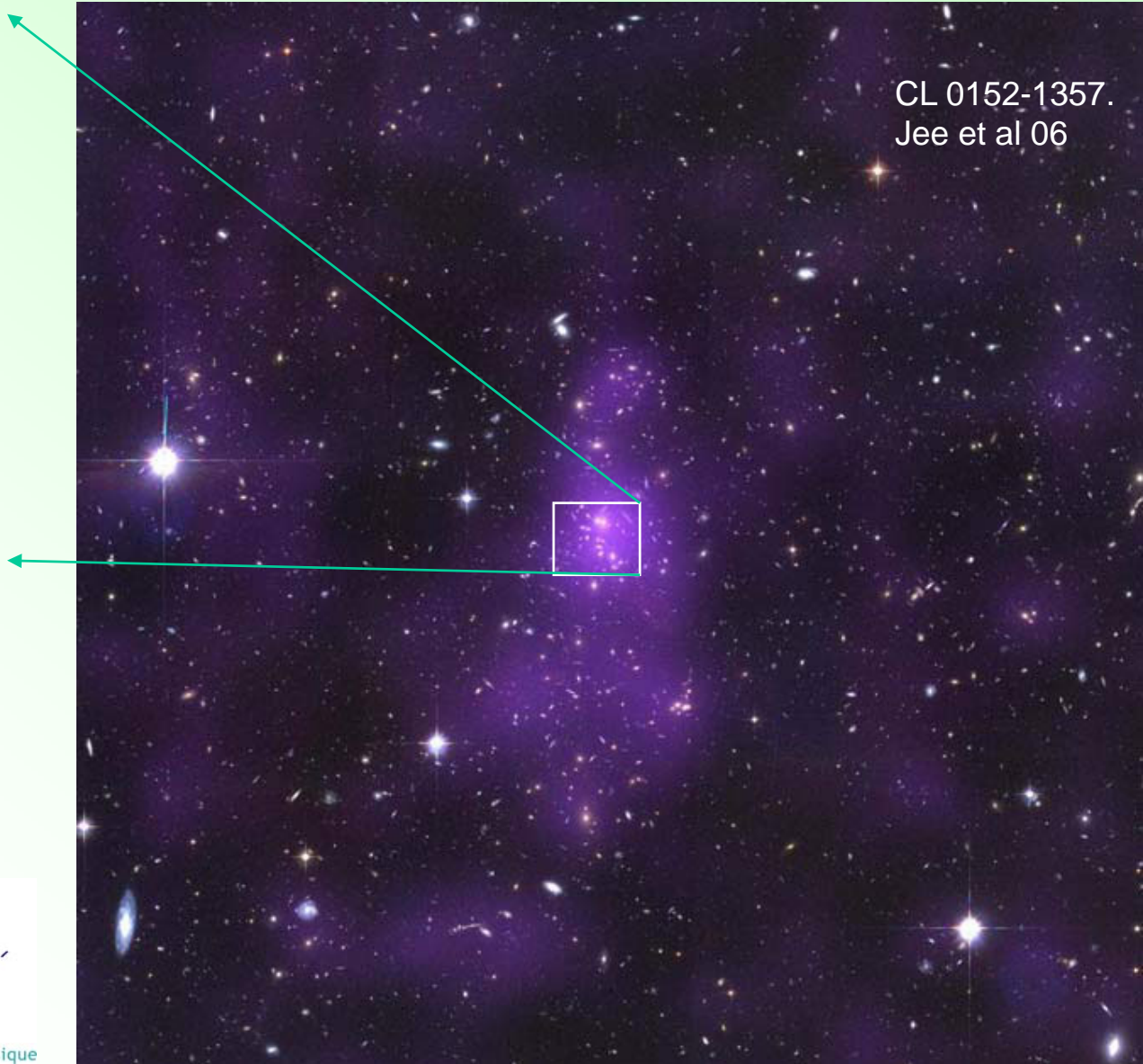


Galaxy Dynamics with MOND

CL 0152-1357.
Jee et al 06



Françoise Combes
Observatoire de Paris

Friday 26 March 2010



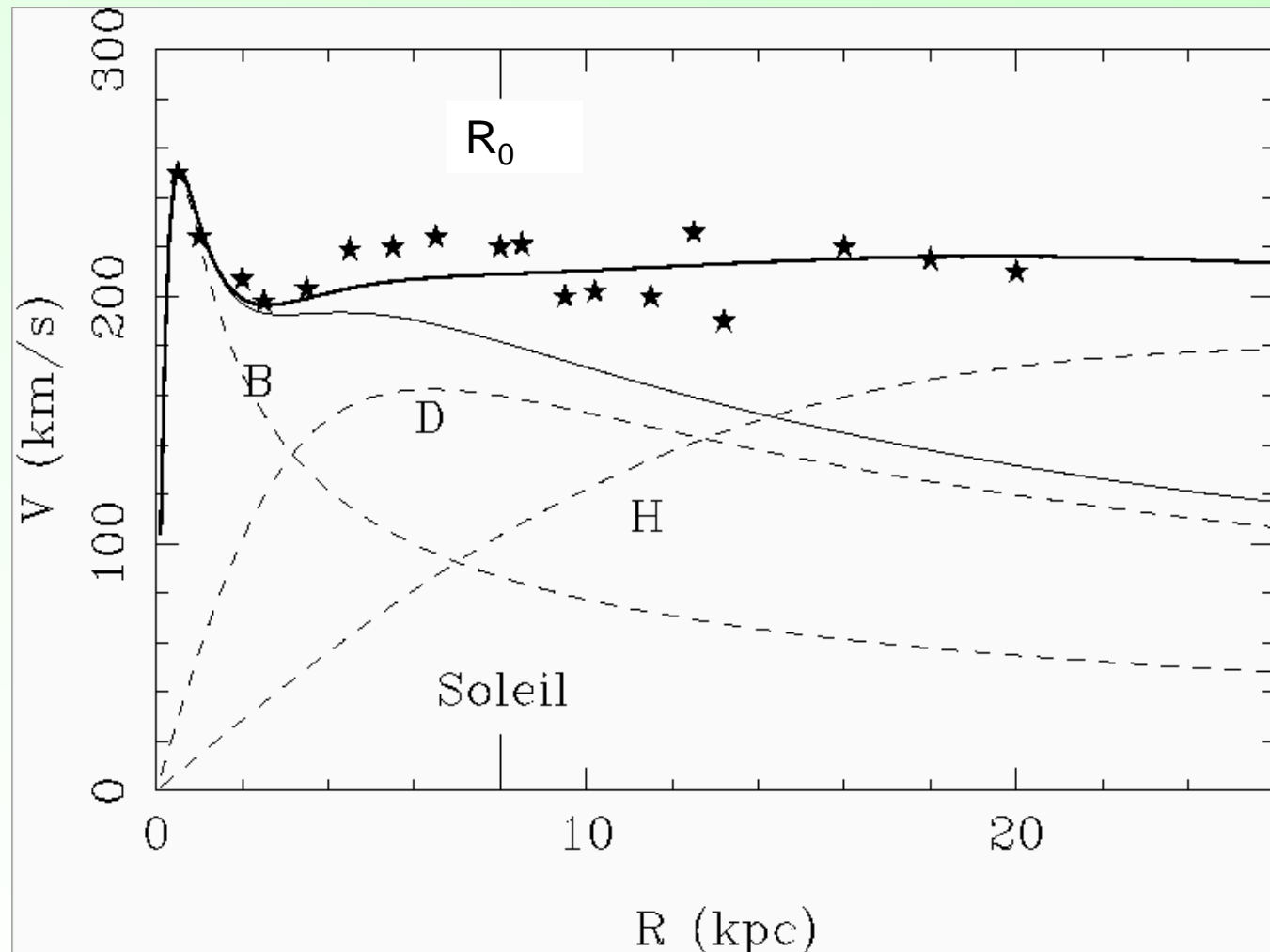
Evidences of dark matter

→ **Galaxy clusters**, Virial /visible mass ~ 100 (Zwicky 1937)

Coma cluster: galaxy velocity dispersion

→ **Rotation curves**
for instance
our Galaxy,
The Milky Way

Well beyond the
visible mass,
The velocity remains
high, instead of
 $V^2 \sim GM/r$
(Kepler)

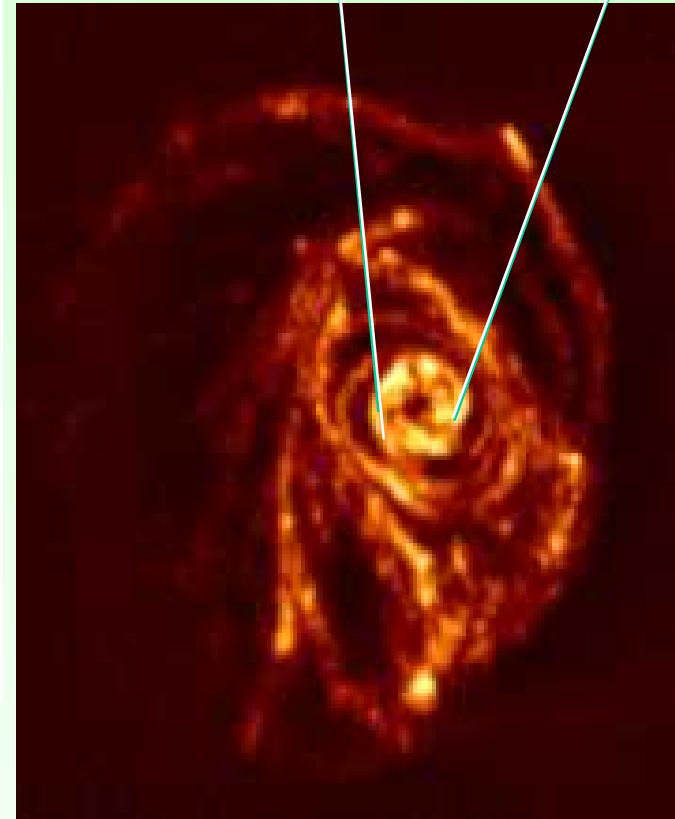
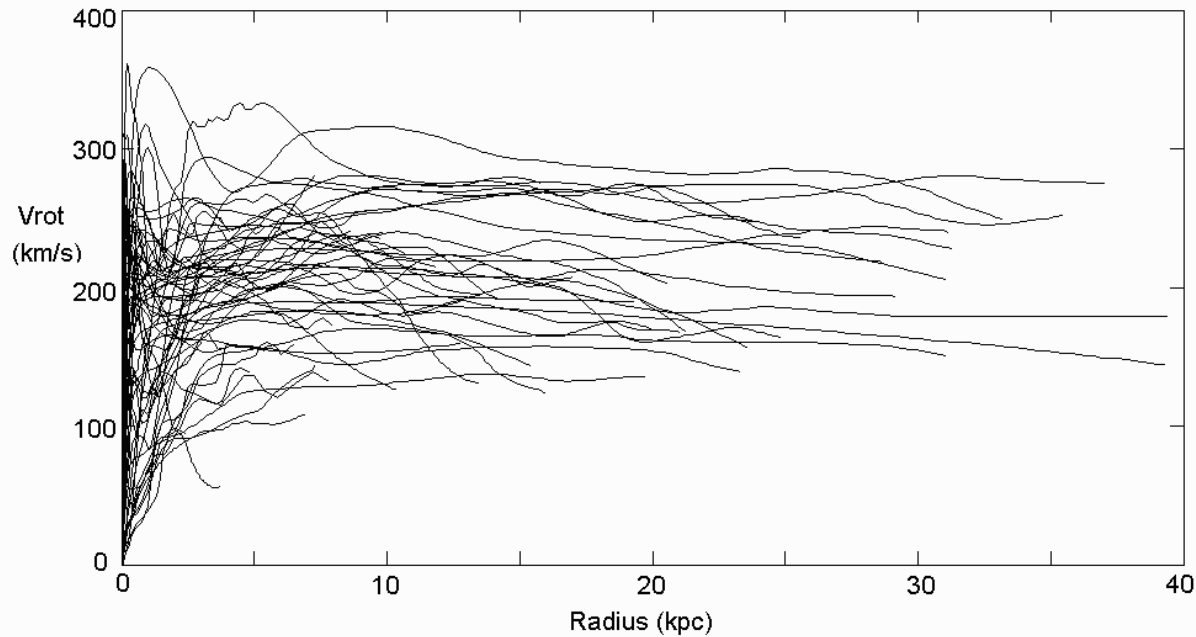


Galaxies with HI

M83: optical



HI: cartography of atomic hydrogen
Wavelength 21cm



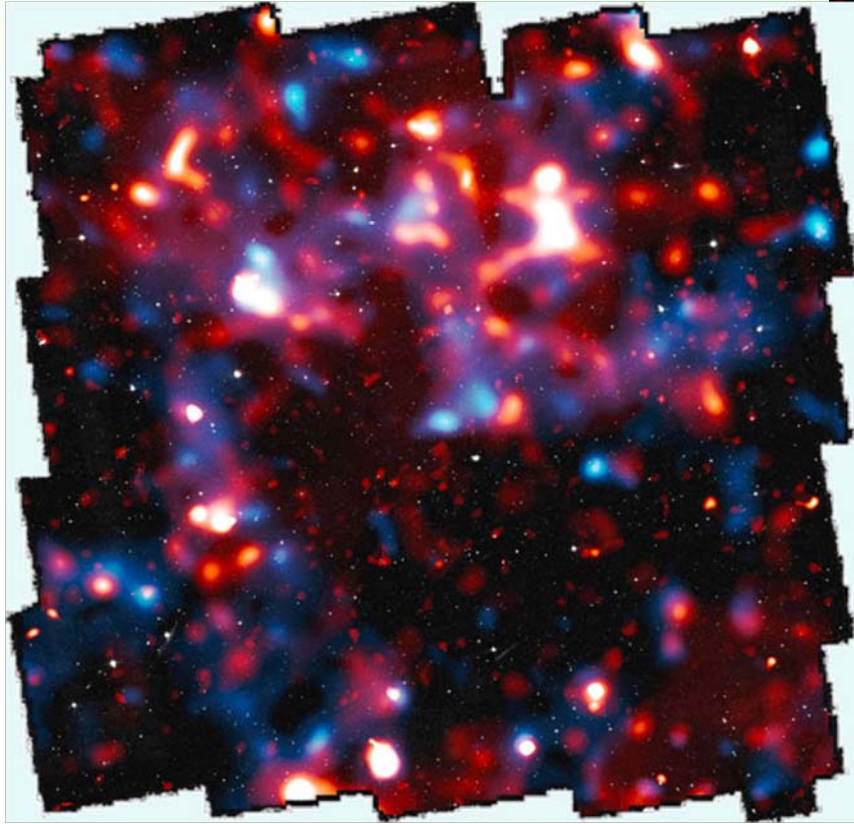
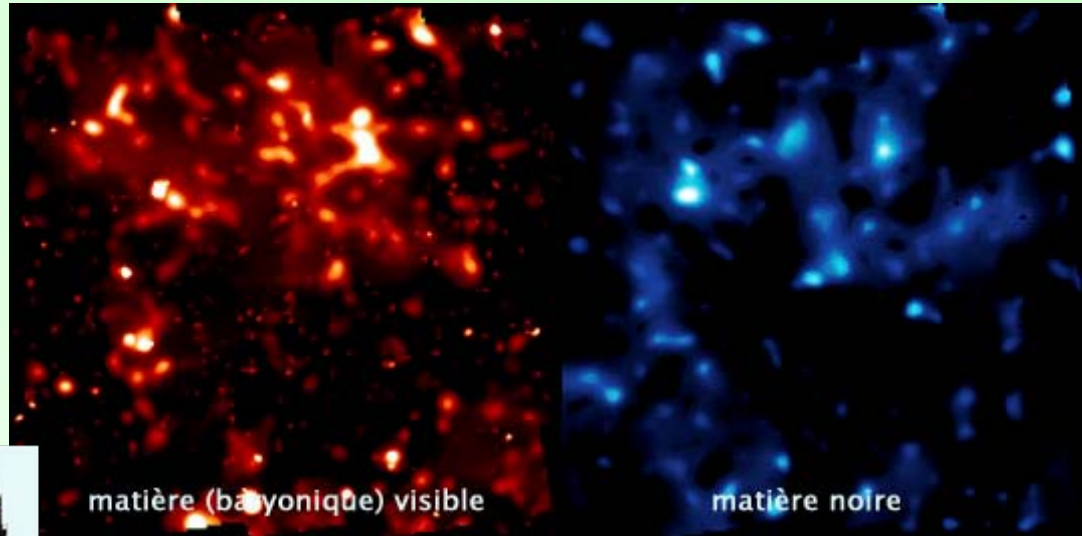
HI in M83: a galaxy similar to the Milky Way³

Gravitationnal shear, weak lensing

Red: X-ray gas

Blue: total matter

Cosmos field



**Constraints on the
Dark Matter, and
Dark Energy**

Massey et al 2007

Tully-Fisher relation

Relation between maximum velocity
and luminosity

ΔV corrected from inclination

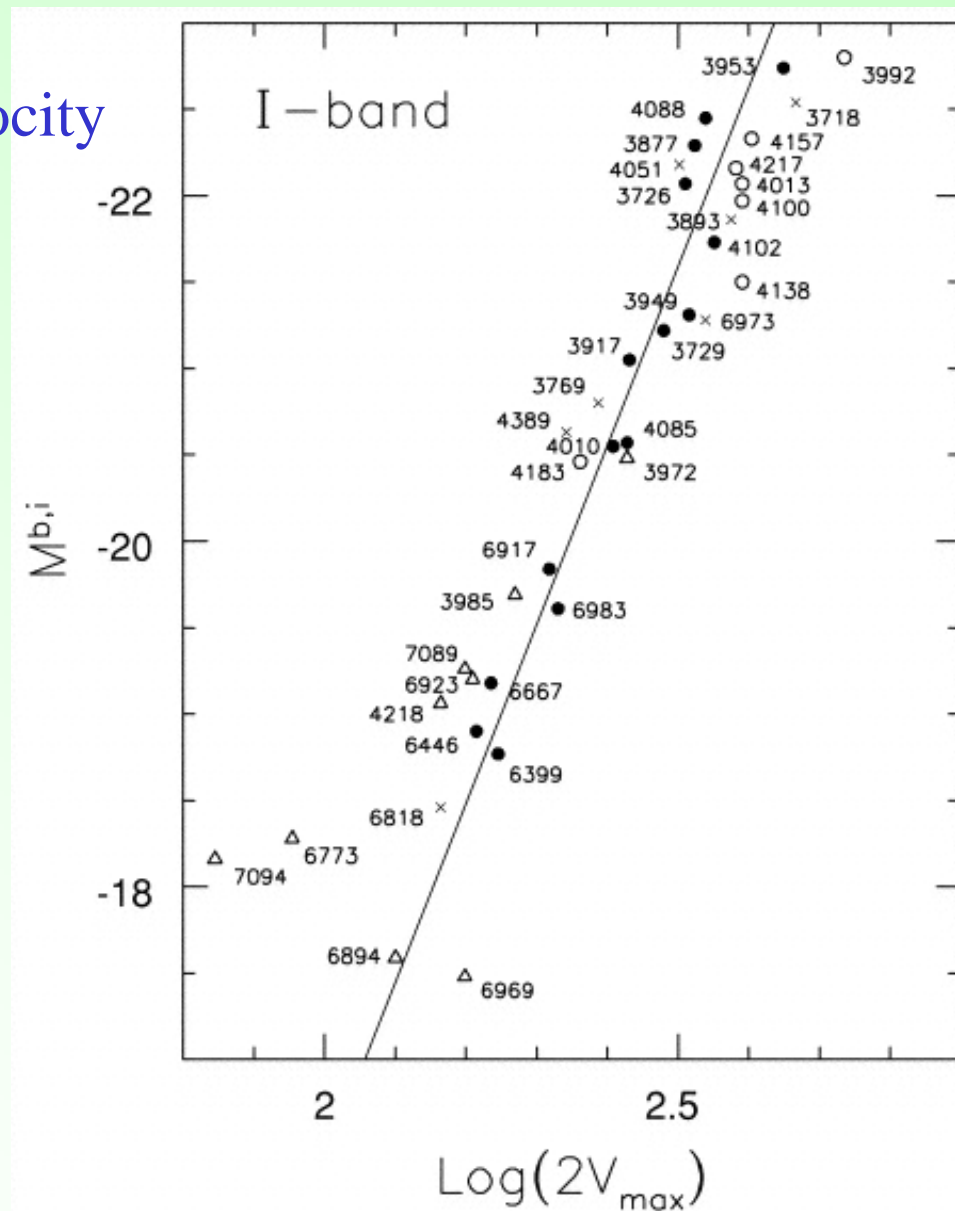
Much less scatter in I or K-band
(no extinction)

Correlation with V_{flat}

Better than V_{max}

Uma cluster

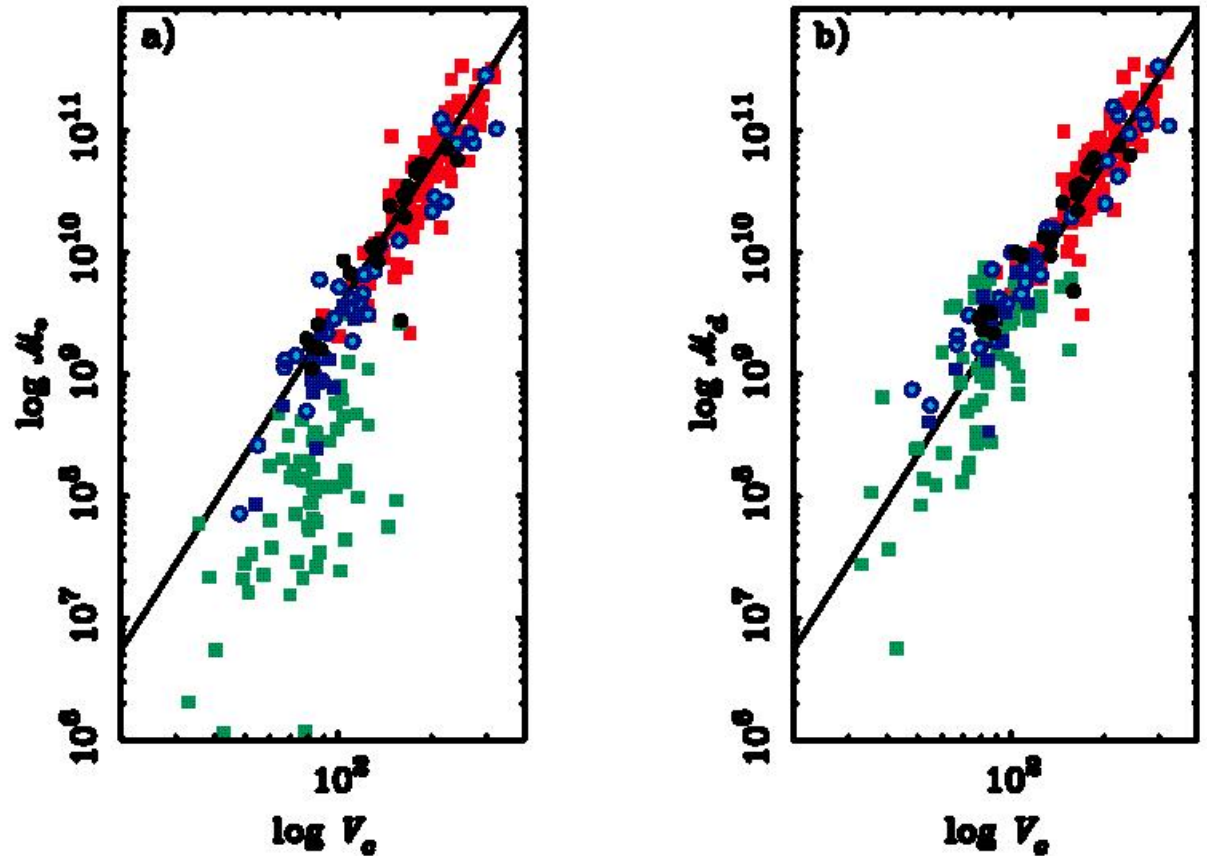
Verheijen 2001



Tully-Fisher relation
for gaseous galaxies
works much better in
adding gas mass

Relation M_{baryons}
with Rotational V

$$M_b \sim V_c^4$$



McGaugh et al (2000) → **Baryonic Tully-Fisher**

Where are the baryons?

