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"Beta Beams: the physics case "



- Introduction
- General principles of a Beta Beam
- Strategies for a Beta Beam experiment
- Sensitivities
- Future options
- Comparison with other setups.

Parameters of the Standard Model

Symbol	Description	Renormalization scheme (point)	Value	
m _e	Electron mass		511 keV	
m _μ	Muon mass		106 MeV	
m _t	Tauon mass		1.78 GeV	
m _u	Up quark mass	$\mu_{\overline{\text{MS}}} = 2 \text{ GeV}$	1.9 MeV	
m _d	Down quark mass	$\mu_{\overline{\rm MS}} = 2 { m GeV}$	4.4 MeV	
m _s	Strange quark mass	$\mu_{\overline{\rm MS}} = 2 { m GeV}$	87 MeV	
m _c	Charm quark mass	$\mu_{\overline{\text{MS}}} = m_c$	1.32 GeV	
m _b	Bottom quark mass	$\mu_{\overline{\text{MS}}} = m_{b}$	4.24 GeV	
m _t	Top quark mass	On-shell scheme	172.7 GeV	
θ_{12}	CKM 12-mixing angle		13.1°	
θ ₂₃	CKM 23-mixing angle		2.4°	
θ_{13}	CKM 13-mixing angle		0.2°	
δ	CKM CP-violating Phase		0.995	
g_1	U(1) gauge coupling	$\mu_{\overline{\text{MS}}} = m_{Z}$	0.357	
g ₂	SU(2) gauge coupling	$\mu_{\overline{\text{MS}}} = m_Z$	0.652	
g ₃	SU(3) gauge coupling	$\mu_{\overline{\text{MS}}} = m_{Z}$	1.221	
$\theta_{\rm QCD}$	QCD vacuum angle		~0	
μ	Higgs quadratic coupling		Unknown	
λ	Higgs self-coupling strength		Unknown	

Parameters added after neutrino oscillations

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Sub leading $u_{\mu} - u_{e}$ oscillations



$$\begin{split} p(\nu_{\mu} \to \nu_{e}) &= 4c_{13}^{2}s_{13}^{2}s_{23}^{2}\sin^{2}\frac{\Delta m_{13}^{2}L}{4E} \times \left[1 \pm \frac{2a}{\Delta m_{13}^{2}}(1 - 2s_{13}^{2})\right] \qquad \theta_{13} \text{ driv} \\ &+ 8c_{13}^{2}s_{12}s_{13}s_{23}(c_{12}c_{23}\cos\delta - s_{12}s_{13}s_{23})\cos\frac{\Delta m_{23}^{2}L}{4E}\sin\frac{\Delta m_{13}^{2}L}{4E}\sin\frac{\Delta m_{12}^{2}L}{4E} \text{ CPert} \\ &\mp 8c_{13}^{2}c_{12}c_{23}s_{12}s_{13}s_{23}\sin\delta\sin\frac{\Delta m_{23}^{2}L}{4E}\sin\frac{\Delta m_{13}^{2}L}{4E}\sin\frac{\Delta m_{12}^{2}L}{4E} \text{ CPodd} \\ &+ 4s_{12}^{2}c_{13}^{2}\{c_{13}^{2}c_{23}^{2} + s_{12}^{2}s_{23}^{2}s_{13}^{2} - 2c_{12}c_{23}s_{12}s_{23}s_{13}\cos\delta\}\sin\frac{\Delta m_{12}^{2}L}{4E} \text{ solar driven} \\ &\mp 8c_{12}^{2}s_{13}^{2}s_{23}^{2}\cos\frac{\Delta m_{23}^{2}L}{4E}\sin\frac{\Delta m_{13}^{2}L}{4E}(1 - 2s_{13}^{2}) \text{ matter effect (CP odd)} \end{split}$$

 $\begin{array}{ll} \theta_{13} & {\rm discovery} \ {\rm requires} \ {\rm a} \\ {\rm signal} & (\propto & {\rm sin}^2 \, 2\theta_{13} \,) \\ {\rm greater} \ {\rm than} \ {\rm the} \ {\rm solar} \\ {\rm driven} \ {\rm probability} \end{array}$

 $\begin{array}{l} \text{Leptonic CP discovery requires} \\ \textbf{A}_{CP} = \frac{P(\nu_{\mu} \rightarrow \nu_{e}) - P(\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e})}{P(\nu_{\mu} \rightarrow \nu_{e}) + P(\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{e})} \neq 0 \end{array}$



Measuring Leptonic CP violation



LCPV asymmetry at the first oscillation maximum, $\delta = 1$, Error curve: dependence of the statistical+systematic (2%) computed for a beta beam the fixed energy $E_{IV} = 0.4$ GeV, L = 130 km.

