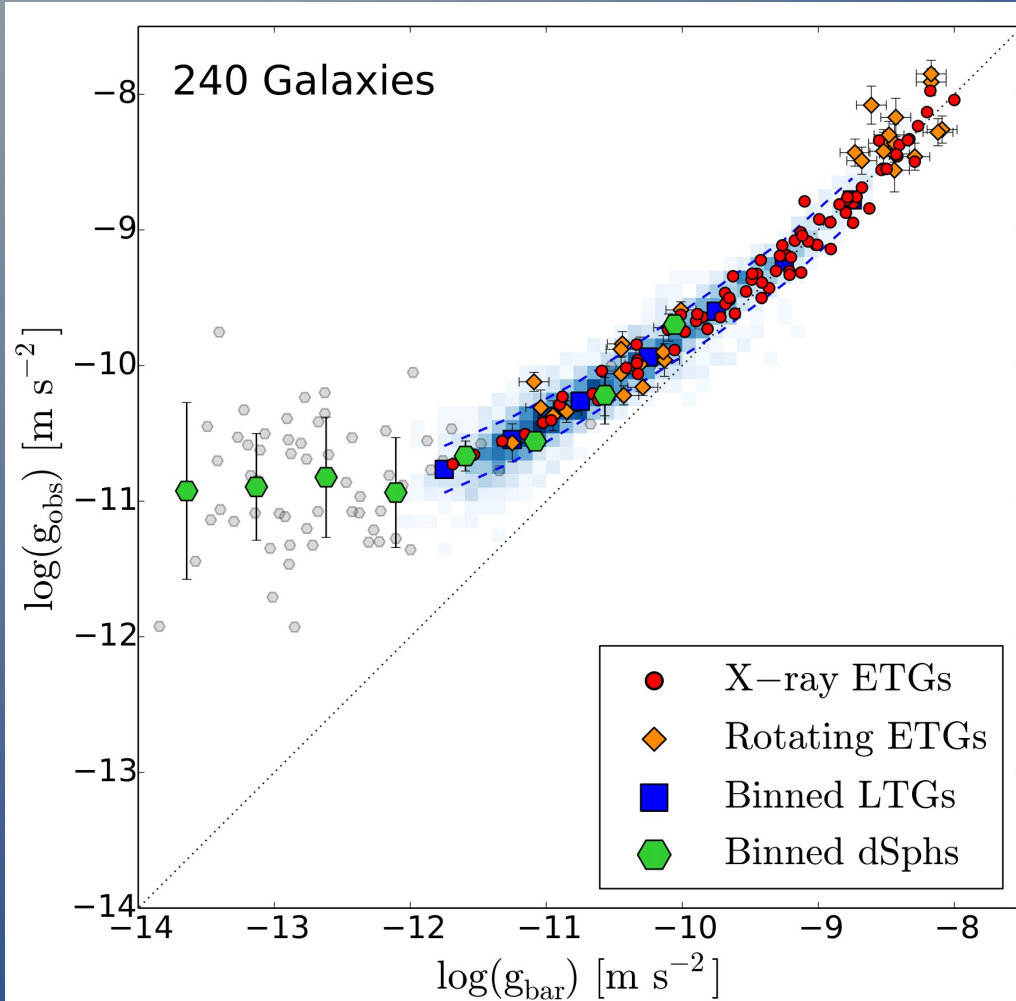
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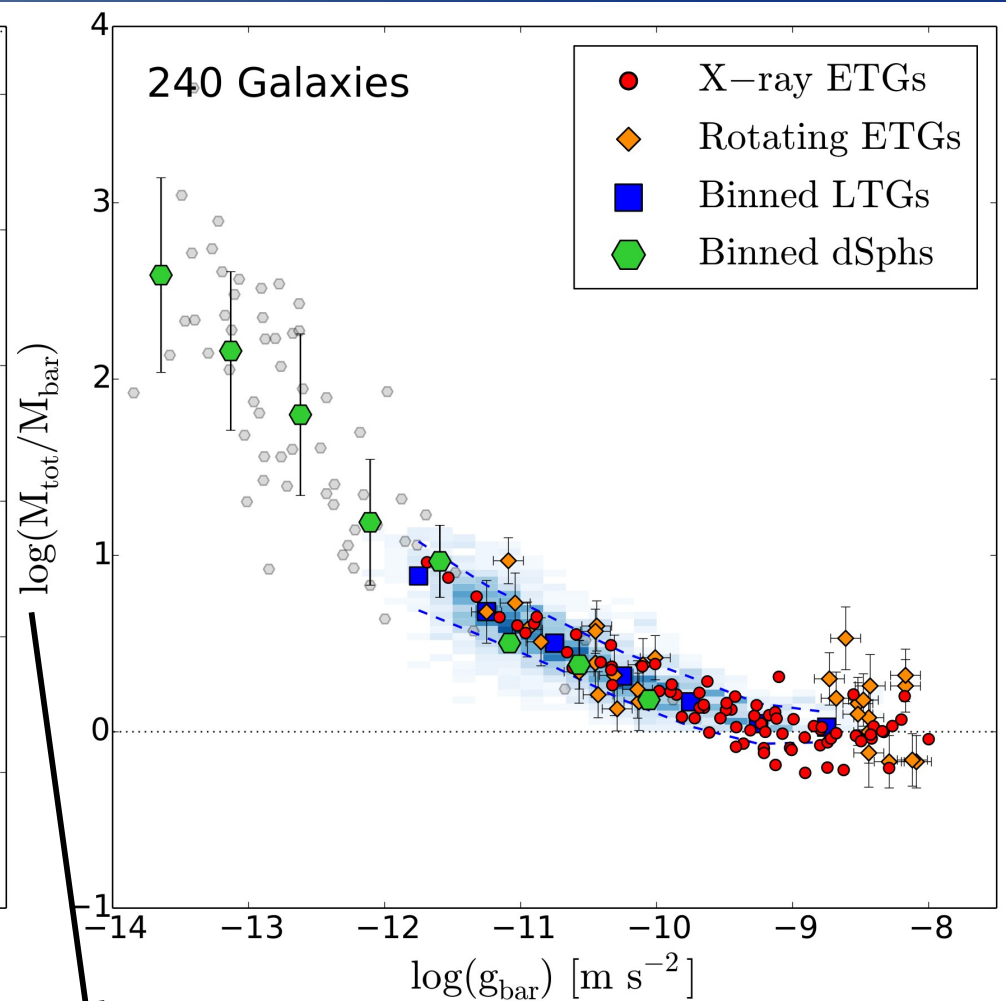
**Small symbols:**  
Ultrafaint dSphs

# A "Kepler" Law for Galaxies?

Radial Acceleration Relation



Mass-Discrepancy Acceleration Relation



Lelli et al. (2016d)

$$M_{\text{tot}}/M_{\text{bar}} = g_{\text{obs}}/g_{\text{bar}}$$

MDAR (Sanders 1990; McGaugh 1999, 2004)

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2. The **intrinsic scatter** around these scaling relations is extremely small (if any).
3. There is an **acceleration scale** of  $\sim 10^{-10} \text{ m s}^{-2}$ .
4. dSphs **may** indicate a flattening at  $\sim 10^{-12} \text{ m s}^{-2}$ .