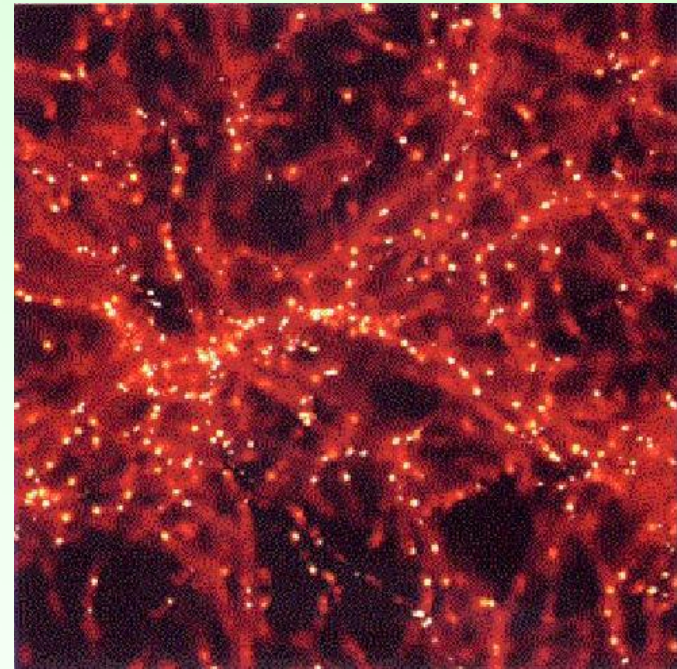
→ 6% in galaxies ; 3% in galaxy clusters as hot X-ray gas

→ <18% in the Lyman-alpha forest (cosmic filaments)

→ 5-10% in the WHIM (Warm-Hot Intergalactic Medium) 10^5 - 10^6 K OVI lines

→ 65% are not yet identified or localised!

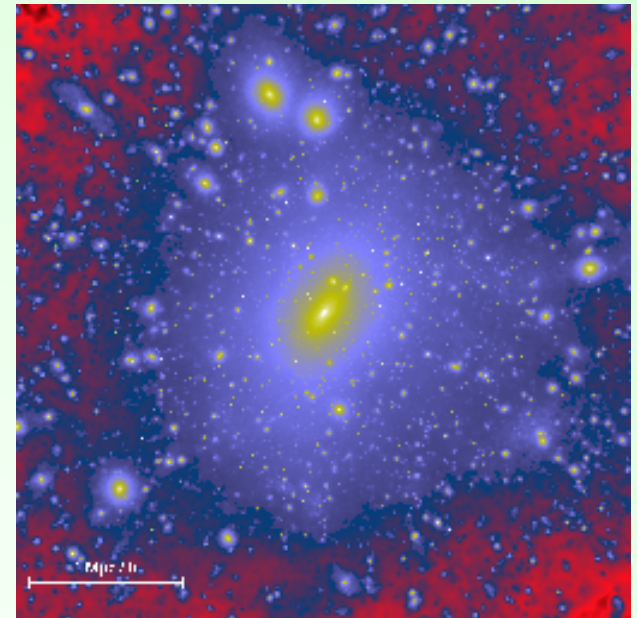
Most of them are not in galaxies



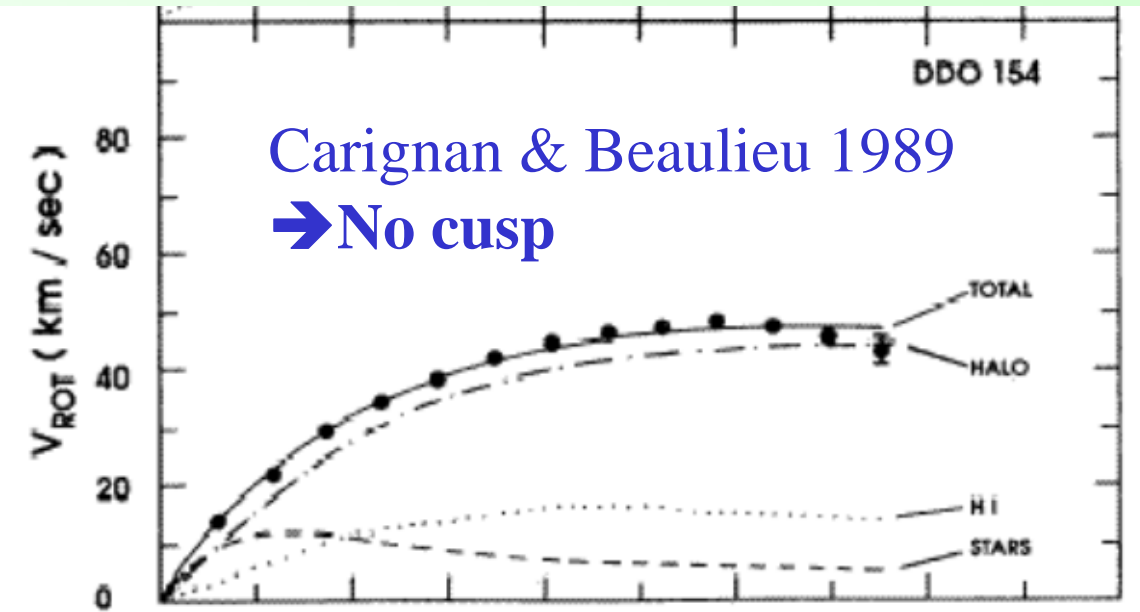
Problems of the standard Λ -CDM model

- Prediction of **cusps in galaxy center**, which are in particular absent in dw-Irr, dominated by dark matter
- Low angular momentum of baryons, and as a consequence **formation of much too small galaxy disks**
- Prediction of a **large number of small halos**, not observed

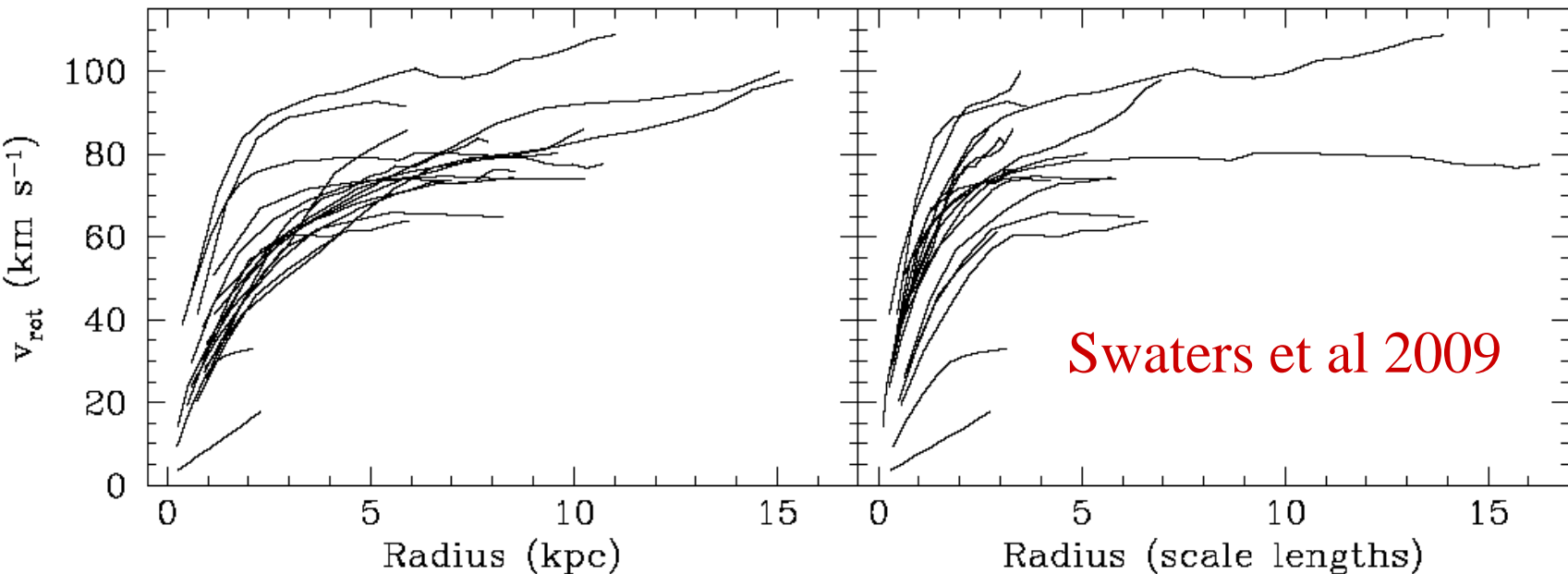
The solution to all these problems could come from unrealistic baryonic physics (SF, feedback?), or lack of spatial resolution in simulations, or wrong nature of dark matter?



Dwarf Irr : DDO154 the prototype



Even the LSB late-type galaxies are dominated by baryons (stars) in their centers



MOND = MOdified Newtonian Dynamics

Modification at weak acceleration

$$a = (a_0 a_N)^{1/2}$$

$$a_N \sim 1/r^2 \rightarrow a \sim 1/r \rightarrow V^2 = \text{cste}$$

$$\nabla \cdot [\mu(|\nabla\phi|/a_0)\nabla\phi] = 4\pi G\rho$$

$$\rightarrow a^2 \sim V^4/R^2 \sim GM/R^2 \text{ (TF)}$$

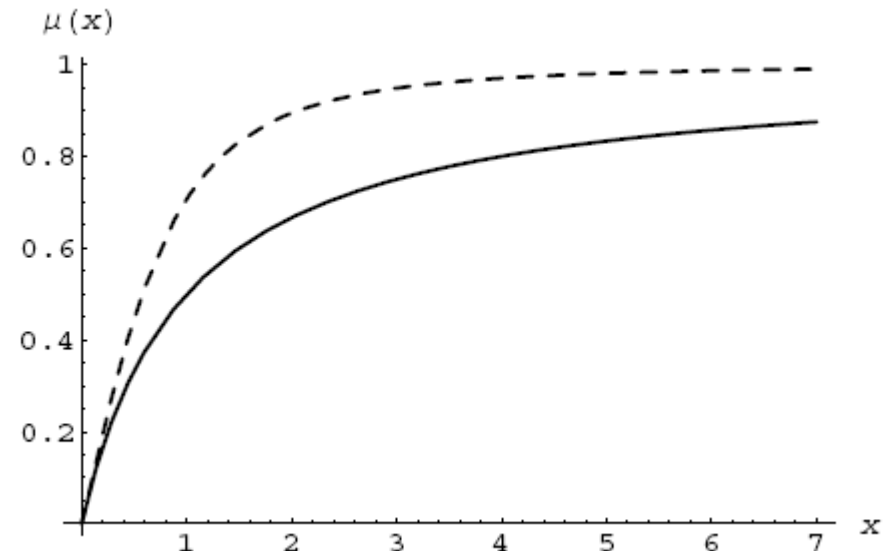
(Milgrom 1983)

$$a_N = a \mu(x)$$

$$x = a/a_0 \quad a_0 = 1.2 \cdot 10^{-10} \text{ m/s}^2 \quad \text{or} \quad 1 \text{ Angstroms/s}^2$$

$x \ll 1$ Mondian regime $\mu(x) \rightarrow x$

$x \gg 1$ Newtonian $\mu(x) \rightarrow 1$



Covariant theory, general relativistic

TeV S Tensor/Vector/Scalar
Bekenstein (2004)

$$\mu(y) = \frac{\sqrt{y/3}}{1 - \frac{4\pi\alpha}{k} \sqrt{y/3}}$$

To replace General relativity in weak curvature

➔ Introduces a 5th force, violation of SEP (not of WEP)

Can get out naturally from some string theory models
(Mavromatos & Sakellariadou 2007)

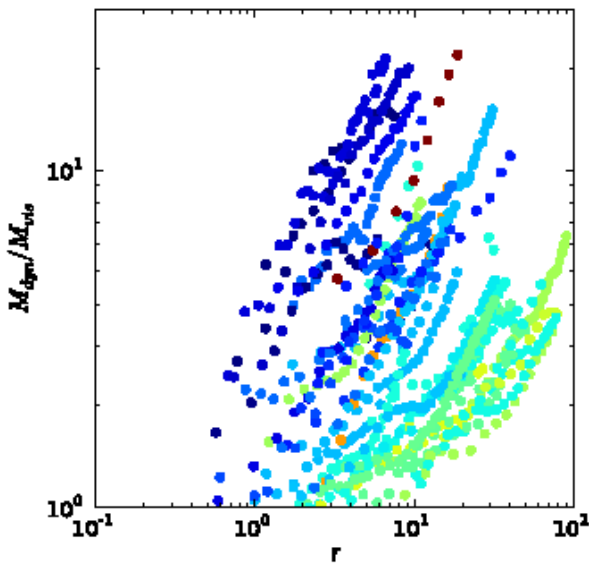
Einstein aether developments
Many other tentative theories

Recent developments: Vector field with non-linear coupling with
space-time metric (Zloznik et al, 2007, Zhao, 2008)

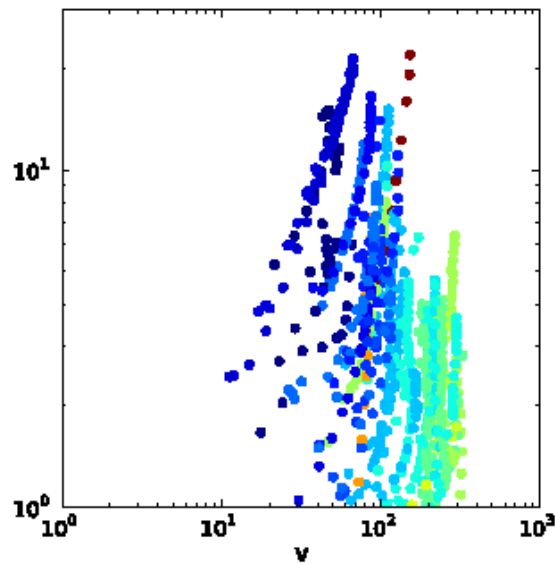
Dynamic Mass / Visible Mass

The ratio remarkably depends on acceleration,

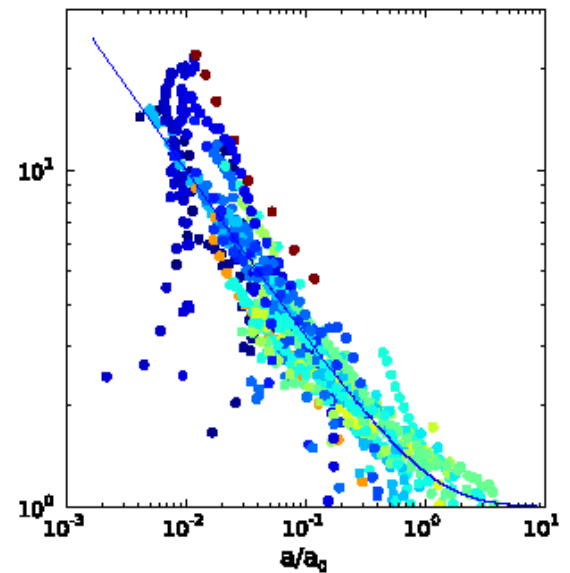
→ The only variable controlling the gravity regime universally



Radius



Velocity

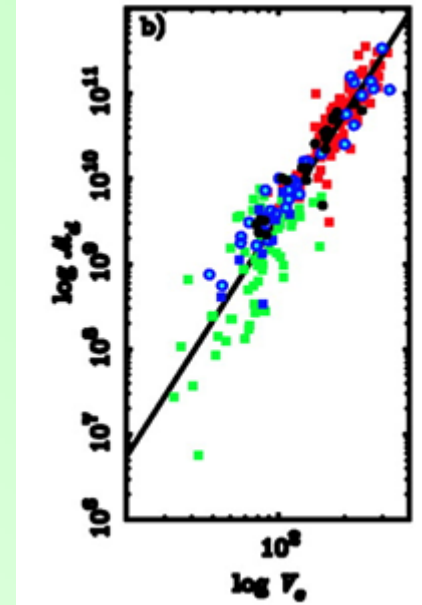


Acceleration

Tully-Fisher relation

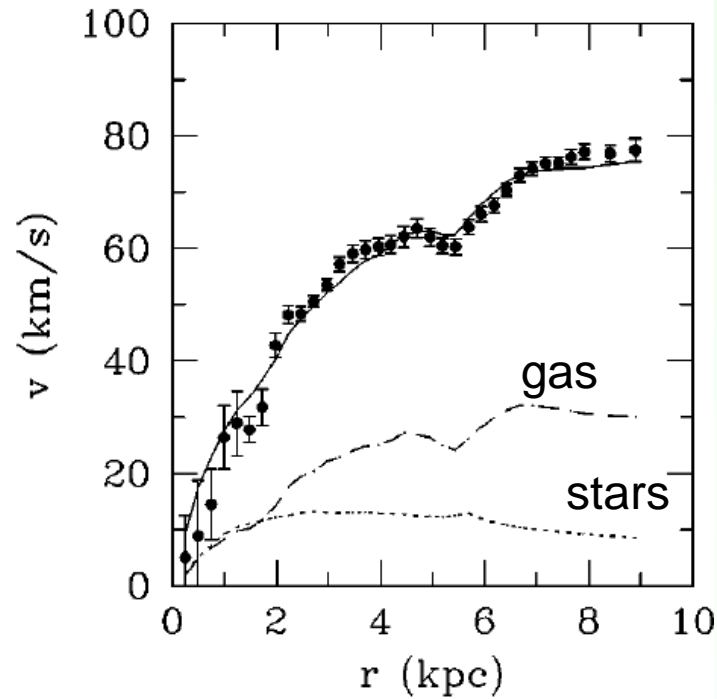
$$g_M^2 = a_0 g_N = a_0 GM/r^2 = V^4/r^2$$

$$\rightarrow V^4 = a_0 GM$$

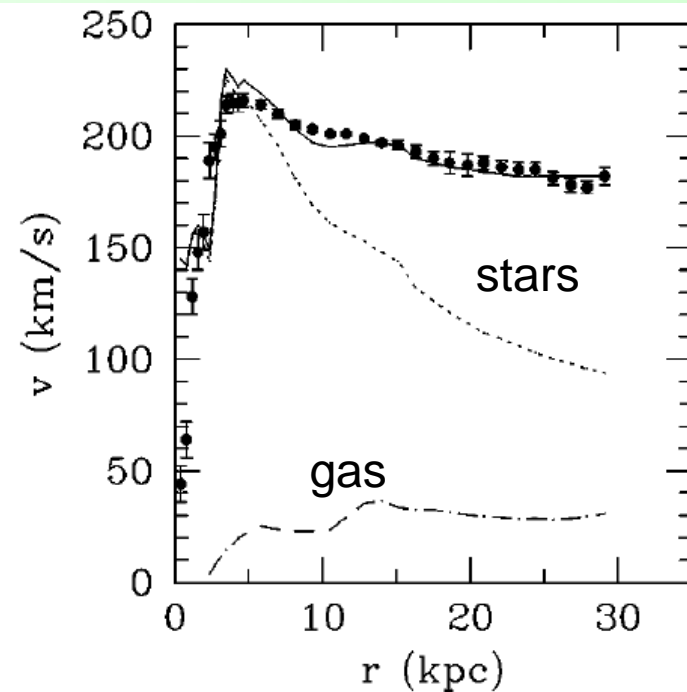


Rotation curves are fit for all types
(dwarfs **LSB**, giant **HSB**)