Measuring Leptonic CP violation



LCPV asymmetry at the first oscillation maximum, $\delta~=~$ 1, Error

curve: dependence of the statistical+systematic (2%) computed for a

beta beam the fixed energy E_{ν} = 0.4 GeV, L = 130 km.

 The detection of such asymmetry is an evidence of Leptonic CP violation only in absence of competitive processes (i.e. matter effects, see following slides) ⇒ "short" Long Baseline experiments

Measuring Leptonic CP violation



LCPV asymmetry at the first oscillation maximum, $\delta~=~$ 1, Error

curve: dependence of the statistical+systematic (2%) computed for a

beta beam the fixed energy $E_{
u}$ = 0.4 GeV, L = 130 km.

- The detection of such asymmetry is an evidence of Leptonic CP violation only in absence of competitive processes (i.e. matter effects, see following slides) ⇒ "short" Long Baseline experiments
- Statistics and systematics play different roles at different values of $\theta_{13} \Rightarrow$ impossible to optimize the experiment without a prior knowledge of θ_{13}
- Contrary to the common belief, the highest values of θ_{13} are not the easiest condition for LCPV discovery

Measuring mass hierarchy

An internal degree of freedom of neutrino masses is the sign of Δm_{31}^2 : $\mathrm{sign}(\Delta m_{23}^2)$.



This parameter decides how mass eigenstates are coupled to flavor eigenstates with important consequencies to direct neutrino mass and double beta decay experiments.

$$P_{\theta_{13}} = \sin^2(2\theta_{13})\sin\theta_{23}^2\sin^2((\hat{A}-1)\hat{\Delta})/(\hat{A}-1)^2;$$

$$p_{\sin\delta} = \alpha \sin(2\theta_{13})\zeta \sin\delta \sin(L\hat{\Delta})\sin(\hat{A}\hat{\Delta})\sin((1-\hat{A})\hat{\Delta})/((1-\hat{A})\hat{A});$$

$$p_{\cos\delta} = \alpha \sin(2\theta_{13})\zeta \cos\delta \cos\hat{\Delta}\sin(\hat{A}\hat{\Delta})\sin(1-\hat{A}\hat{\Delta})/((1-\hat{A})\hat{A});$$

$$p_{\text{solar}} = \alpha^2\cos\theta_{23}^2\sin^22\theta_{12}\sin^2(\hat{A}\hat{\Delta})/\hat{A}^2;$$

$$\begin{split} \alpha &= \operatorname{Abs}(\Delta m_{21}^2 / \Delta m_{31}^2); \ \hat{\Delta} = \frac{\iota \Delta m_{31}^2}{4E} \zeta = \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \\ \hat{\boldsymbol{A}} &= \pm \boldsymbol{a} / \Delta m_{31}^2; \ \boldsymbol{a} = 7.6 \cdot 10^{-5} \rho \cdot E_{\nu} (\text{GeV}) \quad \rho = \text{matter density } (\text{g cm}^{-3}) \\ \text{The } \hat{\boldsymbol{A}} \text{ term changes sign with } \operatorname{sign}(\Delta m_{23}^2) \end{split}$$

Matter effects require long "long baselines"

$$\begin{aligned} P_{\theta_{13}} &= \sin^2(2\theta_{13})\sin\theta_{23}^2\sin^2((\hat{A}-1)\hat{\Delta})/(\hat{A}-1)^2;\\ p_{\sin\delta} &= \alpha\sin(2\theta_{13})\zeta\sin\delta\sin(L\hat{\Delta})\sin(\hat{A}\hat{\Delta})\sin(((1-\hat{A})\hat{\Delta})/(((1-\hat{A})\hat{A});\\ p_{\cos\delta} &= \alpha\sin(2\theta_{13})\zeta\cos\delta\cos\hat{\Delta}\sin(\hat{A}\hat{\Delta})\sin((1-\hat{A}\hat{\Delta})/(((1-\hat{A})\hat{A});\\ p_{\rm solar} &= \alpha^2\cos\theta_{23}^2\sin^22\theta_{12}\sin^2(\hat{A}\hat{\Delta})/\hat{A}^2; \end{aligned}$$

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Matter effects require long "long baselines" $E_{\nu}=0.35{ m GeV}\,L\simeq130$ km



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$\begin{array}{l} \text{Matter effects require long "long baselines"}\\ E_{\nu}=0.35 \text{GeV} \ \textit{L}\simeq 130 \ \text{km} \quad E_{\nu}=1 \text{GeV} \ \textit{L}\simeq 500 \ \text{km} \end{array}$