LSB N1560



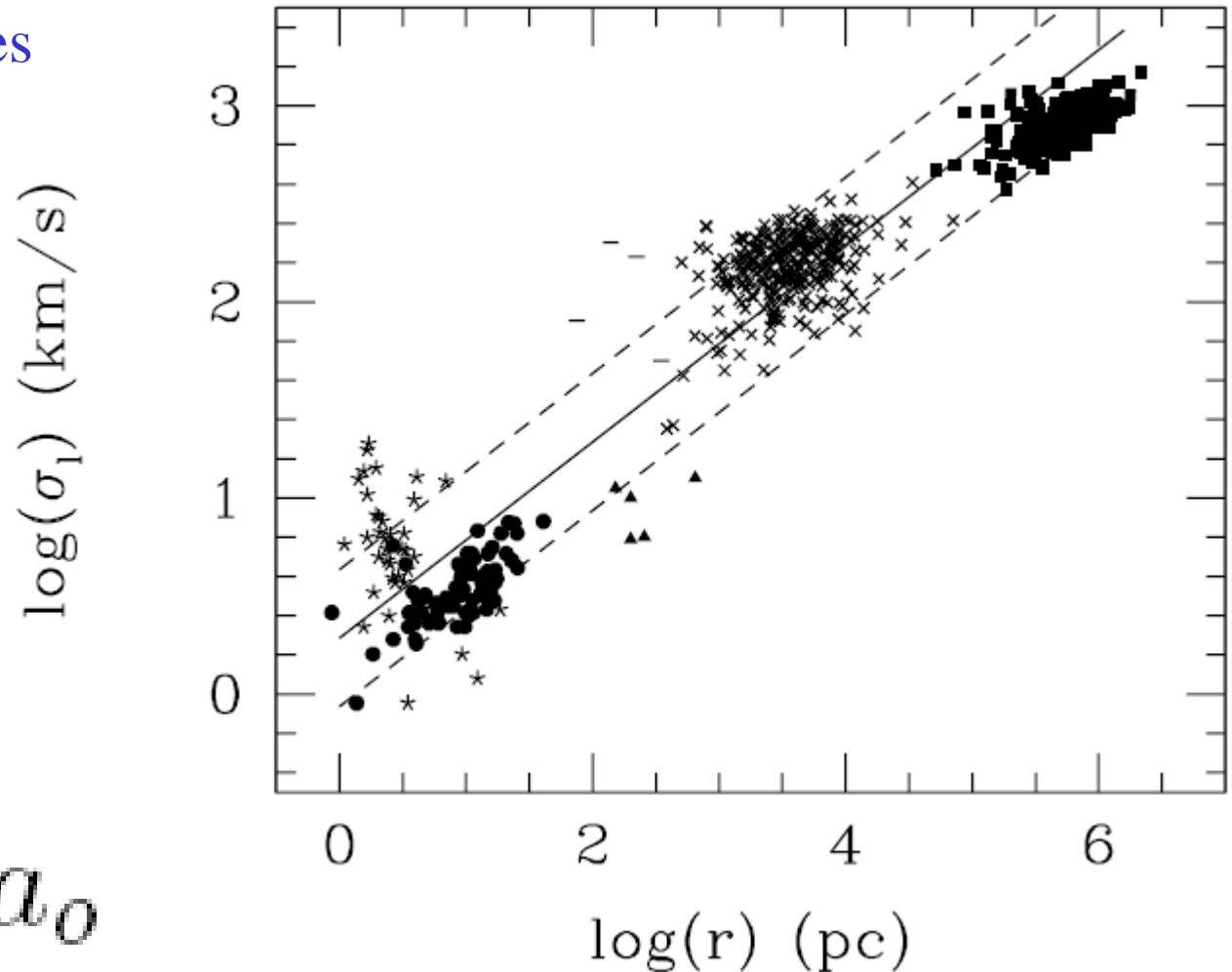
HSB N2903



Pressure-supported systems

Sanders & McGaugh 2002

From GC to galaxies
and clusters

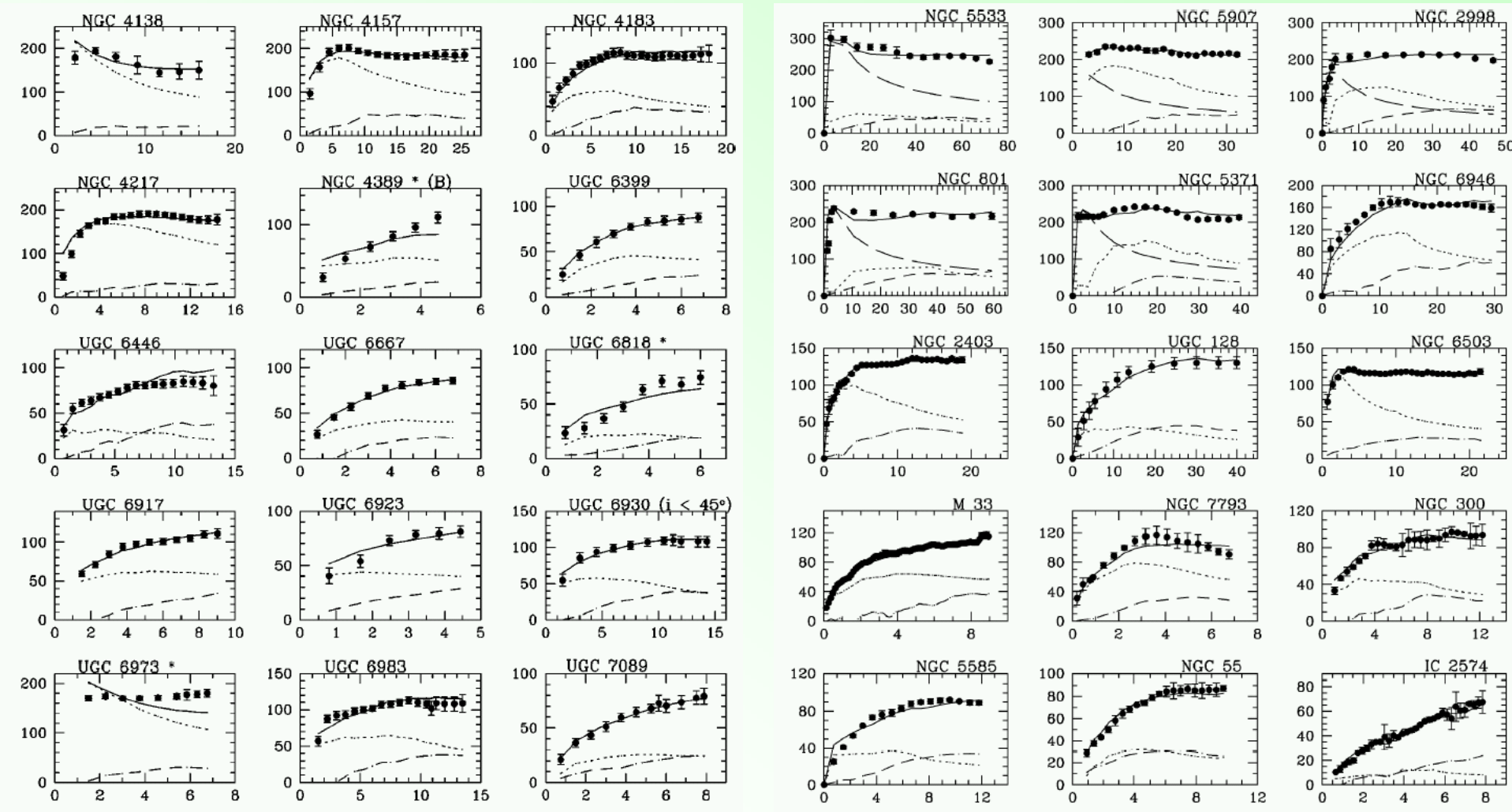


$$\sigma_l^2 / r = a_0$$

Multiple rotation curves..

Sanders & Verheijen 1998, all types, all masses

--- gas, Stellar disk, --- bulge



Problems of MOND in galaxy clusters

Inside galaxy clusters, there still existing some missing mass, which cannot be explained by MOND, since **the cluster center** is only moderately in the MOND regime ($\sim 0.5 a_0$)

Observations in X-rays: hot gas in hydrostatic equilibrium, and weak gravitational lenses (shear)

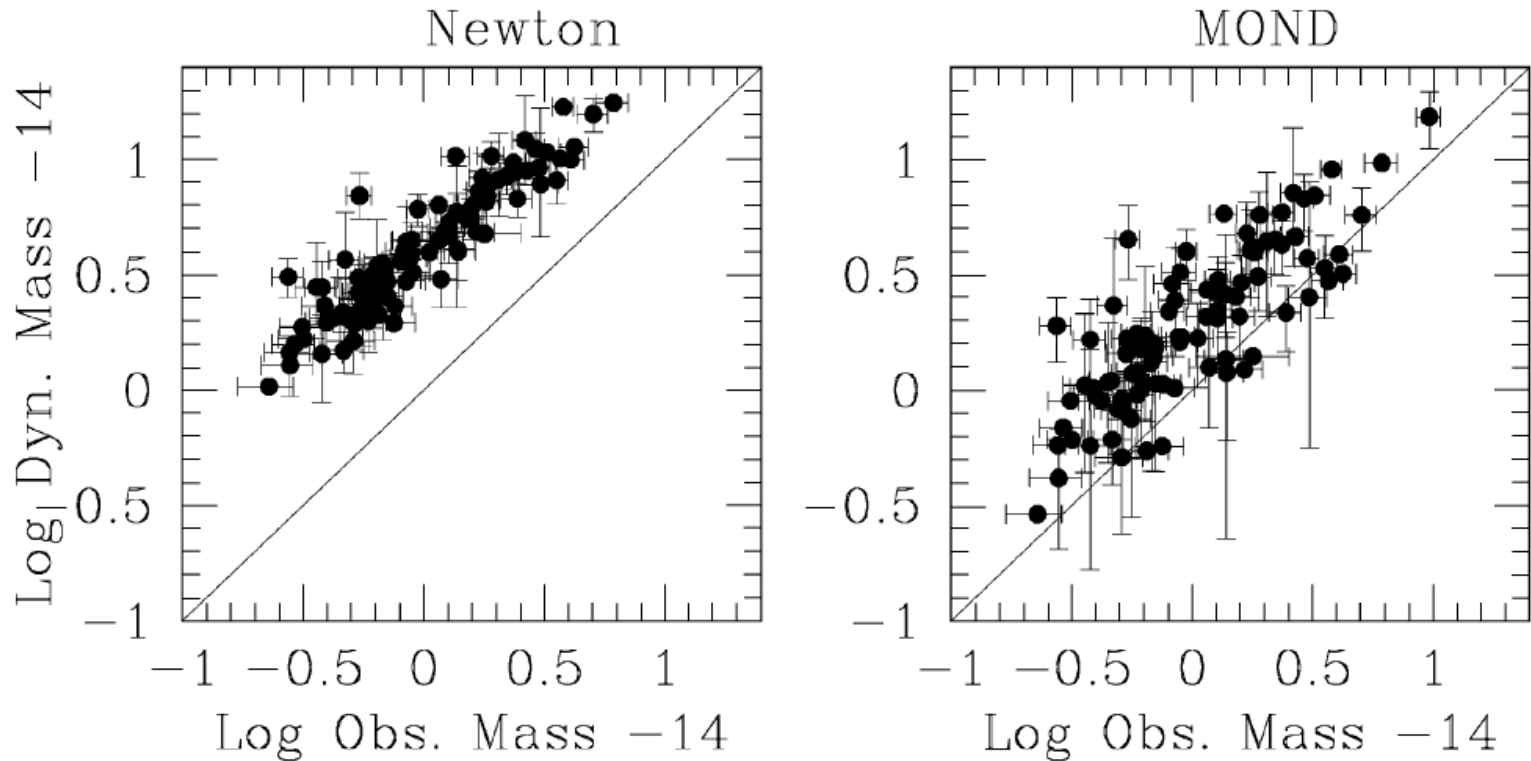
MOND reduces by a factor 2 the missing mass

➔ It remains another component, which could be neutrinos....
(plus baryons)

The baryon fraction is not the universal one in clusters
(so baryons could still exist in the standard Λ CDM model)

But if CDM does not exist, there is no limiting fraction

MOND & galaxy clusters

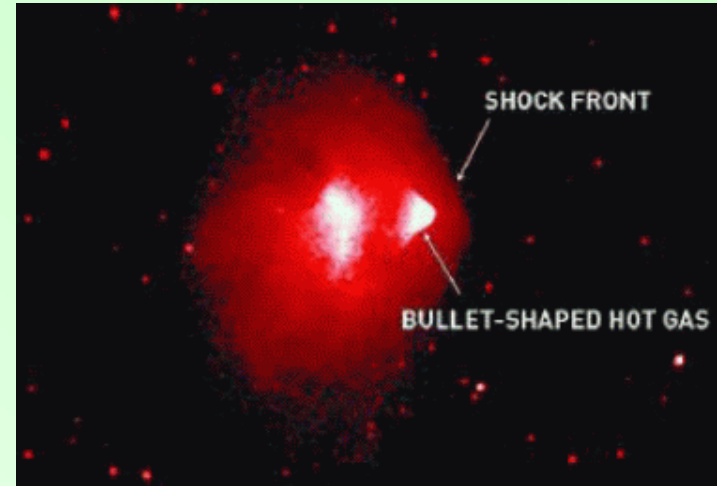


According to baryon physics, cold gas could accumulate at the cluster centers

Alternatively, neutrinos could represent 2x more mass than the baryons

The bullet cluster

X-ray gas



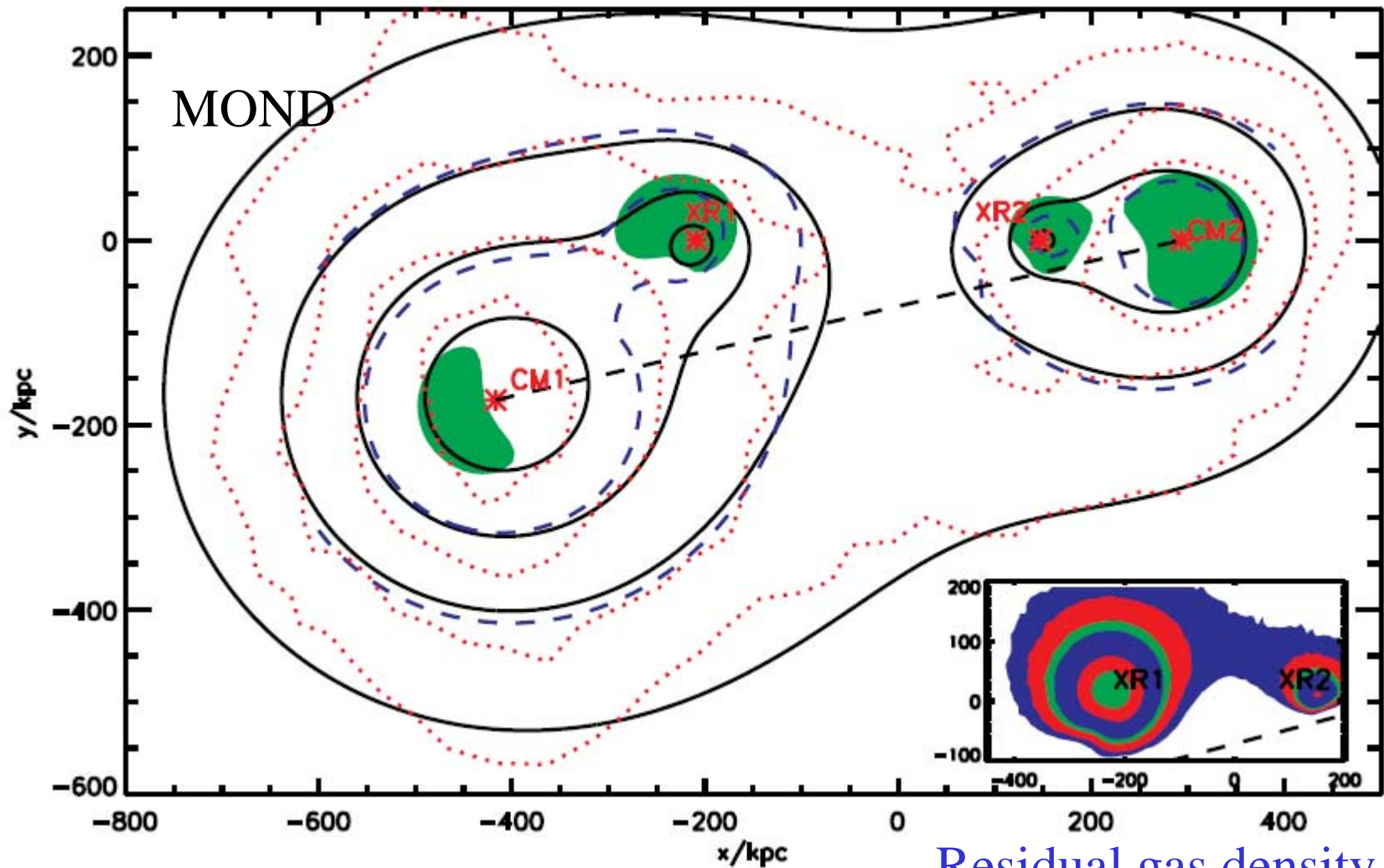
Proof of the existence of non-baryonic matter

Total mass

Accounted for in MOND + neutrinos (2eV, Angus et al 2006) ¹⁸

Model of the bullet in MOND

..... Clowe et al 2006, Angus et al 2007



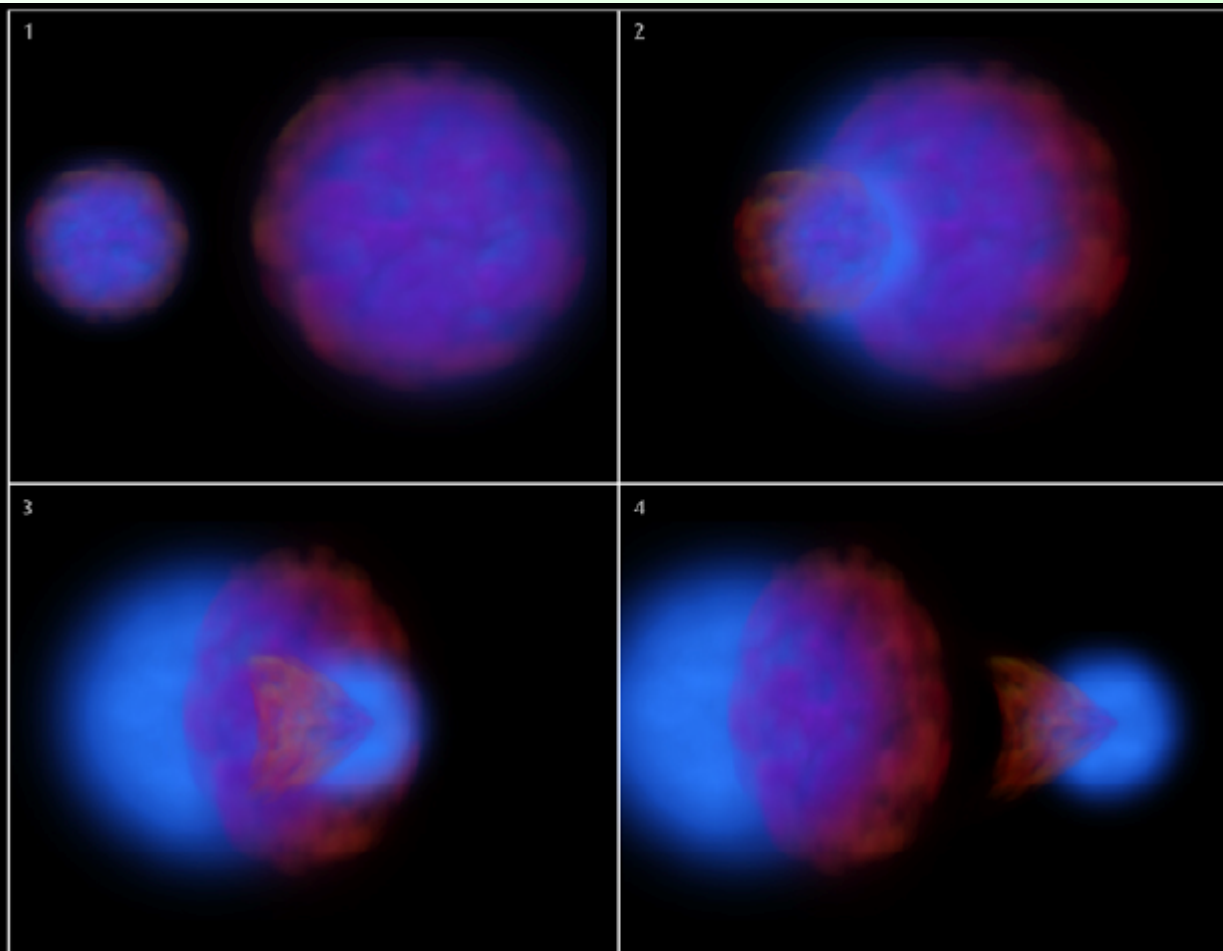
CDM simulation

Collision velocity from the bow-shock = $4700 \pm 500 \text{ km/s}$ (Mach 3)

Hayashi & White 2006 Farrar & Rosen 2007

→ impossible to reconcile with CDM

Milosavljevic et al 2007, Springel & Farrar 2007



CDM can only

$V < 3500 \text{ km/s}$

MOND $> 4500 \text{ km/s}$

Relative velocities
between halos

4 times higher in MOND

Linares et al 2009

Collision by 16%
over-estimated?

V_{gas} could be higher
than V_{CDM}

Mahdavi et al 2007

Abell 520

$z=0.201$

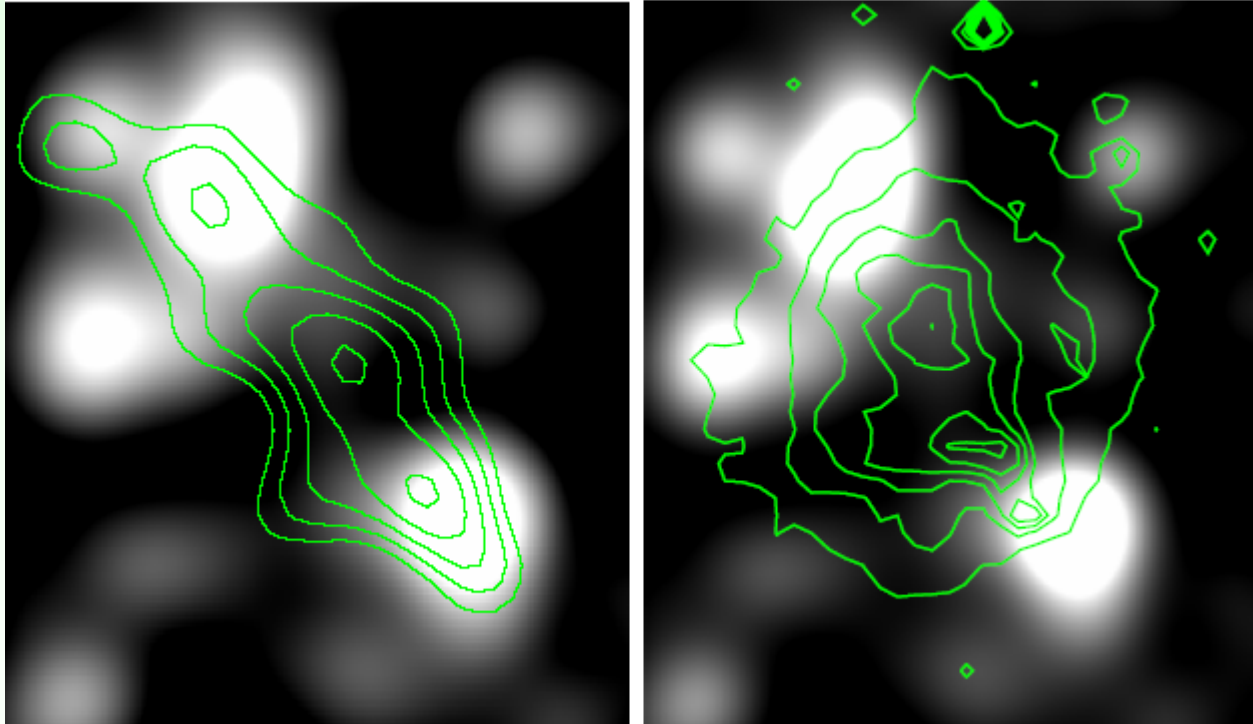
Red= X-ray gas
Contours= lensing
→ Massive DM core
Coinciding with X gas
but devoid of galaxies

Cosmic train wreck

Opposite case!