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Matter effects require long "long baselines" $E_{\nu} = 0.35 \text{GeV} \ L \simeq 130 \text{ km}$ $E_{\nu} = 1 \text{ GeV} \ L \simeq 500 \text{ km}$ $E_{\nu} = 3 \text{ GeV} \ L \simeq 1500 \text{ km}$ (Probs in Vacuum (Magenta) and Matter (blue) (Probs in Vacuum (Magenta) and Matter (blue) {Probs in Vacuum (Magenta) and Matter (blue) } 0.04 0.025 0.02 0.02 0.015 0.02 0.01 0.01 0.01 0.005 0.005 1000^L 1000 1500 2000 2500 3000 L (km)

At 130 km matter effects are negligible. $\tilde{\epsilon}^2$ Inverse hierarchy solutions are very similar to direct hierarchy (changing sign of $\delta_{\rm CP}$ is equivalent of change of ${\rm sign}(\Delta m_{23}^2){\rm sign}) \Rightarrow$ No degeneracies for CP searches but no sensitivity on mass hierarchy.



At 130 km matter effects are negligible. $\overleftarrow{\epsilon}$ Inverse hierarchy solutions are very similar to direct hierarchy (changing sign of $\delta_{\rm CP}$ is equivalent of change of $\operatorname{sign}(\Delta m_{23}^2)$ sign) \Rightarrow No degeneracies for CP searches but no sensitivity on mass hierarchy.



Note however as the normal hierarchy $\delta_{\rm CP} = 0$ probability is very similar to inverse hierarchy $\delta_{\rm CP} = \pi/2$, \Rightarrow very difficult to experimentally disentangle the two.







The synergy with atmospheric neutrinos

P. Huber et al., Phys. Rev. D 71, 053006 (2005): Combining Long Baseline data with atmospheric neutrinos (that come for free in the megaton detector):

- $\bullet\,$ Degeneracies can be canceled, allowing for better performances in $\theta_{13}\, {\rm and}\, {\rm LCPV}\,$ searches
- The neutrino mass hierarchy can be measured
- The θ_{23} octant can be determined.

The main reasons are:

- Octant e-like events in the Sub-GeV data is $\propto \cos^2 \theta_{23}$
- **Sign** e-like events in the Multi-GeV data, thanks to matter effects, especially for zenith angles corresponding to neutrino trajectories crossing the mantle and core where a resonantly enhancement occurs.

NOTE: LBL and atmospherics are a true synergy. They add to each other much more that a simple gain in statistics. Atmospherics alone could not measure the hierarchy, the octant, θ_{13} and LCPV. While the Beta Beam at short baselines could not measure the hierarchy as well as the octant.



Mauro Mezzetto (INFN Padova)

Status after this generation of LBL experiments: θ_{13}



Status after this generation of LBL experiments: CPV



Status after this generation of LBL experiments: CPV



Status after this generation of LBL experiments: CPV



Status after accelerator upgrades

From P. Huber et al., JHEP 0911:044,2009.

Prediction of sensitivity including a **fully optimized global run** (antineutrinos in T2K and NO ν A) and **full upgrade of the accelerators**: 1.6 MW at J-PARC and 2.4 MW at FNAL (Project-X)



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Systematic errors

They could completely destroy leptonic CP violation sensitivity.

Default value are often 5% for SuperBeams, 2% for Neutrino Factory and 2-5% for Beta Beams.

Are

them realistic goals? Are close detectors powerful enough?



The general problem of close detectors in a SB experiment

SuperBeams

$$\begin{split} \mathbf{N}_{\mathrm{events}}^{\mathrm{far}} &= \left(\sigma_{\nu_{\mathrm{e}}} \epsilon_{\nu_{\mathrm{e}}} \mathbf{P}_{\nu_{\mu}\nu_{\mathrm{e}}} + \sigma_{\nu_{\mu}}^{\mathrm{NC}} \epsilon_{\mathrm{NC}} + \sigma_{\nu_{\mu}}^{\mathrm{CC}} \epsilon_{\mathrm{CC}} \mathbf{P}_{\nu_{\mu}\nu_{\mu}}\right) \phi_{\nu_{\mu}} + \sigma_{\nu_{\mathrm{e}}}^{\mathrm{CC}} \epsilon_{\nu_{\mathrm{e}}} \phi_{\nu_{\mathrm{e}}} \\ \mathbf{N}_{\mathrm{events}}^{\mathrm{close}} &= \left(\sigma_{\nu_{\mu}}^{\mathrm{NC}} \epsilon_{\mathrm{NC}}' + \sigma_{\nu_{\mu}}^{\mathrm{CC}} \epsilon_{\mathrm{CC}}'\right) \phi_{\nu_{\mu}}' + \sigma_{\nu_{\mathrm{e}}}^{\mathrm{CC}} \epsilon_{\nu_{\mathrm{e}}} \phi_{\nu_{\mathrm{e}}}' \end{split}$$

- $\bullet\,$ The close detector measures the product of fluxes $\times\,$ cross section $\times\,$ efficiency
- Reduced ν_e flux: small statistics to determine the cross section
- NC backgrounds must be separated from beam ν_e.

Beta Beams

$$\begin{split} \mathbf{N}_{\mathrm{events}}^{\mathrm{far}} &= \left(\sigma_{\nu_{\mu}} \epsilon_{\nu_{\mu}} \mathbf{P}_{\nu_{e}\nu_{\mu}} + \sigma_{\nu_{e}}^{\mathrm{NC}} \epsilon_{\mathrm{NC}} + \sigma_{\nu_{e}}^{\mathrm{CC}} \epsilon_{\mathrm{CC}} \mathbf{P}_{\nu_{e}\nu_{e}}\right) \phi_{\nu_{e}} \\ \mathbf{N}_{\mathrm{events}}^{\mathrm{close}} &= \left(\sigma_{\nu_{e}}^{\mathrm{NC}} \epsilon_{\mathrm{NC}}' + \sigma_{\nu_{e}}^{\mathrm{CC}} \epsilon_{\mathrm{CC}}'\right) \phi_{\nu_{e}} \end{split}$$

Flux known at priori, no intrinsic contamination (direct measure of NC backgrounds), no problems with the close-far extrapolation BUT no events to measure signal (ν_{μ}) cross sections.

Systematic errors and their pulls



Conventional neutrino beams are going to hit their ultimate limitations.



In a **conventional neutrino beam**, neutrinos are produced SECONDARY particle decays (mostly pions and kaons).

Given the short life time of the pions $(2.6 \cdot 10^{-8}s)$, they can only be focused (and charge selected) by means of magnetic horns. Then they are let to decay in a decay tunnel, short enough to prevent most of the muon decays.

- Besides the main component (ν_μ) at least 3 other neutrino flavors are present (ν
 _μ, ν_e, ν
 _e), generated by wrong sign pions, kaons and muon decays. ν_econtamination is a background for θ₁₃ and δ, ν
 _μcontamination dilutes any CP asymmetry.
- Hard to predict the details of the neutrino beam starting from the primary proton beam, the problems being on the secondary particle production side.

Collect, focus and accelerate the neutrino parents at a given energy. This is impossible within the pion lifetime, but can be tempted within the muon lifetime (Neutrino Factories) or within some radioactive ion lifetime (Beta Beams):

- Just one flavor in the beam
- Energy shape defined by just two parameters: the endpoint energy of the beta decay and the γ of the parent ion.
- Flux normalization given by the number of ions circulating in the decay ring.
- Beam divergence given by γ .

Distinctive features of Beta Beams

 \ldots for the limitations see tiny notes in the next slides \ldots

- Don't need a magnetized detector ⇒ make use of next generation megaton water Cerenkov detectors or 100 kton liquid argons.
- Can re-use part of the CERN accelerator complex (this can be seen as a limitation)
- Synergies with Nuclear Physics (share an intense radioactive ion source), SPL Super Beam (two neutrino beams in the same detector), atmospheric neutrinos (physics case of both beams greatly enhanced by this synergy).
- An evolving concept with several interesting possible upgrades.












Possible β^{-} emitters ($\bar{\nu}_{e}$)

lsotope	Ζ	Α	A/Z	T _{1/2}	Q _{β (gs>gs)}	$Q_{\beta \text{ eff.}}$	$E_{\beta av.}$	E _{v av.}	<e_lab>(MeV)</e_lab>
				S	MeV	MeV	MeV	MeV	(@ 450 GeV/p)
6He	2	6	3.0	0.807	3.5	3.5	1.57	1.94	582
8He	2	8	4.0	0.119	10.7	9.1	4.35	4.80	1079
8Li	3	8	2.7	0.838	16.0	13.0	6.24	6.72	2268
9Li	3	9	3.0	0.178	13.6	11.9	5.73	6.20	1860
11Be	4	11	2.8	13.81	11.5	9.8	4.65	5.11	1671
15C	6	15	2.5	2.449	9.8	6.4	2.87	3.55	1279
16C	6	16	2.7	0.747	8.0	4.5	2.05	2.46	830
16N	7	16	2.3	7.13	10.4	5.9	4.59	1.33	525
17N	7	17	2.4	4.173	8.7	3.8	1.71	2.10	779
18N	7	18	2.6	0.624	13.9	8.0	5.33	2.67	933
23Ne	10	23	2.3	37.24	4.4	4.2	1.90	2.31	904
25Ne	10	25	2.5	0.602	7.3	6.9	3.18	3.73	1344
25Na	11	25	2.3	59.1	3.8	3.4	1.51	1.90	750
26Na	11	26	2.4	1.072	9.3	7.2	3.34	3.81	1450