Abell 520 merging clusters



Contours=total mass

Contours = X-ray gas

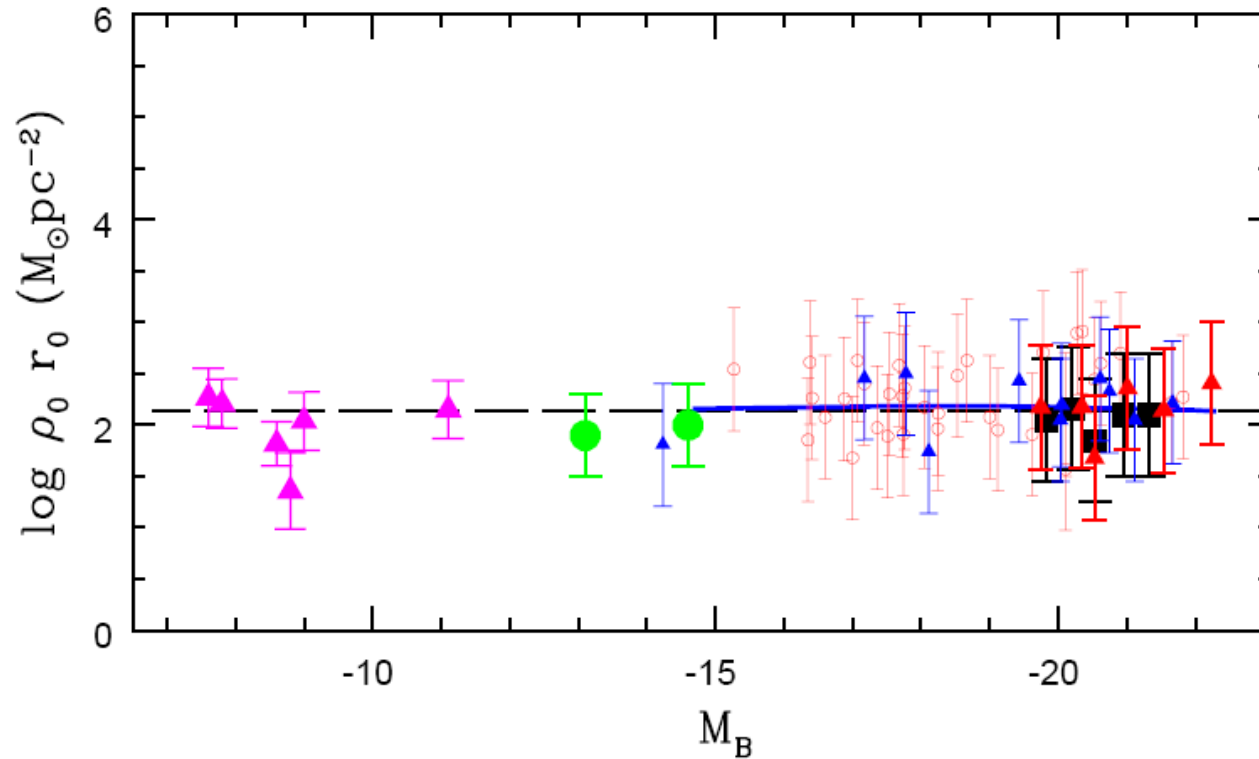
How are the galaxies ejected from the CDM peak??

Constraints on MOND from galaxy dynamics and observations

Are the stability, evolution & formation of galaxies stringent tests of the theory?

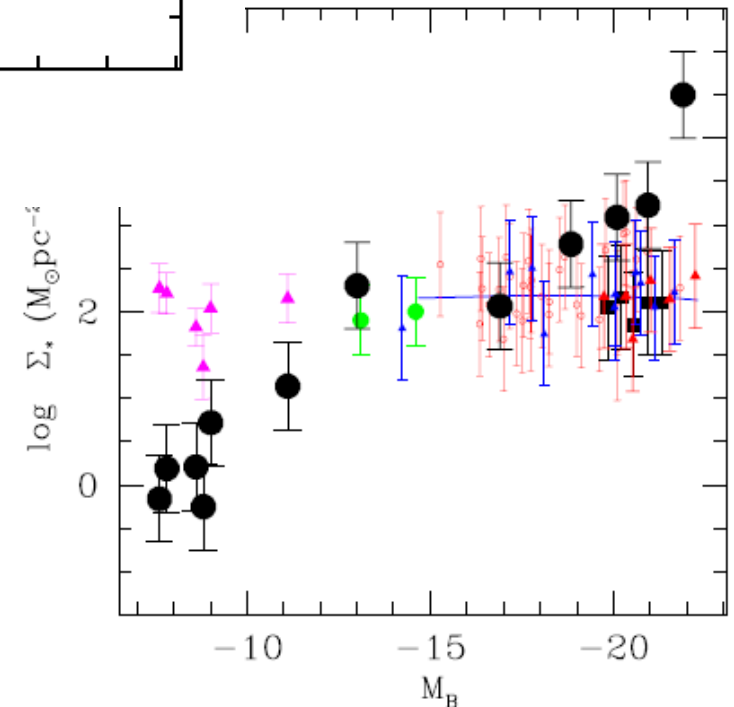
Can we determine the form of the interpolation function μ ?

Scaling laws, DM surface density



Kormendy & Freeman 2004
Gilmore et al 2007, **Donato et al 2009**

$$\Sigma_M = 142 M_\odot/\text{pc}^2$$



$$\Sigma(0) = \int_{-\infty}^{\infty} \rho_p dz = \Sigma_M [\mathcal{U}(\infty) - \mathcal{U}(0)] = \Sigma_M \int_0^{\infty} L(x) dx \equiv \lambda \Sigma_M,$$

Implications

$$\rightarrow \Sigma_M = 138 (a_0/1.2 \text{ E}10 \text{ m/s}^2) \text{ M}_\odot/\text{pc}^2$$

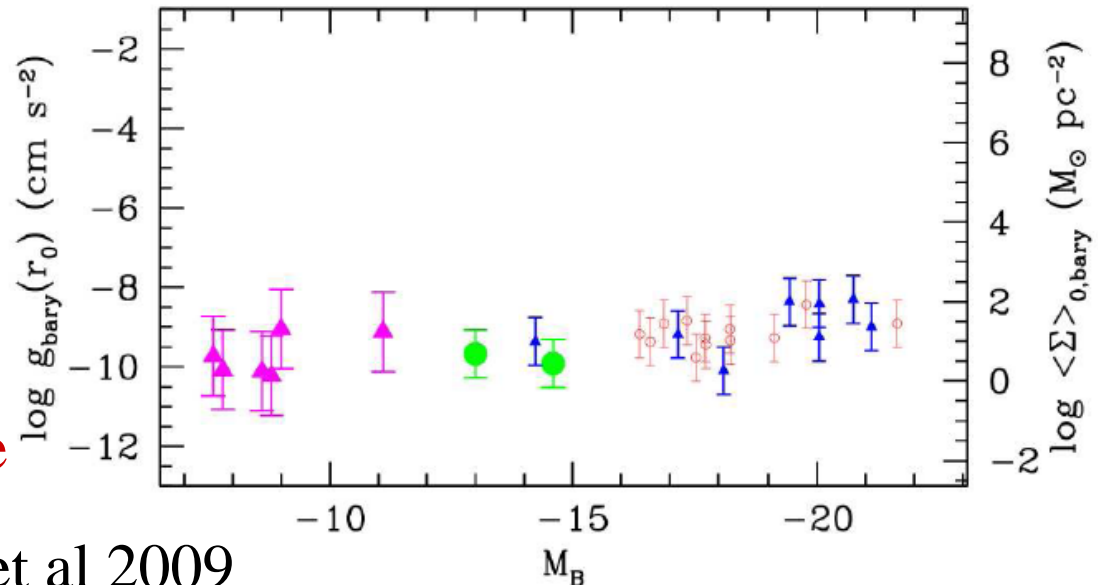
In MOND: the « phantom »
dark matter added under
the Newton hypothesis,
has the appearance of a
Cste Σ , $\propto a_0$
(Milgrom 2009)

At least if the central parts
are Newtonian

It is possible to have systems
with lower densities $\sim 0.5 \Sigma_M$
Not in the Donato et al sample

Large central Σ_b means
high DM core radius

The DM core radius is where
the acceleration falls below
 $6 \cdot 10^{-10} \text{ m/s}^2$



Gentile et al 2009

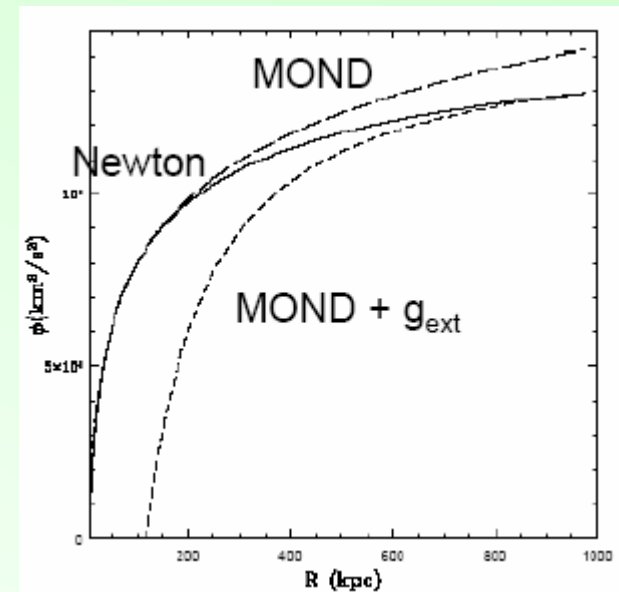
Escape velocity

Potential in the MONDian regime $\Phi(r) = (GMa_0)^{1/2} \ln r$

$$\frac{1}{2} V_{\text{esc}}^2 = \Phi(\infty) - \Phi(r) \rightarrow \text{no escape possible!}$$

But a galaxy is never totally isolated \rightarrow External field effect (EFE)

$$-\nabla \cdot [\mu(x)g] = 4\pi G\rho(X, Y, Z), \quad x \equiv \frac{|g|}{a_0}.$$



EFE: External Field Effect

If external field g_e , is in the **X** direction

At large radii, it is equivalent to a dilatation Δ

$$\Phi_{\text{int}}^{\infty}(X, Y, Z) = - \frac{GM_{\text{int}}}{\mu_m \sqrt{(1 + \Delta)(Y^2 + Z^2) + X^2 + s^2}},$$

Define an internal potential Φ_{int}

$$\nabla^2 \Phi_{\text{int}} + \Delta \frac{\partial^2}{\partial X^2} \Phi_{\text{int}} \rightarrow 4\pi G\rho/\mu_m,$$

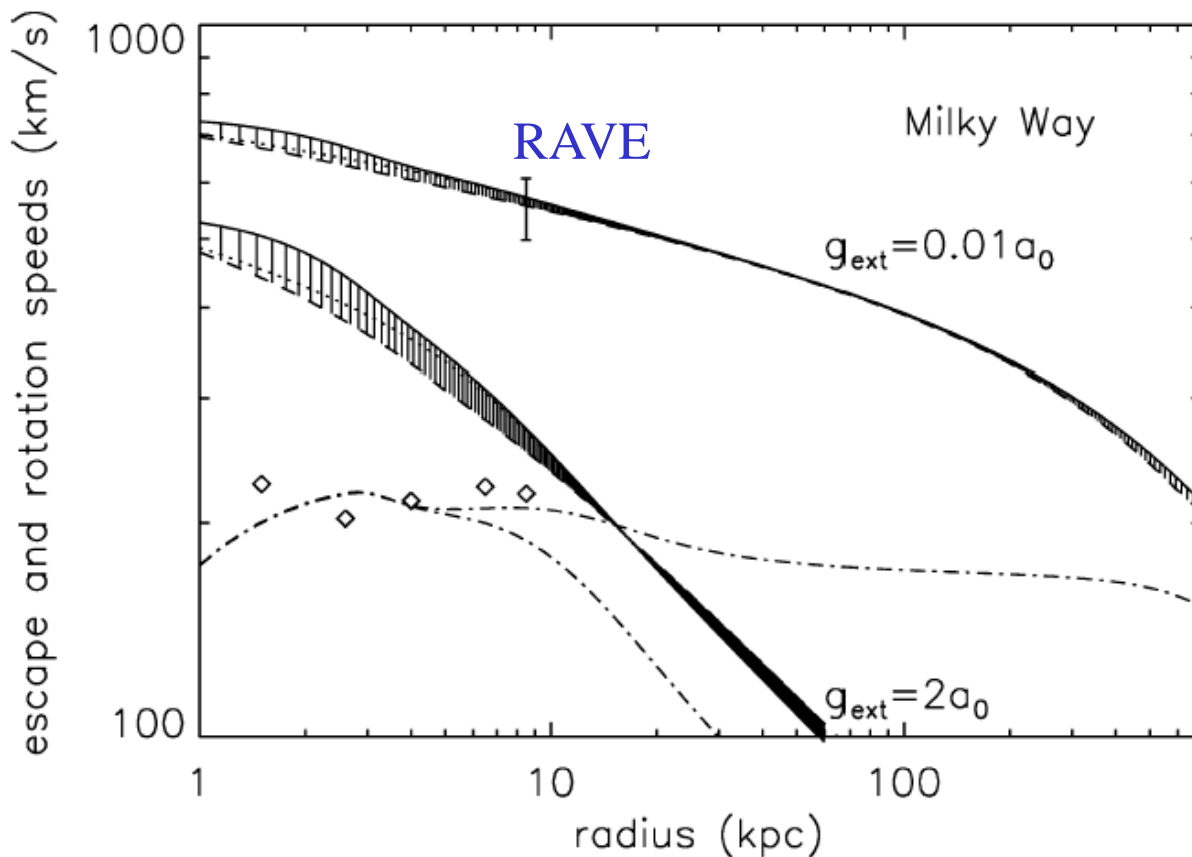
Where $g \ll g_e \ll a_0$

Keplerian dependence, with renormalization $G \rightarrow Ga_0/g_e$

Milky Way: effect from Andromeda

Observations RAVE (Smith et al 2007) $\rightarrow 498 < v_{\text{esc}} < 608 \text{ km s}^{-1}$

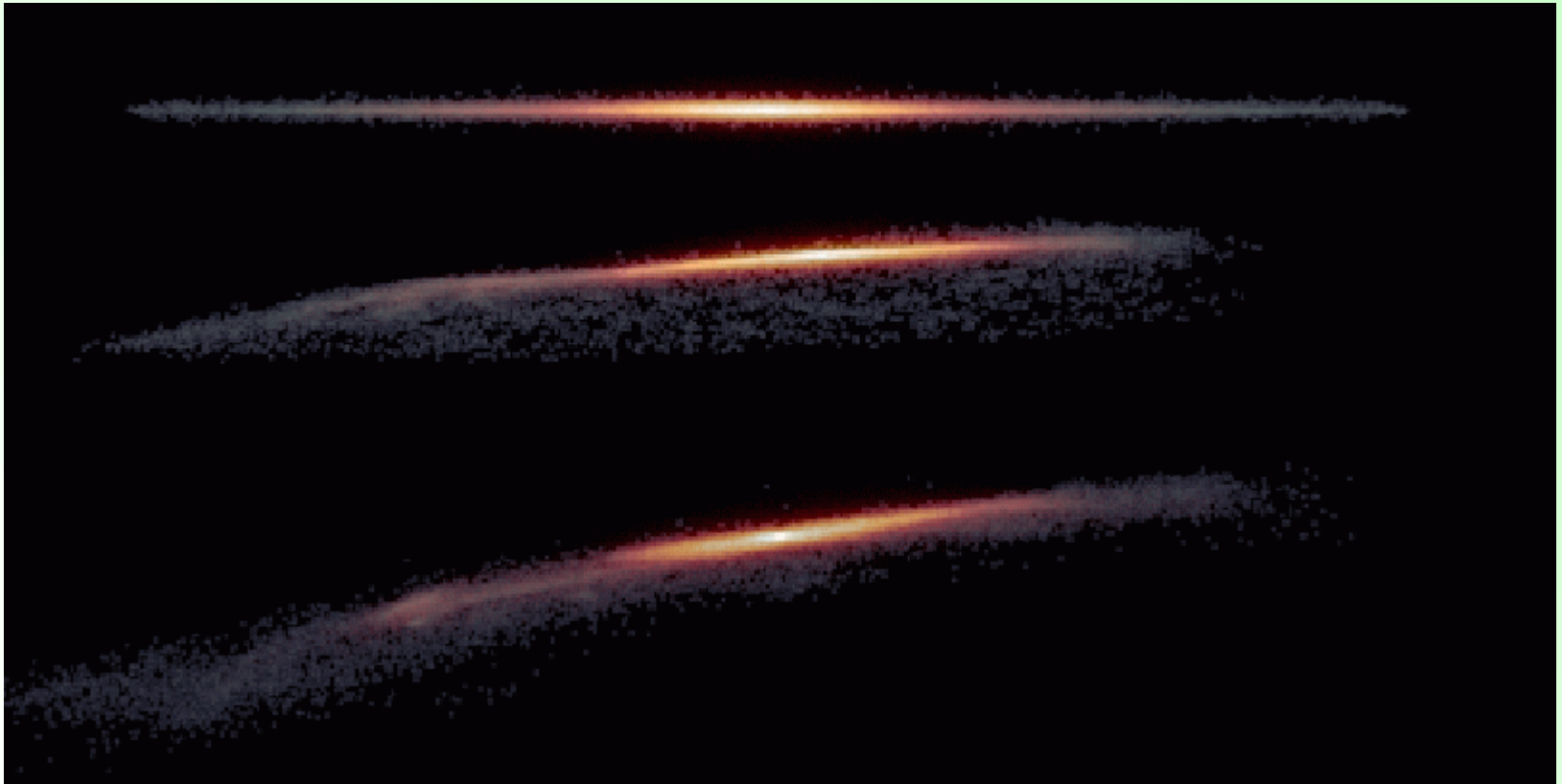
$$544 \text{ km/s} \rightarrow g_e = a_0/100$$



Wu et al 2007
Simulations with
the Besançon
model of MW

EFE: precession

Newton: no effect



MOND: non-linear effect, gravitationnal torque and precession

Violation of the strong equivalence principle

→ Origine of Warps? (also Brada & Milgrom 2000, LMC/MW)
29

Orbit of the LMC (Large Magellanic Cloud)

Recent proper motions measurements with **HST**
Reveal that the velocity of the LMC is 378km/s
(SMC 302km/s)

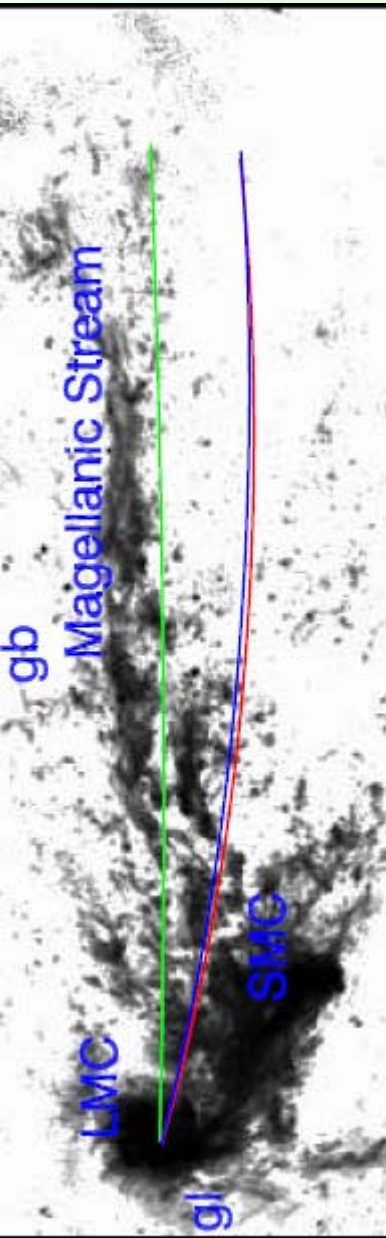
Kallivayalil et al 2006, Piatek et al 2007

100km/s higher than before, close to escape

→ First passage of LMC+SMC

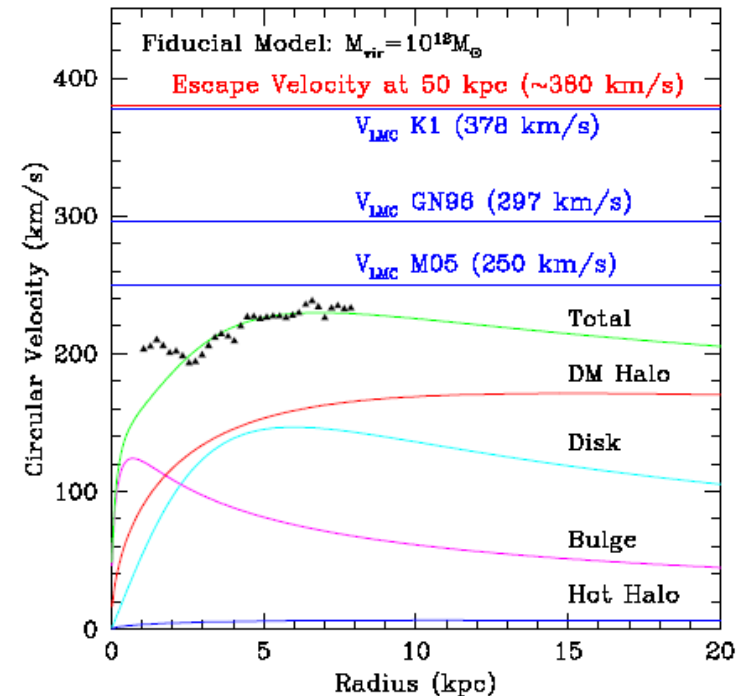
→ Origin of the Magellanic Stream?

Besla et al 2007



Tidal forces,
or ram-pressure stripping?
Efficiency?

Ruzicka et al 2008,
Mastropietro 2008



Stability of galaxy disks

spirals and bars are the motor of evolution

CDM: Spheroidal haloes stabilise the disks

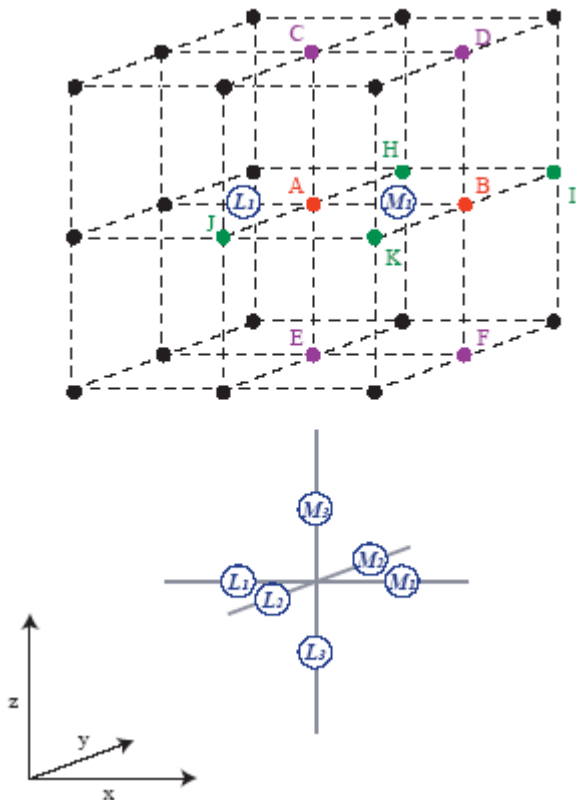
MOND; disks are entirely self-gravitating

However, the gravity law is not linear
but in $M^{1/2}$ in the MOND regime

Bars grow when angular momentum is transferred
→ accepted by spheroidal haloes

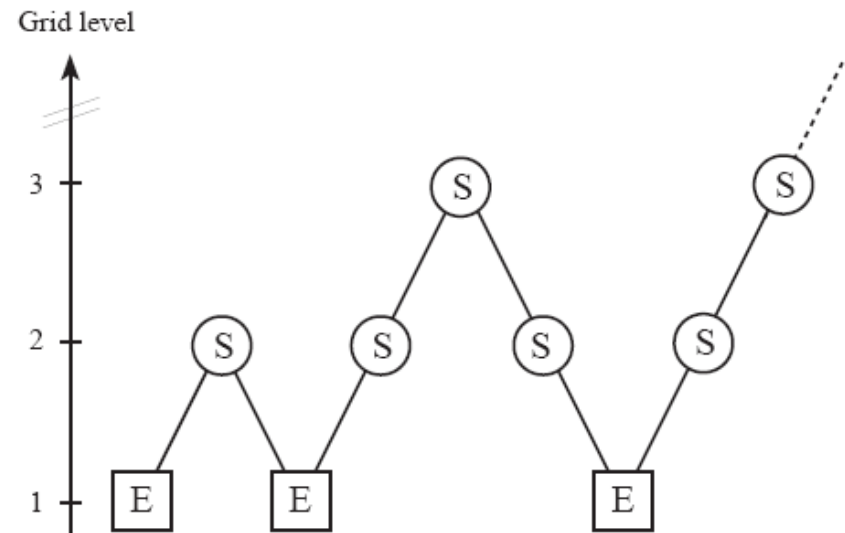
Disk dynamics in MOND

Multi-grid algorithm



Finite Differences + adaptative grid

$$\nabla[\mu(|\nabla\Phi|/a_0)\nabla\Phi] = 4\pi G\rho,$$



Interpolation

Restriction

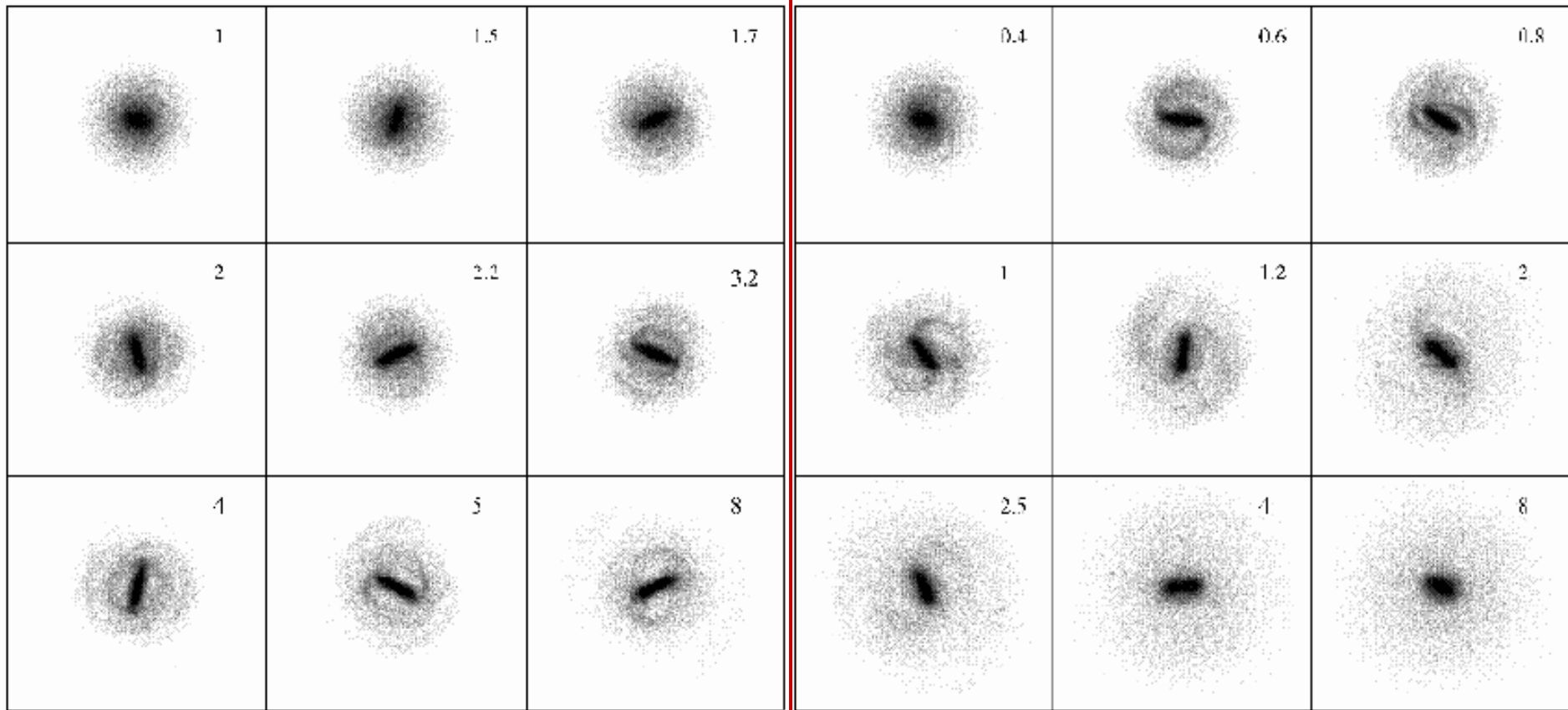
E Exact

Ⓢ Smoothing

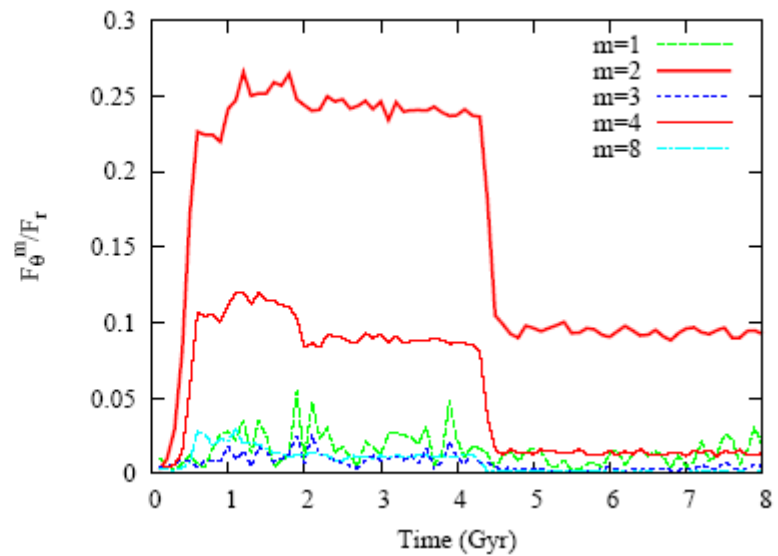
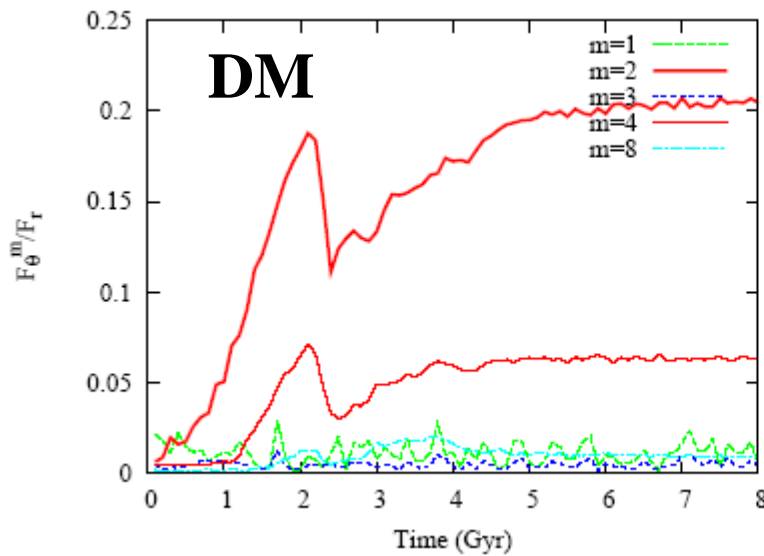
Influence of DM halo

With DM halo

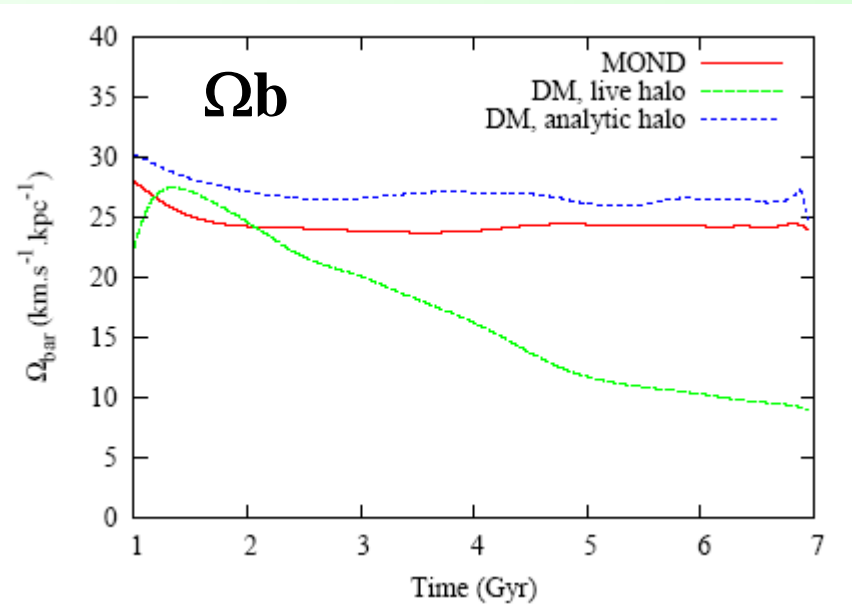
Without DM (MOND)



Bar strength and pattern speed with and w/o DM

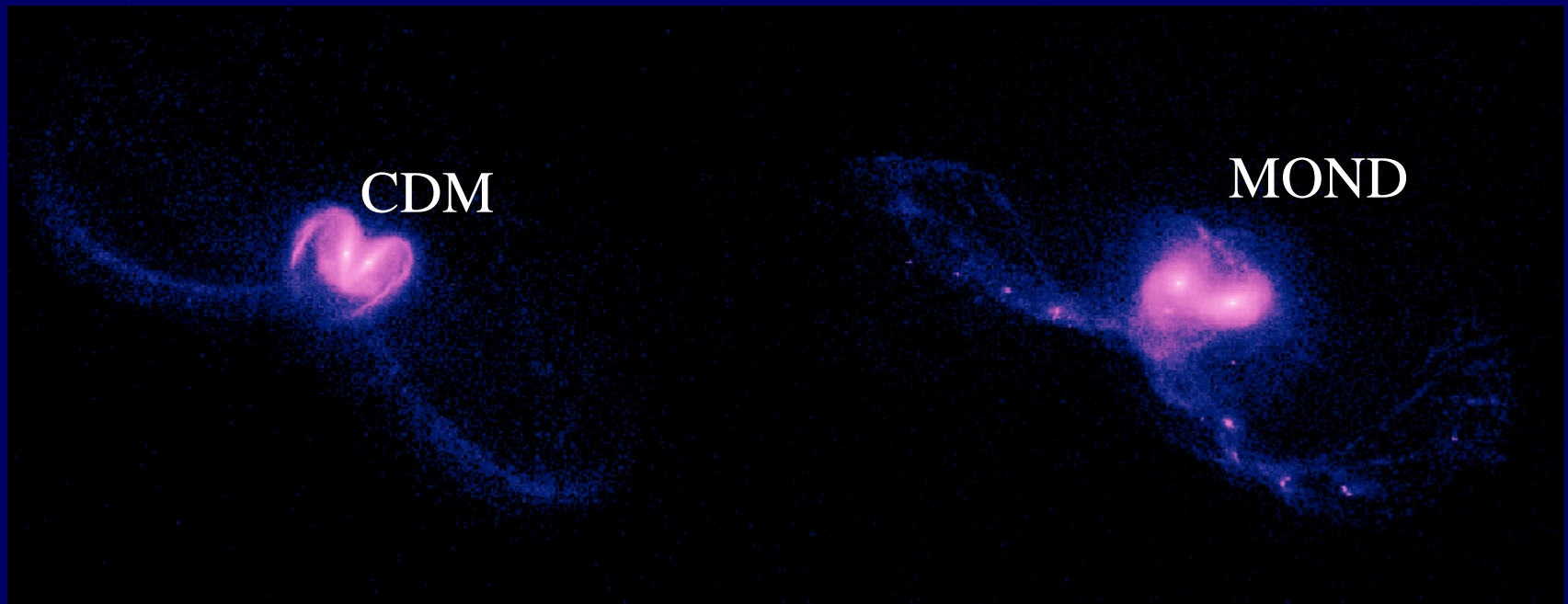


With DM, the bar appears later, and can reform after the peanut weakening through halo AM exchange, \rightarrow But Ω_b falls off



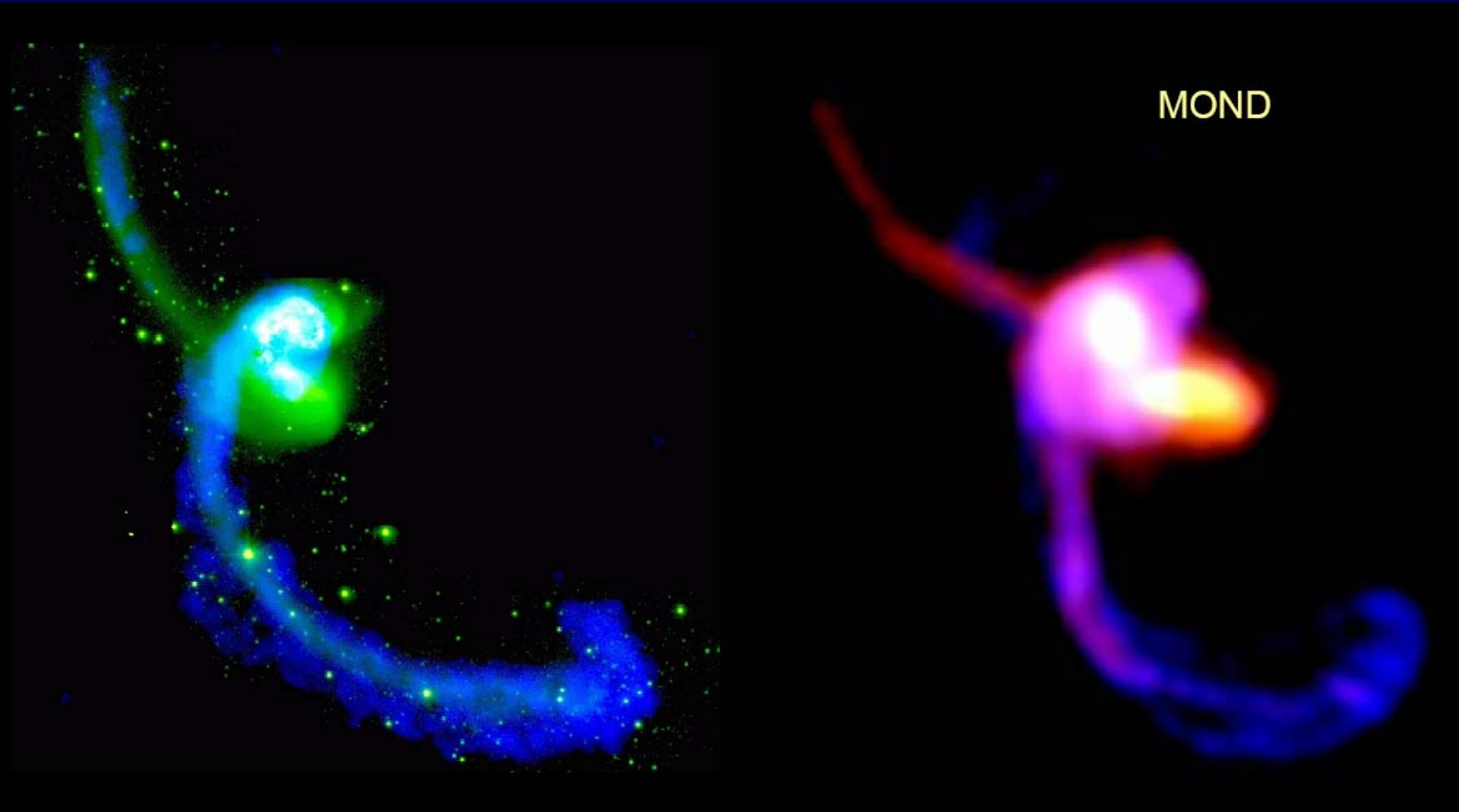
Interactions of galaxies: the Antennae: MOND versus CDM

Dynamical friction is much lower with MOND: mergers last much longer

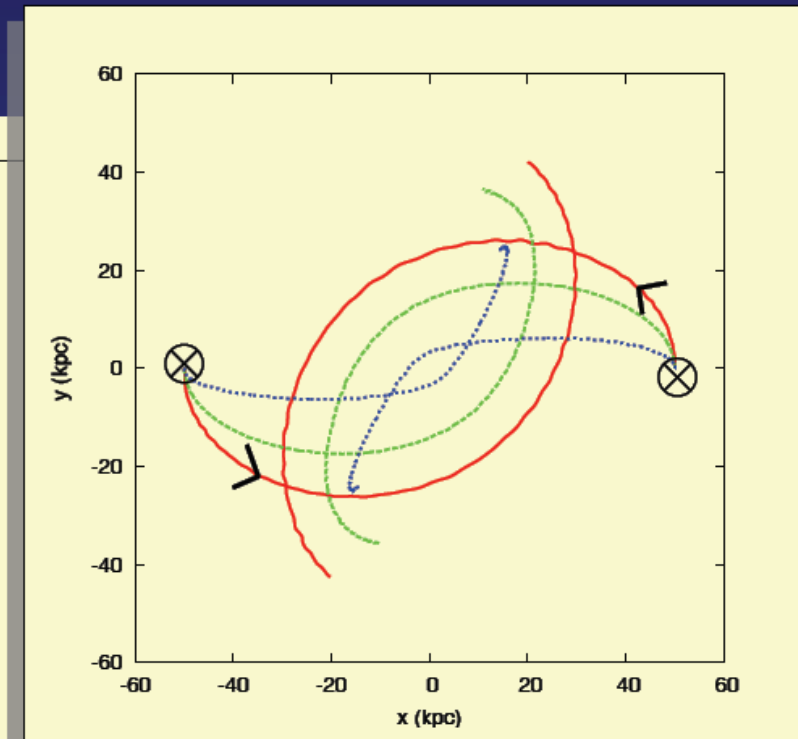
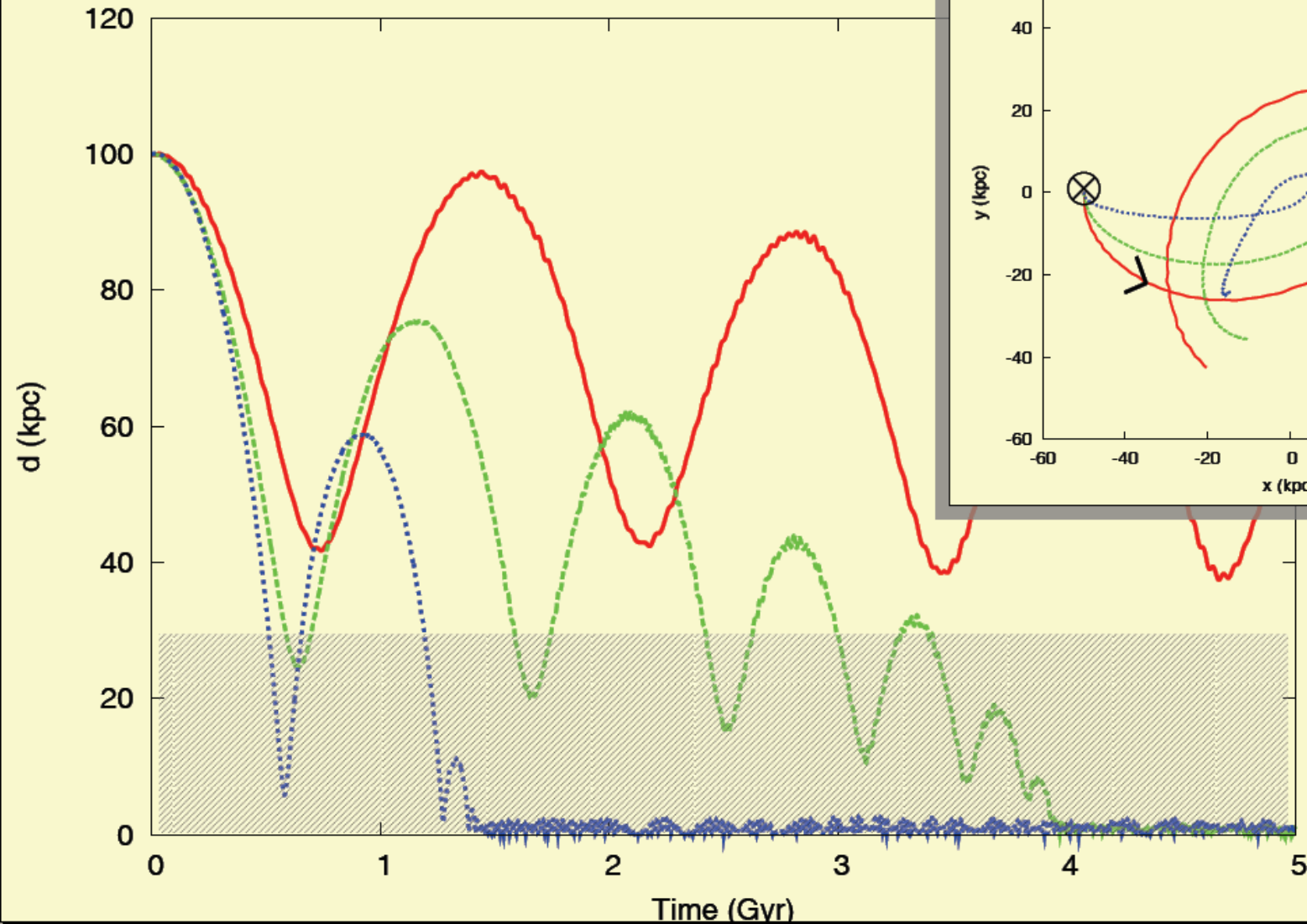