From P..Zucchelli talk at Nufact 03. Table compiled by U. Koster

Possible β^+ emitters (ν_e)

lsotope	Ζ	Α	A/Z	T _{1/2}	Q _{β (gs>gs)}	$Q_{\beta \text{ eff.}}$	$E_{\beta av.}$	E _{v av.}	<e_lab>(MeV)</e_lab>
				S	MeV	MeV	MeV	MeV	(@450 GeV/p)
8B	5	8	1.6	0.77	17.0	13.9	6.55	7.37	4145
10C	6	10	1.7	19.3	2.6	1.9	0.81	1.08	585
140	8	14	1.8	70.6	4.1	1.8	0.78	1.05	538
15O	8	15	1.9	122.2	1.7	1.7	0.74	1.00	479
18Ne	10	18	1.8	1.67	3.4	3.4	1.50	1.86	930
19Ne	10	19	1.9	17.34	2.2	2.2	0.96	1.25	594
21Na	11	21	1.9	22.49	2.5	2.5	1.10	1.41	662
33Ar	18	33	1.8	0.173	10.6	8.2	3.97	4.19	2058
34Ar	18	34	1.9	0.845	5.0	5.0	2.29	2.67	1270
35Ar	18	35	1.9	1.775	4.9	4.9	2.27	2.65	1227
37K	19	37	1.9	1.226	5.1	5.1	2.35	2.72	1259
80Rb	37	80	2.2	34	4.7	4.5	2.04	2.48	1031

From P..Zucchelli talk at Nufact 03. Table compiled by U. Koster

Some scaling laws in Beta Beams

	β^+ emitters		β^- emitters			
lon	Q_{eff} (MeV)	Z/A	lon	Q_{eff} (MeV)	Z/A	
¹⁸ Ne	3.30	5/9	⁶ He	3.508	1/3	
⁸ B	13.92	5/8	⁸ Li	12.96	3/8	

- Proton accelerators can accelerate ions up to $Z/A \times$ the proton energy.
- Lorentz boost: end point of neutrino energy $\Rightarrow 2\gamma Q$
- In the CM neutrinos are emitted isotropically \Rightarrow neutrino beam from accelerated ions gets more collimated $\propto \gamma^2$
- Merit factor for an experiment at the atmospheric oscillation maximum: $\mathcal{M} = \frac{\gamma}{0}$

- Ion lifetime must be:
 - As long as possible: to avoid ion decays during acceleration
 - As short as possible: to avoid to accumulate too many ions in the decay ring
 - \Rightarrow optimal window: lifetimes around 1 s.
- Decay ring length scales $\propto \gamma$, following the magnetic rigidity of the ions.
- Two body decay kinematics : going off-axis the neutrino energy changes (feature used in some ECB setup and in the low energy setup)

Production of 6He ions for beta beams





10¹⁴ ⁶He/s 200 kW, 2 GeV proton beam in-target production. 50 – 90% extraction efficiency from realistic big targets (reduced scale experiment doe at CERN-ISOLDE to confirm these numbers; Weizmann, GANIL and CERN collaboration).

M. Hass et al

Numbers have now been carefully checked. 1 kW of 1-2 GeV protons produces more ⁶He than 1 kW of 40 MeV deuterons.



Production of ¹⁸Ne ions for beta beams

The beam current and power for a constant yield 10¹³ ¹⁸Ne/s



NEU2012

Where do we stand for BaseLine ion production for beta beams

◆ ⁶He

Can be produced with *(a variant of)* SPL 200kW, 2 GeV Linac : synergies with a future Radioactive Ion Beam facility at CERN (light EURISOL or super-ISOLDE).

◆ ¹⁸Ne

Could be produced with upgraded Linac4. This project is stopped at present.

T. Stora – EN-STI (TISD-ISOLDE)

28/09/2010

Boundary conditions:

- CERN SPS can accelerate ${}^{6}\text{He} \text{ up to } \gamma = 150 \Rightarrow E_{\nu} \simeq 0.5 \text{GeV}$ \Rightarrow baselines within 300 km.
- The only viable candidate to host a megaton detector is Frejus lab, 130 km away from CERN

Optimal γ : $\gamma = 100$.