Also much longer time-scale for merging of dissipationless galaxies (Nipoti et al 2007)

Simulations of the Antennae



Dynamical friction



Dynamical friction

Analytically, the dynamical friction is **predicted stronger** with MOND than in the equivalent Newtonian system with dark matter

Ciotti & Binney 2004 (CB04), Nipoti et al 2008

However simulations show DF **less efficient** in galaxy interactions

In CDM, a lot of particles acquire E and AM, and **DF concept applicable**

➔ In MOND, a small number of particles in the outer parts acquire big quantities (no analytical treatment)

Nipoti et al 2007, Tiret & Combes 2007

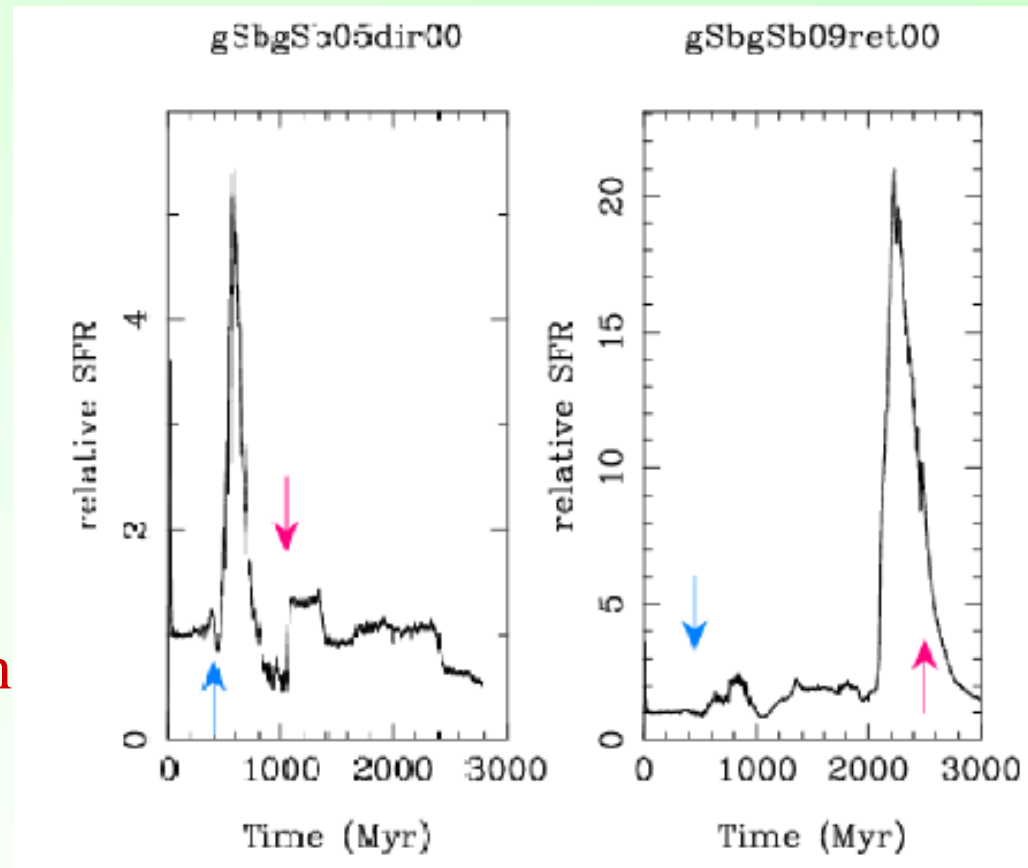
Merger induced starbursts degeneracy

CDM: dynamical friction on DM particles very efficient
→ mergers in one passage

MOND: with the same angular momentum, merger will require many passages

Starburst at each passage when minimal approach

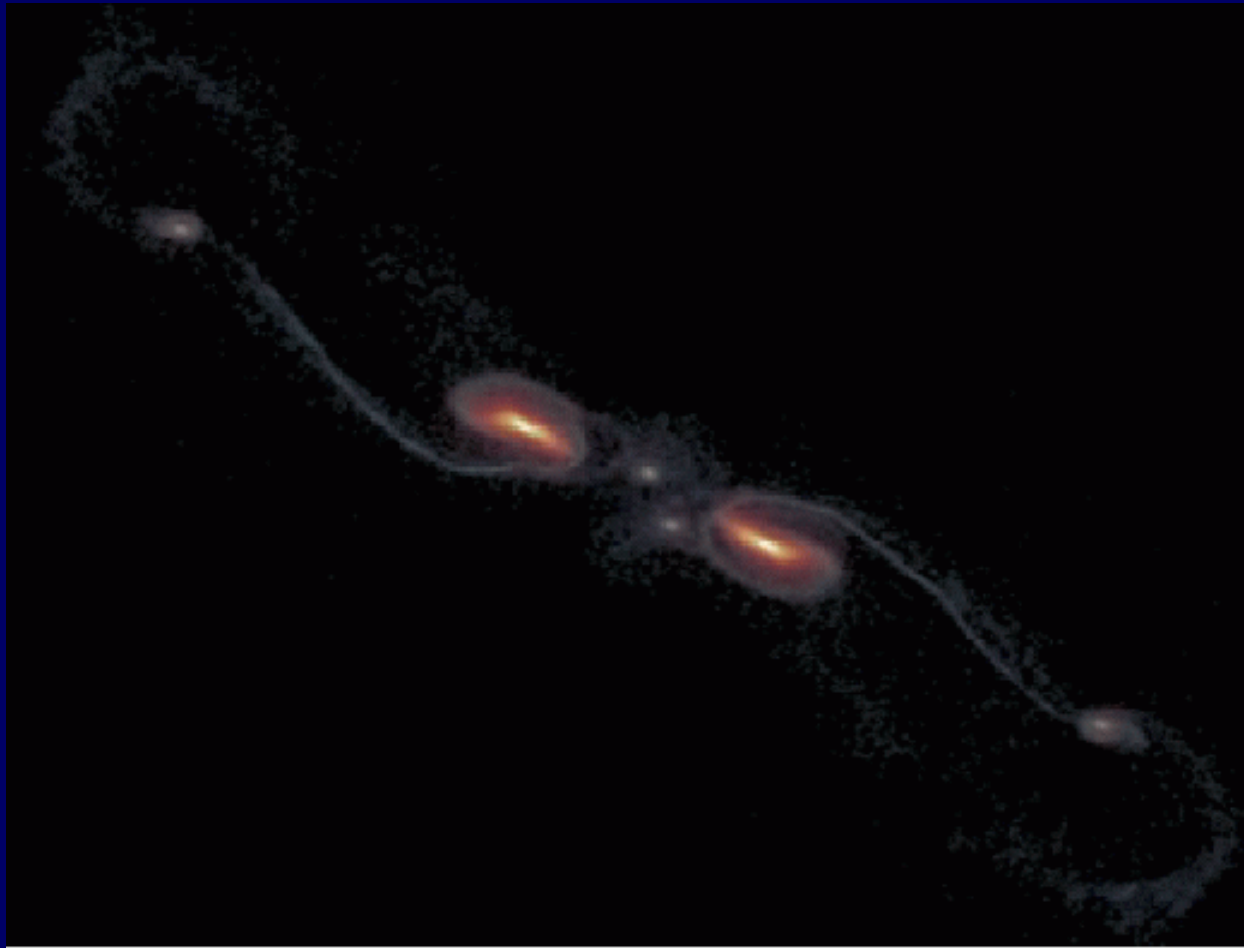
→ Number of "merger/SB" can be explained both ways



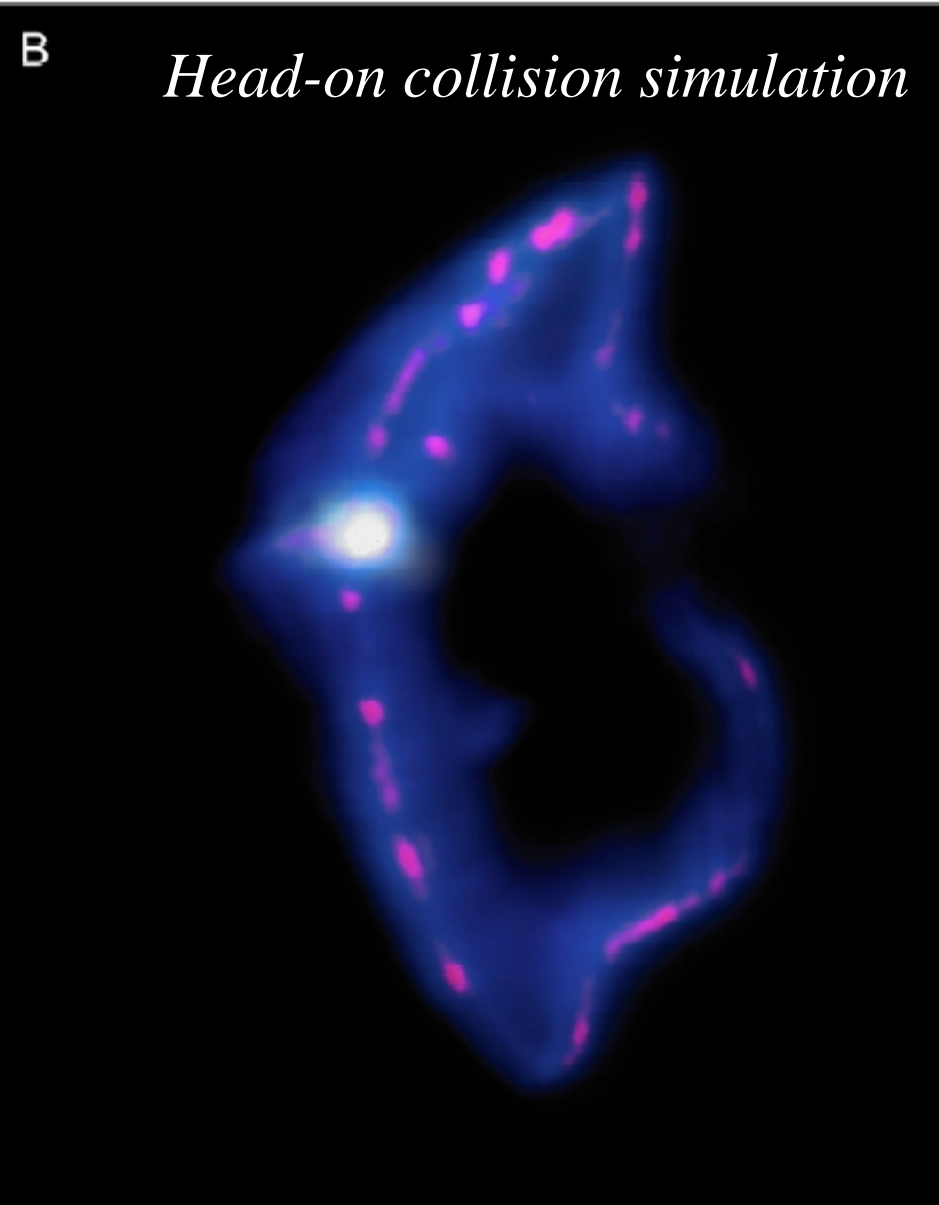
Formation of Tidal Dwarf Galaxies

Exchange of AM is within the disk: ➔ much easier with MOND to form TDG

In DM, requires very extended DM distribution (Bournaud et al 03)

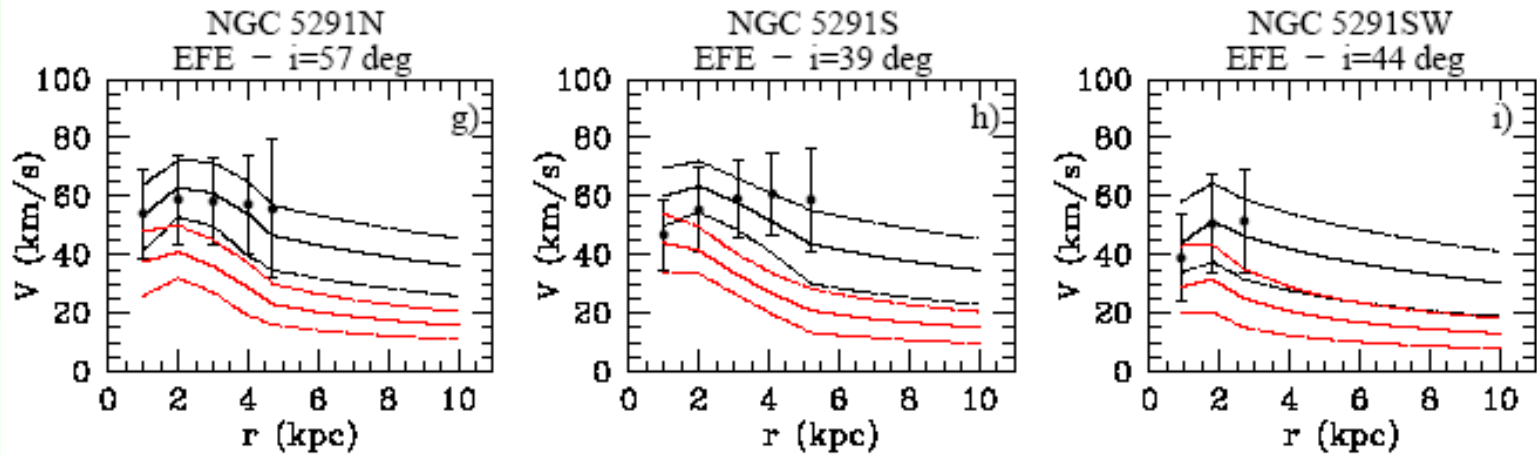


TDG in N5291 HI ring



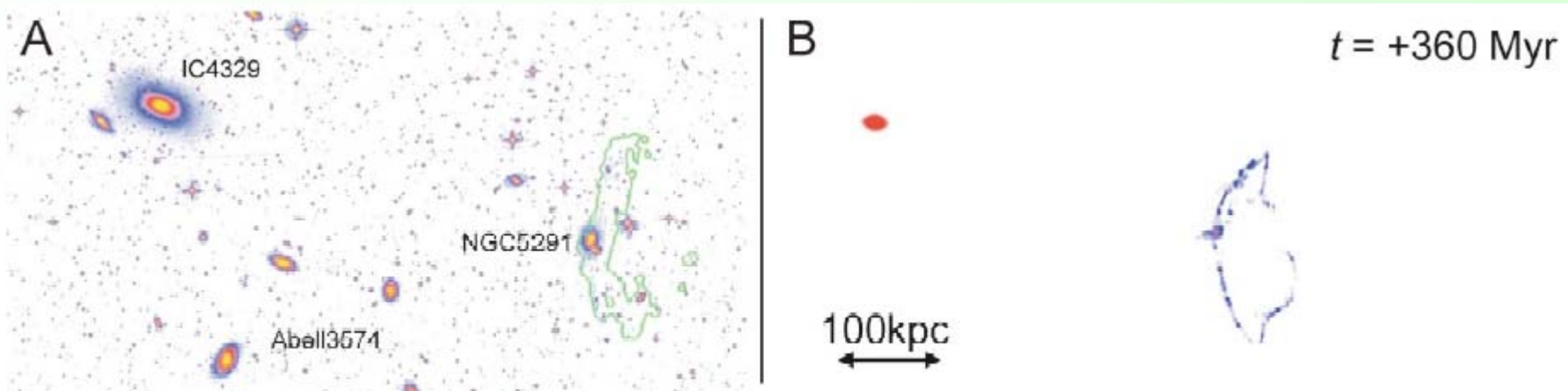
Bournaud et al 2007

Dynamics of the TDGs



With MOND, *Gentile et al 2007*

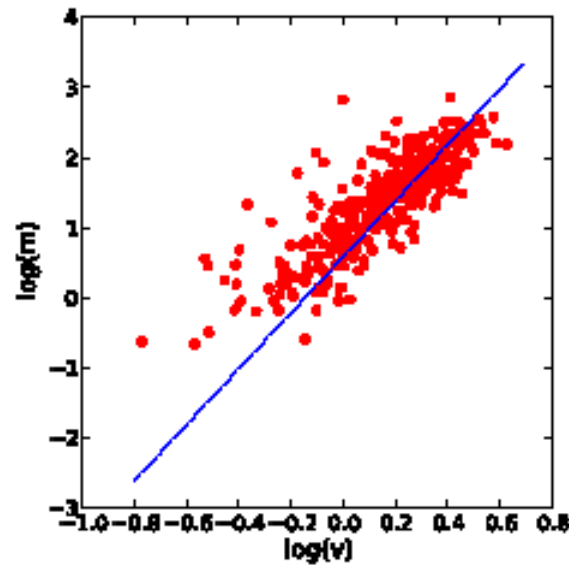
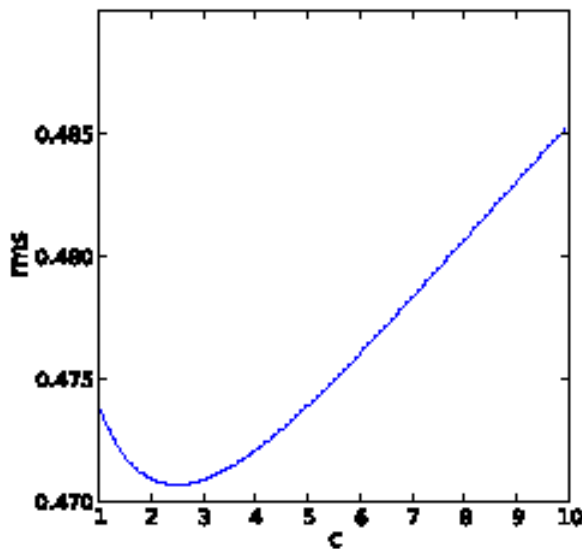
All inclinations = 45° , from simulations (Bournaud et al 07) \rightarrow dark H_2



MOND and the dark baryons

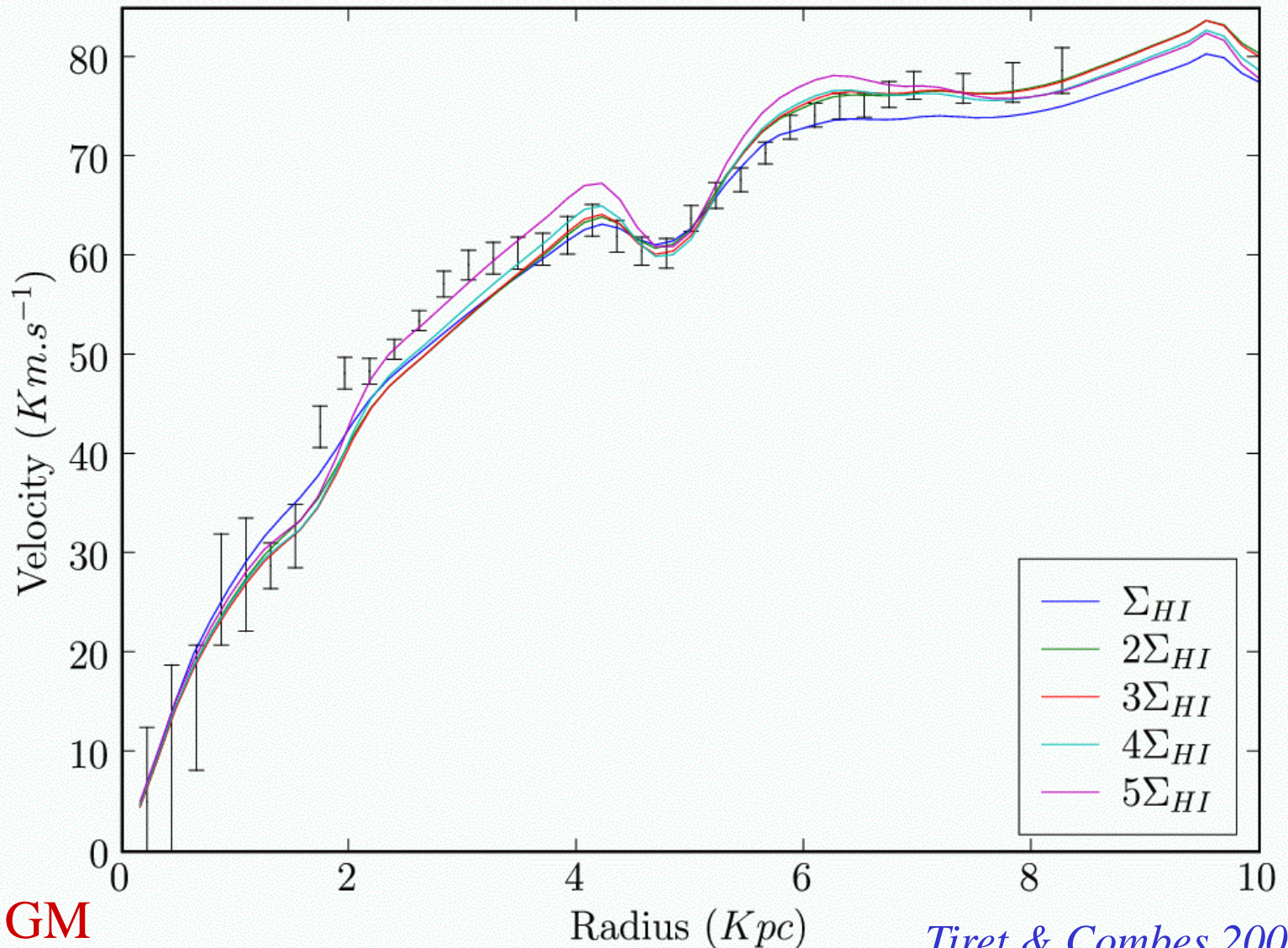
Is MOND compatible with the existence of dark gas in galaxies? What fraction provides the best fit to the rotation curves?