This is the option studied by the Eurisol design study and now by the EuroNu design study



Experimental strategy

Beta Beam signal is ν_{μ} appearance.

To profit of the no-background beam, detector backgrounds should be taken at minimum:

- ν_e events mis-identified as ν_μ events
- Charged pions from NC and NC-like ν_e interactions mis-identified as muons.
- Atmospheric neutrinos

As described in the following, background reduction will not rely on kinematical cuts.

Particle identification and signal efficiency

Electron/muon misidentification must be suppressed much more than in standard SK analysis to guarantee a negligible background level.

Pid in SK is performed through a Likelihood, the Pid > 0 identifies muons. Use Pid > 1



 $\begin{array}{ccccc} To & further & suppress & ^2 \\ electron background ask for the signal & ^{175} \\ of the Michel electron from <math display="inline">\mu$ decay. & ^{15} \\ Final efficiency for positive muons. & ^{125} \\ Negative muons have an efficiency & ^{128} \\ smaller by \sim 22\% \ because they can be & ^{075} \\ absorbed before decaying. & & \\ \hline Electron & mis-identification & \\ suppressed to \sim 10^{-5}. & & \\ \end{array}



Energy reconstruction for beam neutrinos





Single ring non Quasi Elastic are badly measured



bkg. for E, measurement

High energy part

bkg.for e-appearance

Goodness of energy reconstruction



Migration Matrixes

A gaussian assumption for energy resolution is a too crude approximation





The pion background



The pions generated in NC events can fake the muon signal.

They are the main concern at high gammas.

To estimate these backgrounds

- Generate CC and NC events with Nuance
- Count events with a pion and no other track above the Čerenkov threshold (single ring events)
- Apply the tight pid cuts of SuperKamiokande
- Follow pions in water (Geant 3.21) to compute the probability for $\pi \rightarrow \mu \rightarrow e$.
- Reconstruct the neutrino energy from the survived pions treating them as the signal muons

The pion background (cont.)



A very important cross check

Chizuelshihara, arXiv:0912.1002v2

Beta Beam signals and backgrounds recalculated with theSuperKamiokande analysis tools: full simulation and full reconstruction.



Figure 3: The final sample neutrino true energy distributions for each beam type, in case of $\sin^2 2\theta_{13} = 0.15$. The different event types are shown in different colors as shown right side.



Figure 4: (1) are the reconstructed energy distributions in case of $\sin^2 2\theta_{13} = 0.15$. (2) are in case of $\sin^2 2\theta_{13} = 0.01$.

Atmospheric neutrino background



The only viable tool to keep them at a negligible rate is to keep very short the live time of the neutrino beam. This is a tight requirement for the Beta Beam accelerator complex.

Question: why atmospherics are not a great concern at T2K phase 1, that has much smaller signal neutrino fluxes?



Atmospheric neutrino background

Sub-GeV $\mu\text{-like}$ events in SK integrated over the solid angle. 45.3 kton year exposure

Sub-GeV μ -like events zenithal distribution







True-Reconstructed v direction

Kamioka to Frejus flux correction: + 20%

Signal efficiency with respect to standard SK algorithms: 54% (flat in energy)

A duty cycle of 1% would keep the atmospheric background rate below the pion bkg rate (Eurisol DS duty cycle: 0.45%).

The cross sections problem



Neutrino cross-sections are poorly measured around 300 MeV.

Nuclear effects are very important at these energies. No surprise that different MonteCarlo codes predict rates with a 50% spread.

On the other hand: Beta Beam is the ideal place where to measure neutrino cross sections

- Neutrino flux and spectrum are completely defined by the parent ion characteristics and by the Lorentz boost γ.
- Just one neutrino flavour in the beam.
- You can scan different γ values starting from below the Δ production threshold.
- A close detector can then measure neutrino cross sections with unprecedent precision.

A systematic error ranging from 2% to 5% both in signal and backgrounds is used in the following

Neutrino Cross Sections

From: NOMAD Collaboration, Eur. Phys. J. C 63 (2009) 355 [arXiv:0812.4543 [hep-ex]].