Fit of ~ 50 rotation curves, $c = M(\text{dark})/M_{\text{HI}}$



Combination with MOND

NGC 1560: fits with variation of $a_0 \sim 1/(\text{gas}/\text{HI})$



$$V^4 = a_0 \text{ GM}$$

Tiret & Combes 2008

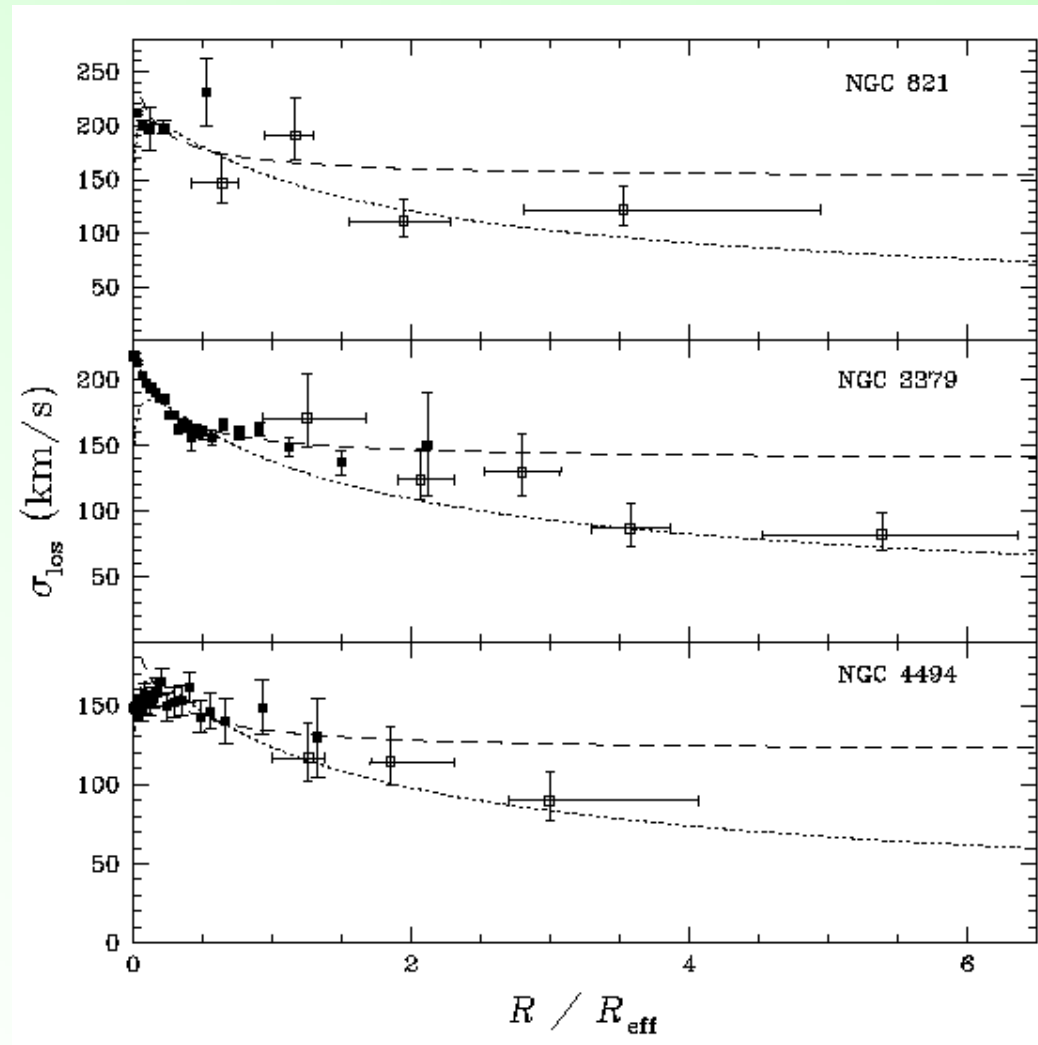
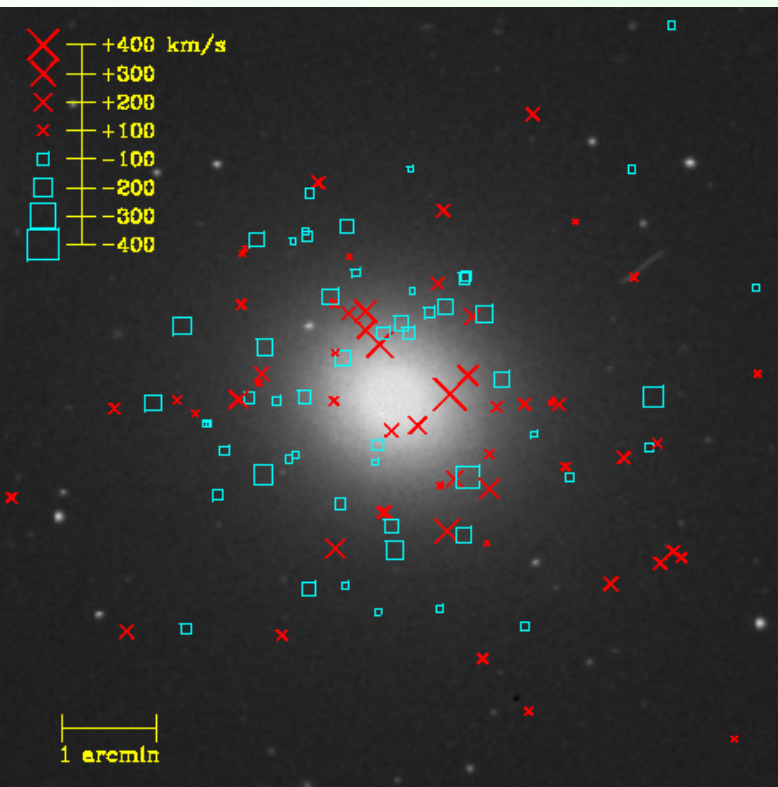
Dark matter in Ellipticals

Planetary Nebulae: Romanowsky et al 2003

Dearth of dark matter??

..... Visible matter (isotropic)

- - - isothermal (isotropic)

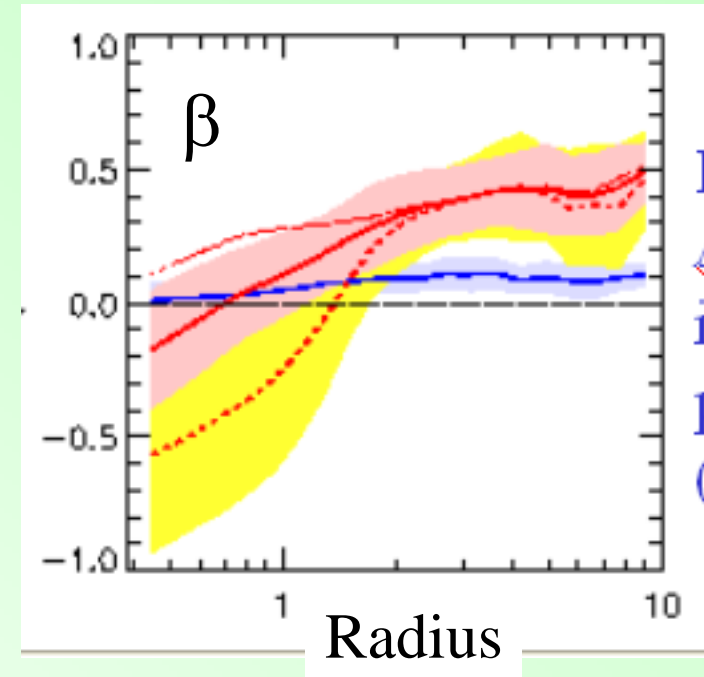


Anisotropy of velocities

$$\beta = 1 - \sigma_{\theta}^2 / \sigma_r^2, \quad -\infty, 0, 1$$

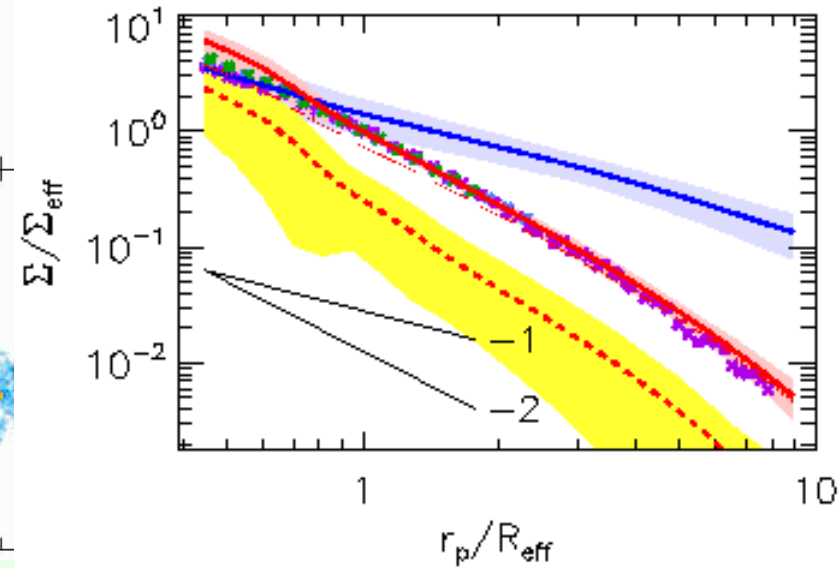
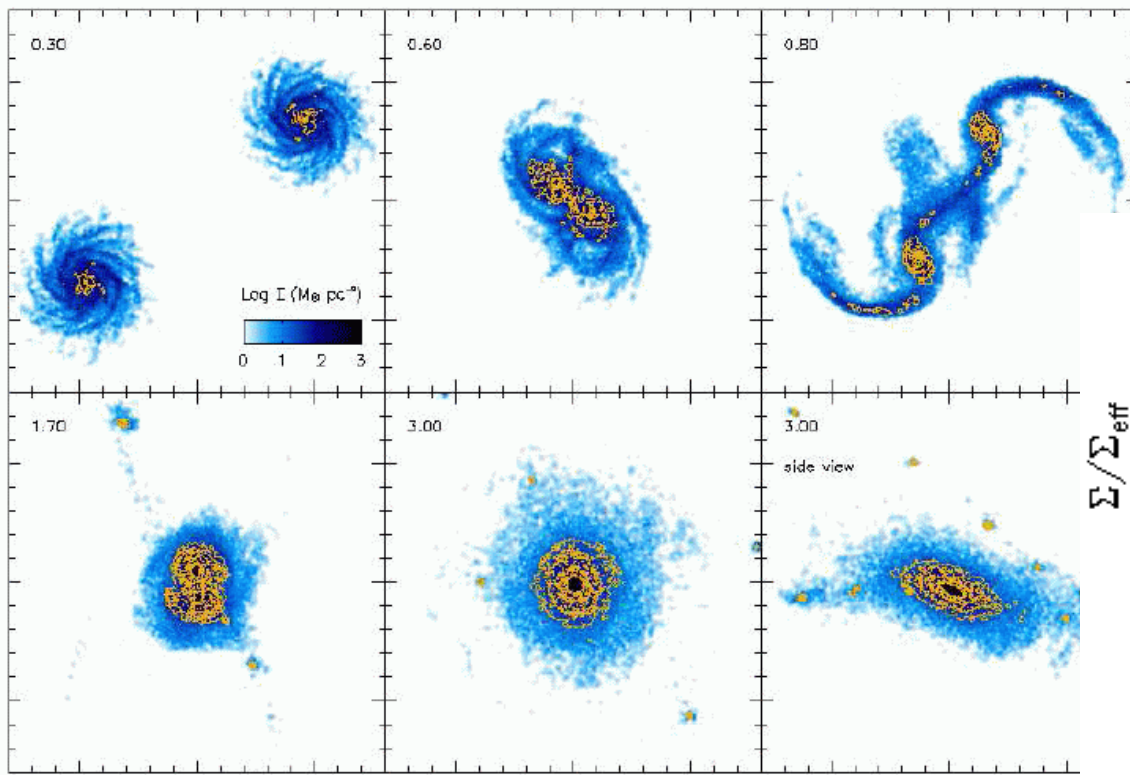
β circular, isotropic and radial orbits

When galaxy form by mergers,
orbits in the outer parts are
strongly radial, which could explain
the low projected dispersion
(Dekel et al 2005)

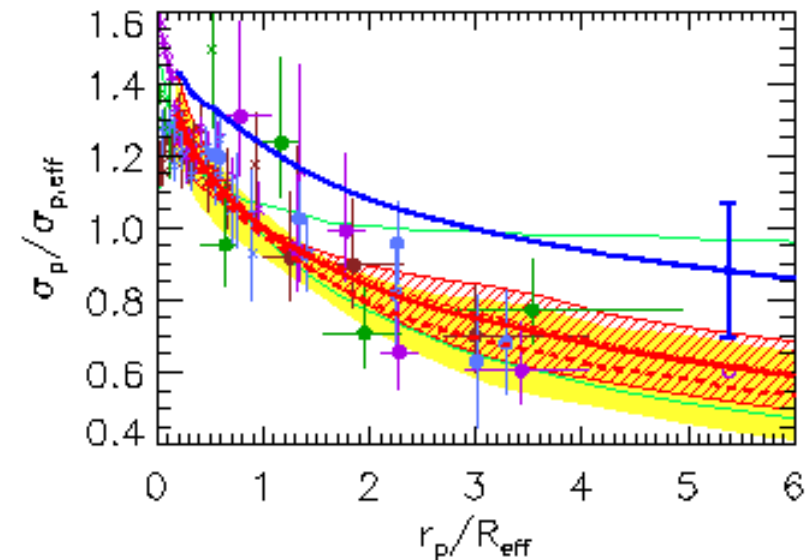


The observation of the velocity profile is somewhat degenerate
and cannot lead to the dark matter content univocally

Young stars are
in yellow contours



Comparison with data for
N821 (green), N3379(violet)
N4494 (brown), N4697 (blue)



DM profile from satellites

SDSS, 2500 deg², 3000 satellites $M_b = -16, -18$ (galaxies -14)

Removal of interlopers

$\sigma_v = 120 \text{ km/s}$ at 20kpc and 60km/s at 350kpc (Prada et al 2003)

→ Declines agree with $\rho \sim r^{-3}$ of NFW (CDM profile)

σ_v within 100kpc varies as $L^{0.3}$, quite close to TF relation

In average 2 satellites per galaxy, and 0.2 interlopers

See also McKay et al (2002) $\sigma \sim L^{0.5}$ from 1225 SDSS satellites
 M_{260} in agreement with lensing results

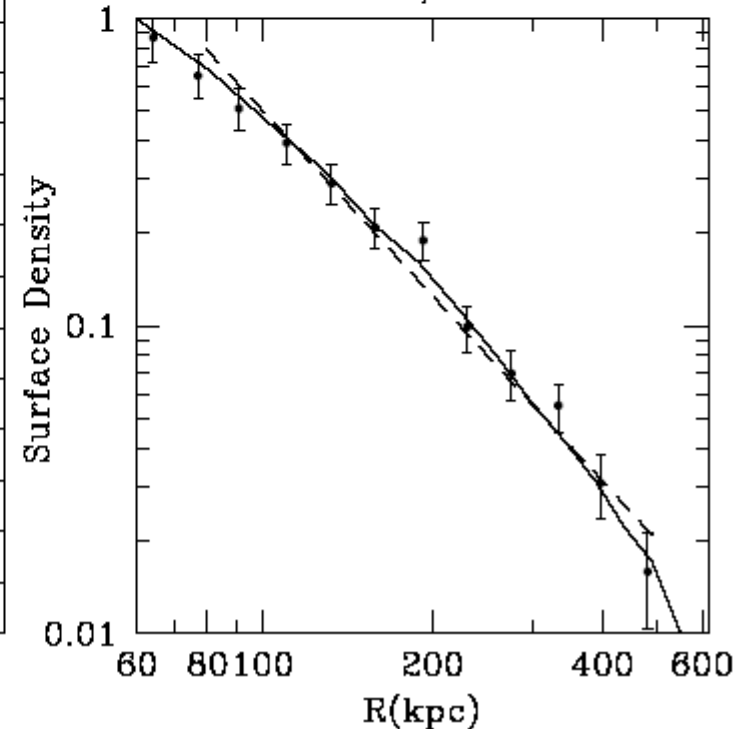
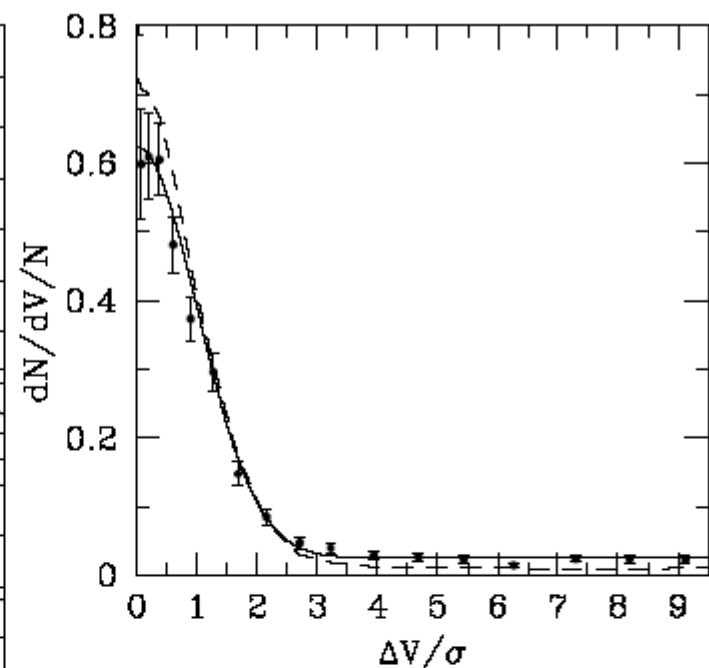
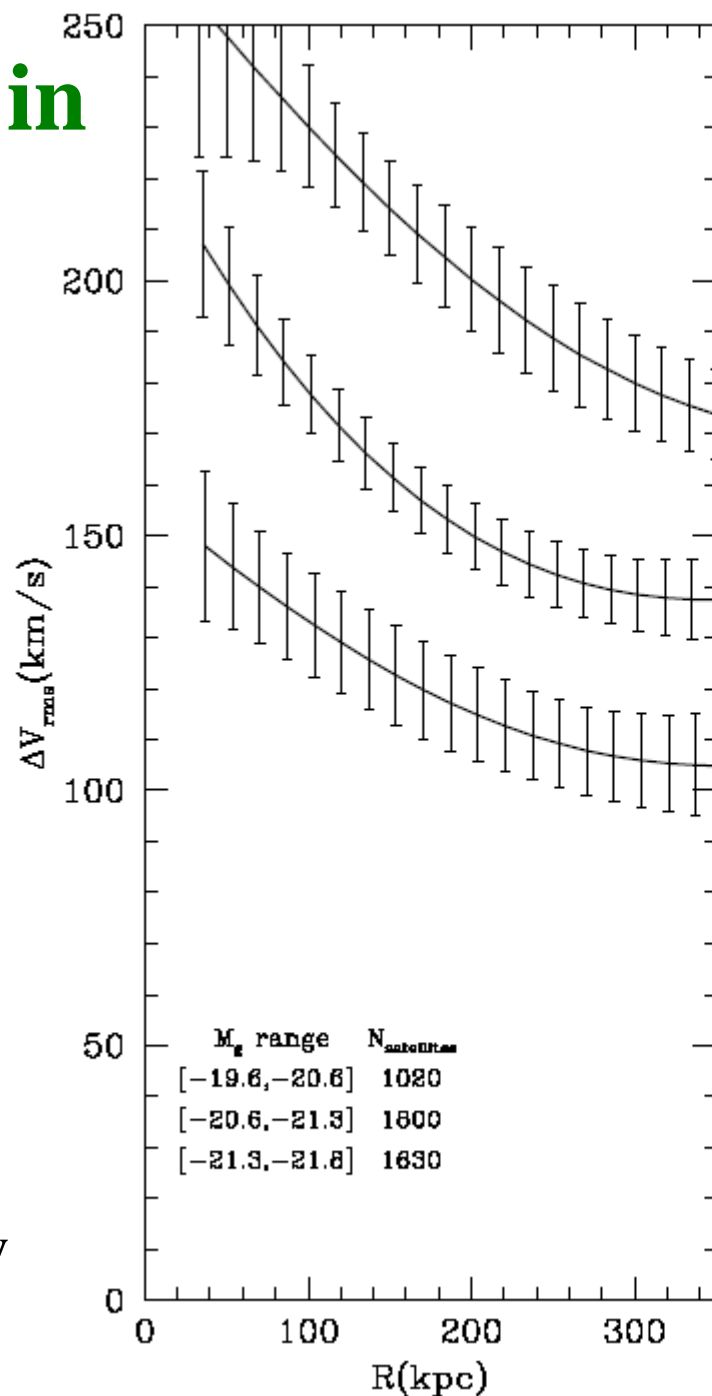
But flat velocity dispersion recovered (as if $\rho \sim r^{-2}$)