Oscillation signals

1.0				,		
	β	В	S	PL	T2HK	
	$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = 0$	$\delta_{\rm CP}=\pi/2$	$\delta_{CP} = 0$	$\delta_{\rm CP}=\pi/2$
appearance v background $sin^2 2\theta_{13} = 0$ $sin^2 2\theta_{13} = 10^{-3}$ $sin^2 2\theta_{-3} = 10^{-2}$	11 2 66 285	13 4 76 214	6 4 93 287	00 11 10	1 181 754	1017 84 18 240
$\frac{\sin^2 2\theta_{13} - 10^2}{\sin^2 2\theta_{13} - 0}$ $\frac{\sin^2 2\theta_{13} - 0}{\sin^2 2\theta_{13} - 10^{-3}}$ $\frac{\sin^2 2\theta_{13} - 10^{-2}}{\sin^2 2\theta_{13} - 10^{-2}}$	285 12 2 64 271	27 3 10 100	5 3 74 297	00 36 104 390	188 746	240 1428 90 261 977

From J.E.Campagne, M. Maltoni, M.M., T.Schwetz, hep-ph/0603172, revised

How to extract $heta_{13}$ and δ_{CP}

The problem is not that simple

- The 3 ν oscillation formula contains all the mixing matrix parameters and Δm^2 . The parameters already measured do have errors that will influence the extraction of the unknown parameters.
- Several parameters still unknown: θ_{13} , δ_{CP} , sign(Δm^2) (hierarchy), the octant of θ_{23} . Different combinations of the above unknowns can fit the same data: \Rightarrow The eightfold degeneracy



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Degeneracies (cont.)

To solve degeneracies:

- A single experiment, single channel, can't get rid of degeneracies.
- The combination of different channels in the same detector can solve degeneracies, i.e. first a second oscillation maximum measurement in LBNE or at Okinoshima.
- Different signals in the same detector can also do the job, i.e. beta beams and atmospheric neutrinos.
- A third possibility is to combine the information of different detectors along the same neutrino beam, as exploited by several proposed neutrino factory configurations.
- Of course the combination of the above combinations can also measure all the unknown parameters: can we define an optimal strategy?



Line width: 2% and 5% systematic errors.



Can the θ_{13} and LCPV searches be improved?

Two pathways explored so far. In order of comparison:

- Fire a conventional neutrino beam (the SPL-SuperBeam) to the same detector.
- Combine BB information with the atmospheric neutrinos that the megaton detector will record for free

P.S. Also ν_e disappearance could help in determining θ_{13} and in removing degeneracies (it's the same channel of reactor experiments). However it would help if systematic errors could be pushed below 0.5%. At present 2% seems to be the ultimate level of systematics for a Beta Beam. You should consider that is very unpractical to build a close detector IDENTICAL to the far detector.

The Beta Beam - SPL Super Beam synergy

MM, Nucl. Phys. Proc. Suppl. 149 (2005) 179.

Yearly Fluxes

A Beta Beam has the same energy spectrum than the SPL SuperBeams and consumes 5% of the SPL protons. The two beams could be fired to the same detector \Rightarrow LCPV searches through CP and T channels (with the possibility of using just neutrinos).

Access to CPTV direct searches.

Cross measurement of signal cross section in the close detectors



The synergy with atmospheric neutrinos

P. Huber et al., Phys. Rev. D 71, 053006 (2005): Combining Long Baseline data with atmospheric neutrinos (that come for free in the megaton detector):

- \bullet Degeneracies can be canceled, allowing for better performances in $\theta_{13} \, {\rm and} \, {\rm LCPV}$ searches
- The neutrino mass hierarchy can be measured
- The θ_{23} octant can be determined.

The main reasons are:

- Octant e-like events in the Sub-GeV data is $\propto \cos^2 \theta_{23}$
- **Sign** e-like events in the Multi-GeV data, thanks to matter effects, especially for zenith angles corresponding to neutrino trajectories crossing the mantle and core where a resonantly enhancement occurs.

NOTE: LBL and atmospherics are a true synergy. They add to each other much more that a simple gain in statistics. Atmospherics alone could not measure the hierarchy, the octant, θ_{13} and LCPV. While the Beta Beam at short baselines could not measure the hierarchy as well as the octant.

Synergy with atm. neutrinos: degeneracy removal

J.E.Campagne, M.Maltoni, M.M., T.Schwetz, JHEP 0704 (2007) 003





Updated sensitivities of SPL, BB and SPL+BB



Ways to improve beta-beam performances

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- Electron capture Beta Beams: monochromatic neutrino beams, a very attractive option
 - They require long lived, high-A, far from the stability valley ions, r \Rightarrow challenging R&D to match the needed fluxes.



- Only longitudinal component recovered in RF cavities
 → Transverse emittance shrinks
- Cooling in 6D
 - (dE/ds) ~ $β^{-2}$ smaller at higher energies → cooling not effective in longitudinal
 - need coupling between transverse and longitudinal:
 - \rightarrow Dispersion & wedge-shaped target

Faster ions will travel on an outer orbit and see a larger target thickness \rightarrow they will get more (dE/ds)

Target: width @ closed orbit = 5 cm $t = 0.289 \text{ mg/cm}^2$ If angle = 20° \rightarrow D_x> 24 cm

E. Benedetto, WP4 meeting, INFN Legnaro, 9/11/10

Preliminary lattice



M. Schaumann, CERN-THESIS-2009-128

Particle		⁷ Li
Energy	E_c	25 MeV
Relativistic gamma	γ_r	1.00383
Beam rigidity	B ho	0.636 T m
Transition γ	γ_t	3.58
Tune	$Q_{x,y}$	2.58, 1.63
Natural chromaticity	$Q'_{x,y}$	-3.67, -3.58
β @ target	$\beta_{x,y}^*$	2.62 m, 0.35 m
Dispersion @ target	$D_{x,y}^*$	0.523 m, 0 m
Target thickness	t_0	0.27 mg/cm^2
	n_t	$10^{19} \text{ atoms/cm}^2$
Energy losses @ target	E_{BB}	$\sim 0.30~{ m MeV}$



- C=12m
- normal-conducting magnets
- Capacitive loaded RF cavity
- Charge-exchange injection Li⁺¹

E. Benedetto, WP4 meeting, INFN Legnaro, 9/11/10

FFAG-ERIT @ KURRI (Osaka)

FFAG and Ionization Cooling: Y.Mori, NIM A 562 (2006) 591



E. Benedetto, WP4 meeting, INFN Legnaro, 9/11/10

Sensitivity Comparison

Based to arXiv:1005.3146, the EuroNu midterm physics report **WBB**: Fermilab to Dusel, 1 MW for ν running, proton energy: 120 GeV, 2 MW for $\overline{\nu}$ running (5+5 yr), 100 kton liquid argon detector, according to Barger et al, Phys. Rev. D76:053005, 2007 (hep-ph/0703029). This setup is different from the proposed LBNE experiment. **T2KK**: J-Parc ν beam running at 4 MW. 270 kton WC detector at Kamioka (295 km) and 270 ktor MC and the proposed LBNE experiment.

kton WC detector in Korea (1050 km), Barger et al, Phys. Rev. D76:053005, 2007 (hep-ph/0703029).

PS2-Slanic CERN-PS2 SuperBeam fired to 100 kton LAr detector at Slanic, as computed by A. Rubbia, arXiv:1003.1921.

SPL: Neutrino beam from CERN-SPL running at 3.5 GeV, 4 MW. 440 kton WC detector at Frejus (130 km). Campagne et al. JHEP **0704** (2007) 003 (hep-ph/0603172).

Beta Beam $\gamma = 100$ Eurisol Beta Beam to Frejus (440 kton WC detector). Campagne et al. JHEP 0704 (2007) 003 (hep-ph/0603172).

Beta Beam + SPL The combination of the above two.

Beta Beam $\gamma = 350$ Beta Beam at $\gamma = 350$, running ⁶He and ¹⁸Ne at the same decay rates as the Eurosol Beta Beam. WC detector of 500 kton at Canfranc (650 km). S. Choubey et al., JHEP 0912:020,2009 (arXiv:0907.2379)

Low Energy Neutrino Factory (LENF) Neutrino Factory running at 4.12 GeV delivering 10^{21} muon decays/year for each sign, 30 kton No ν a like detector, fully magnetized (!) at 1480 km (Fermilab-Henderson mine). A. Bross et al, Phys.Rev.D77:093012,2008. (arXiv:0709.3889)

IDS 1.0 Neutrino Factory 25 GeV neutrino factory delivering $0.5\cdot10^{21}$ muon decays/year for each sign, a 50 kton iron magnetized detector and a 10 kton Emulsion Cloud Chamber, at 4000 km and

a 50 kton iron magnetized detector at 7500 km.

Sensitivity Comparison: θ_{13}



Mauro Mezzetto (INFN Padova)

Sensitivity Comparison: $sign(\Delta m_{23}^2)$



Mauro Mezzetto (INFN Padova)

Sensitivity Comparison: LCPV



Mauro Mezzetto (INFN Padova)

Sensitivity Comparison: LCPV

Additional Slides

Conclusions

- Neutrino oscillations have many foundamental results to offer, and maybe unexpected surprises. Certainly not for free.
- Future experiments will probably require innovative instruments rather than brute force.
- Beta Beams are a realistic possibility solving most of the bottlenecks of conventional neutrino beams.
- They require anyway R&D and manpower, so far they are funded only by EU funds.
- There are several very interesting develoments of the Beta Beams concept that can allow interesting future upgrades.