Satellites in SDSS

Klypin &
Prada 2009

Statistical
satellites

Only 1 or 0
for each galaxy

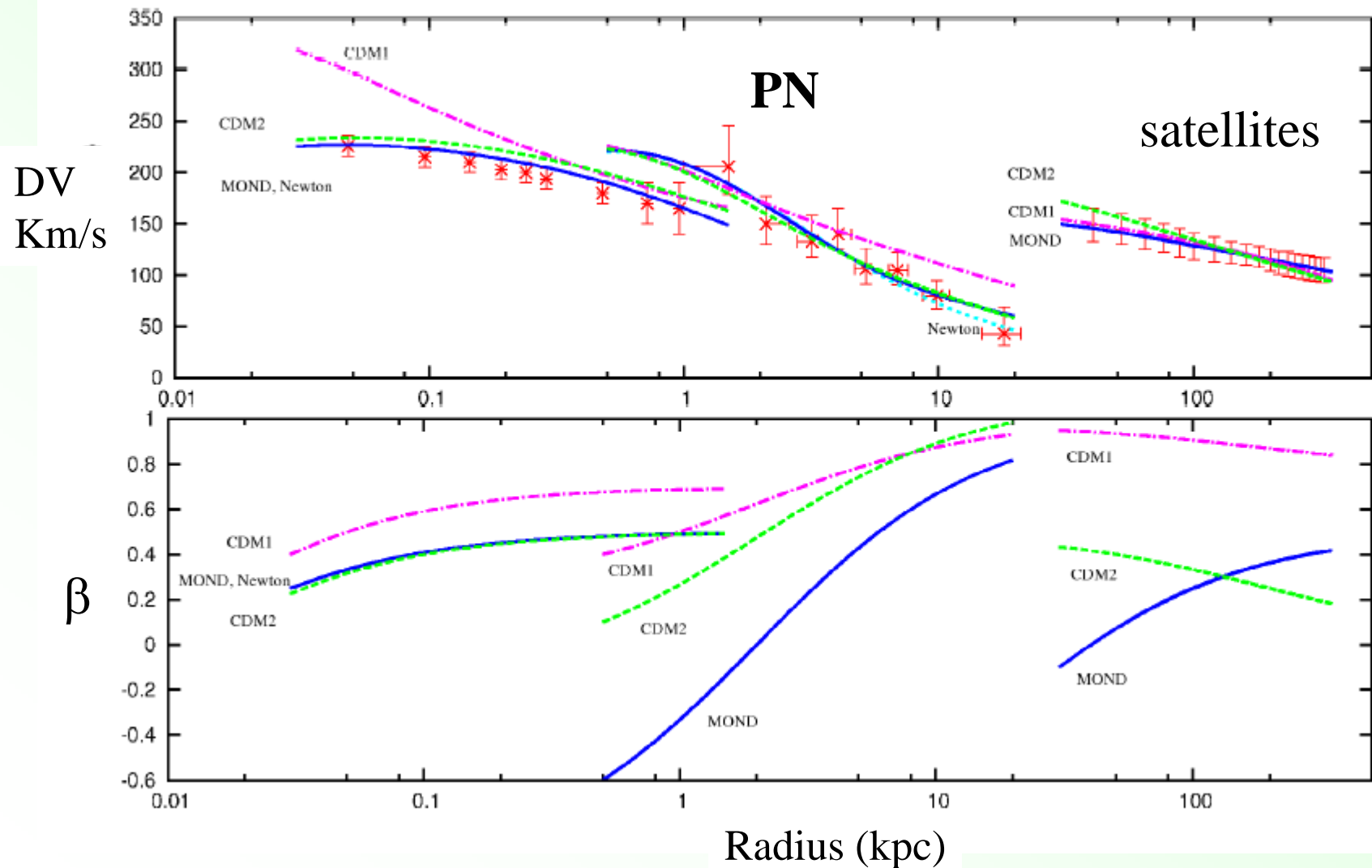


Test of the SDSS satellites

2 types of CDM **CDM1: NFW cusp**

CDM2: as required by rotation curves

Tiret et al 2007

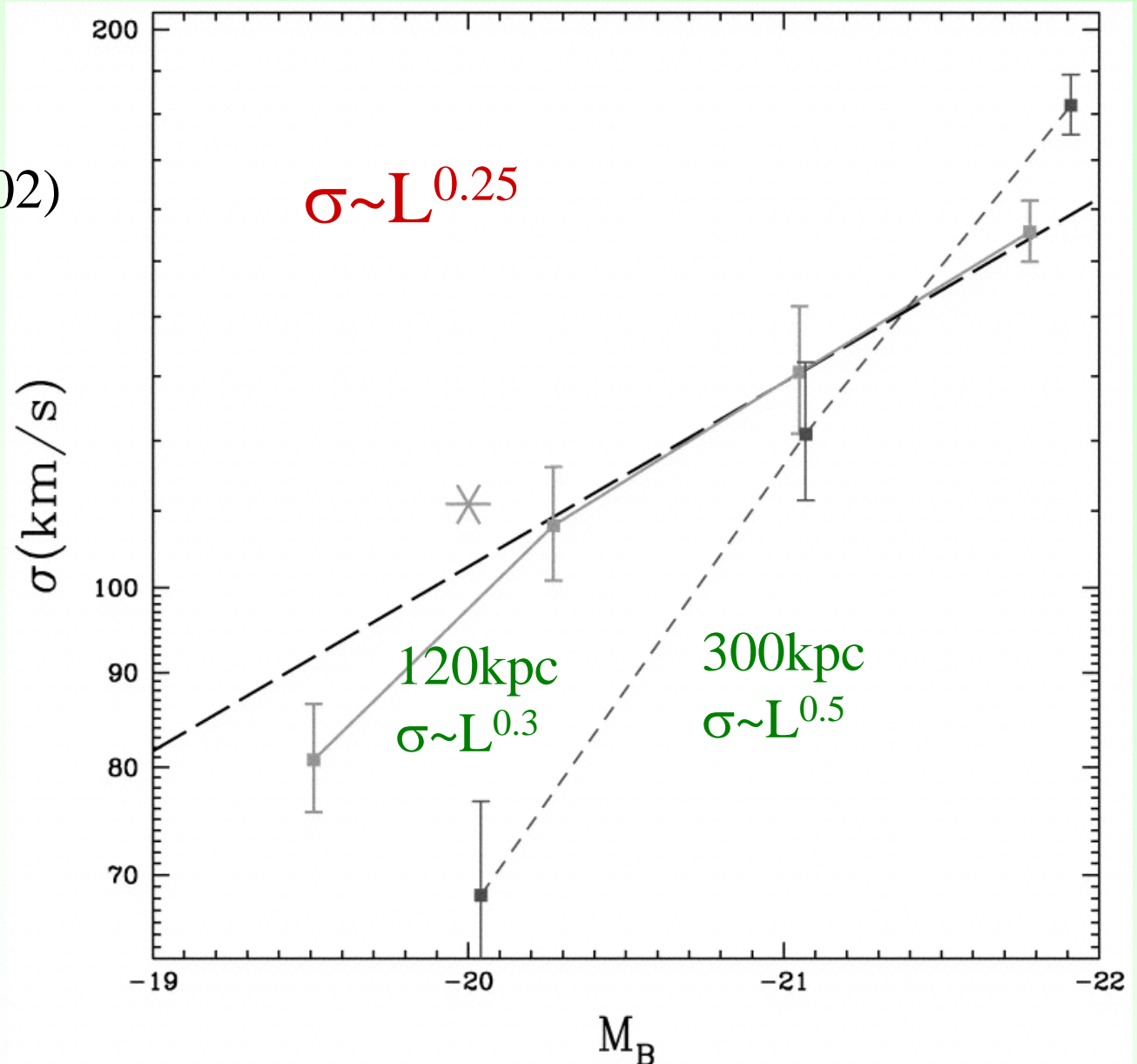


Tully Fisher Equivalent

Asterisk: Lenses
(Hoekstra et al 2002)

--- TF normal
spirals
(Verheijen 2001)

Prada et al (2003)



Large scale structure

In comoving coordinates: $\mathbf{r} = a \mathbf{x}$, $\mathbf{v} = da/dt \mathbf{x} + a \mathbf{u}$

$$\rightarrow \Delta\Phi = 4\pi G \delta\rho$$

$$\mu(g_M/\gamma) g_M = g_N + \mathbf{C} \quad \mathbf{C} = \text{rot}(\mathbf{h}) \quad \gamma \text{ critical acceleration } (=a_0)$$

Previous approximations $h=0$ (Nusser 2002, Knebe & Gibson 2004)

Newton and MOND accelerations are then parallel

Start from a cosmological Newton+ CDM \rightarrow then find MOND produces as much clustering ($\gamma = \text{cste}$)

$\delta \sim a^2$, instead of $\delta \sim a$ for Newton+ CDM

New code **AMIGA**, taking into account the curl (Llinares et al 2009)

Initial conditions from CMBFAST, displacements (Zeldovich approx)

128^3 grid, $32h^{-1}$ Mpc, *assuming Newtonian initial state*

\rightarrow For that critical acceleration γ varies with time

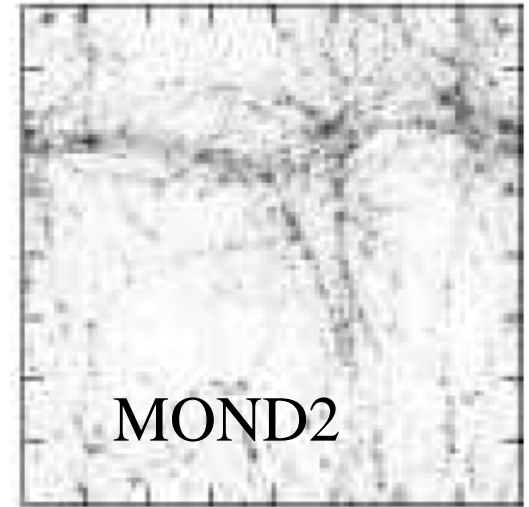
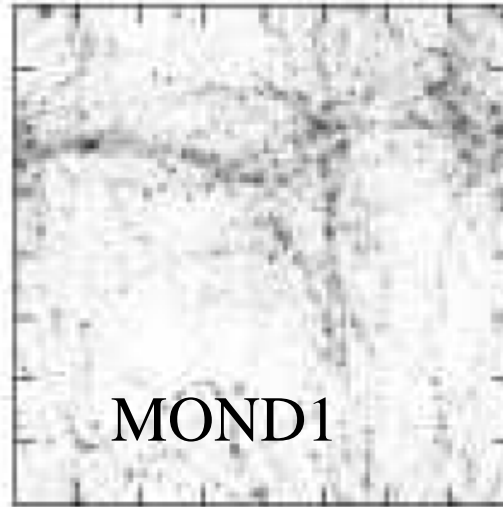
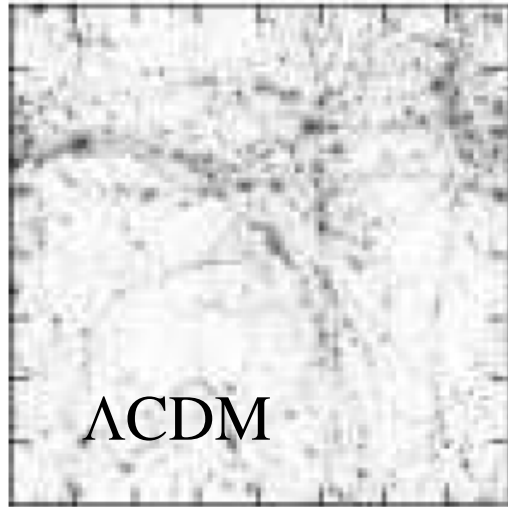
$$\gamma = a \gamma_0$$

MOND cosmological simulations

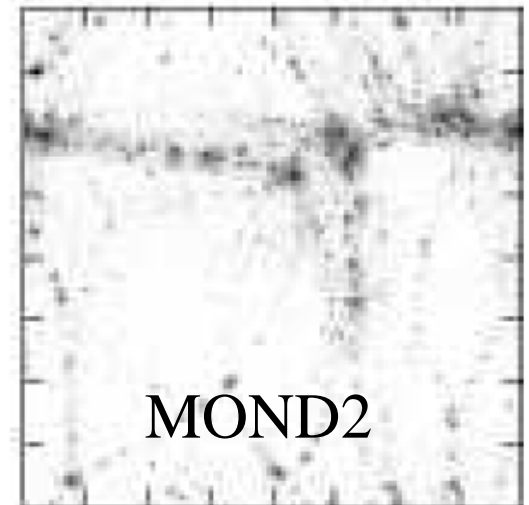
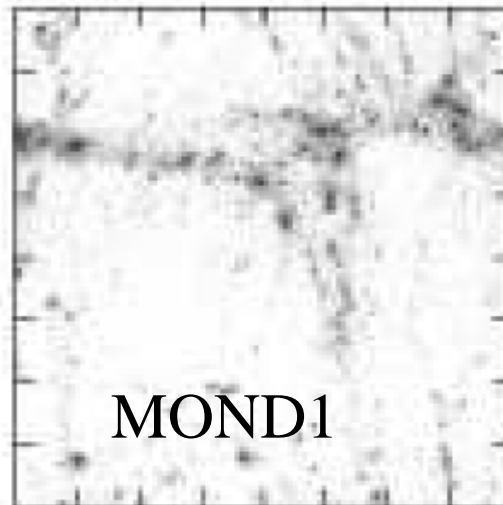
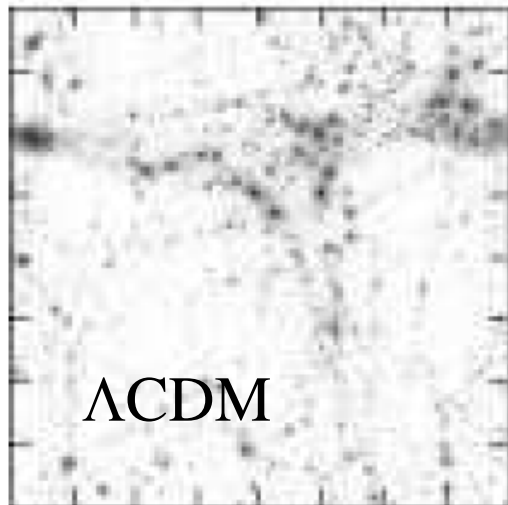
Starting $z=50$, dissipationless matter, 2 low Ω models + Λ CDM

Llinares et al 2009

$z=2$



$z=5$



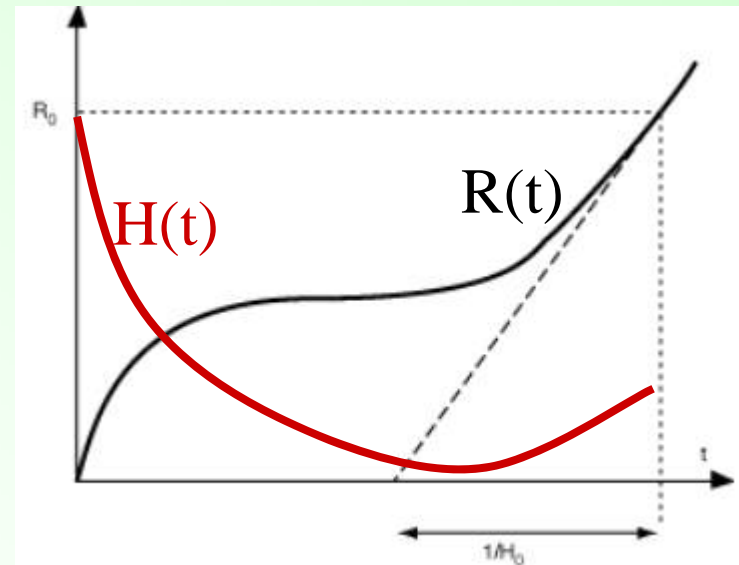
Evolution with time

Does the critical acceleration vary?

$$a_0 \sim c H_0, \text{ or also } a_0 \sim c (\Lambda/3)^{1/2}$$

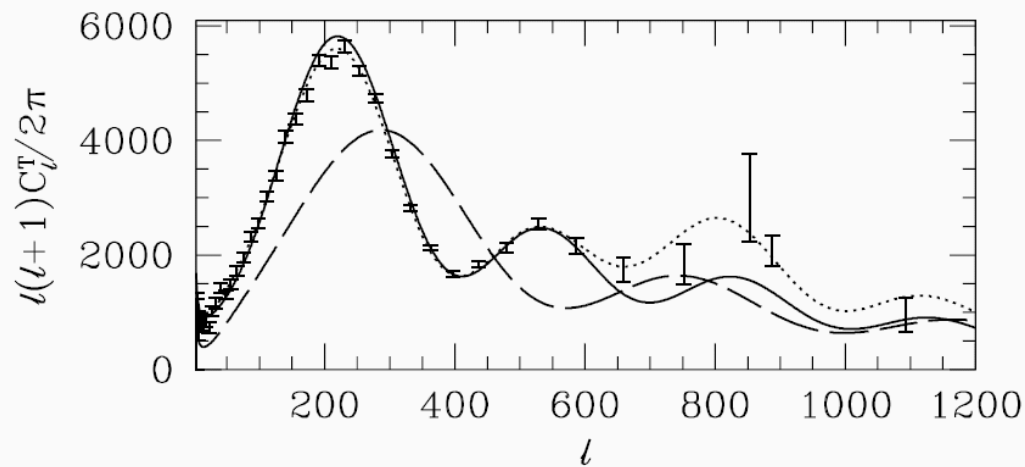
Possible to imagine variations, in either way (more or less MOND in the early universe)

Open question, as is the evolution of Ω_Λ



MOND: fit of CMB data, WMAP

Include massive neutrinos 1-2eV

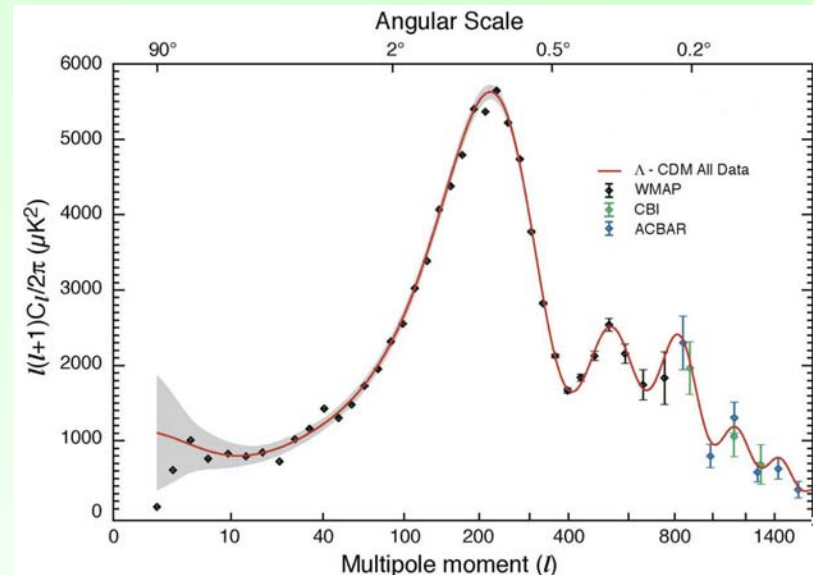


—: $\Omega_{\Lambda}=78\%$ $\Omega_{\nu}=17\%$ $\Omega_b=5\%$ MOND

-- : $\Omega_{\Lambda}=95\%$ $\Omega_b=5\%$

.....: Λ CDM

Fit with MOND
(no-DM) of
Acoustic peaks
(Skordis et al 2006)

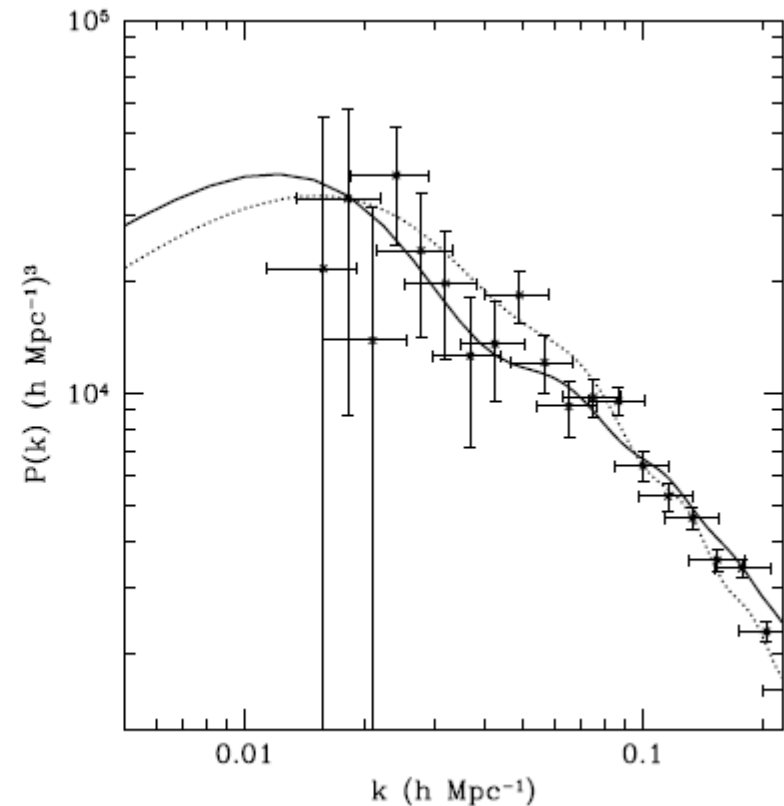
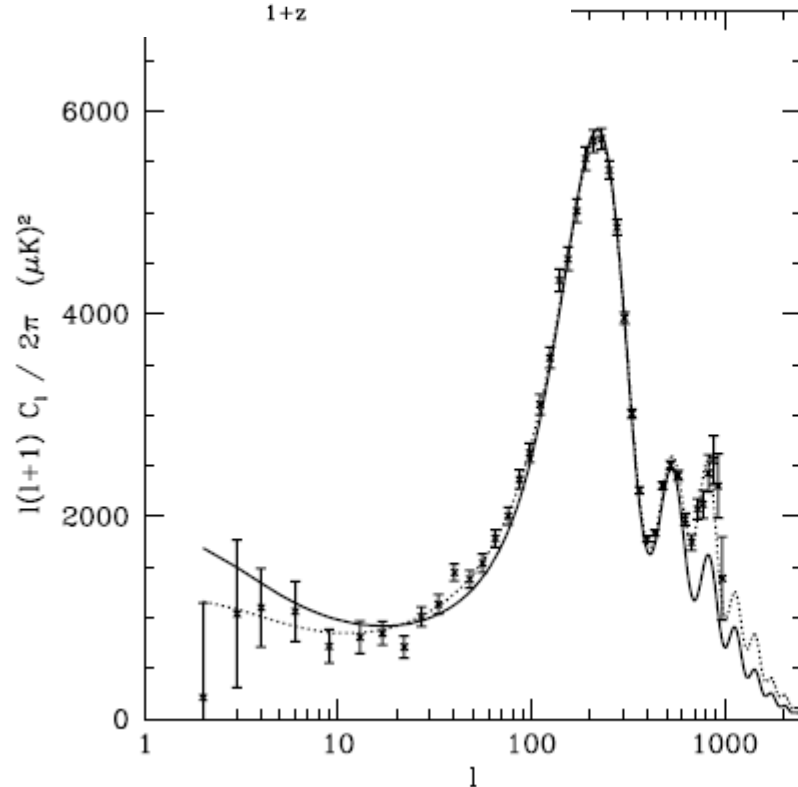
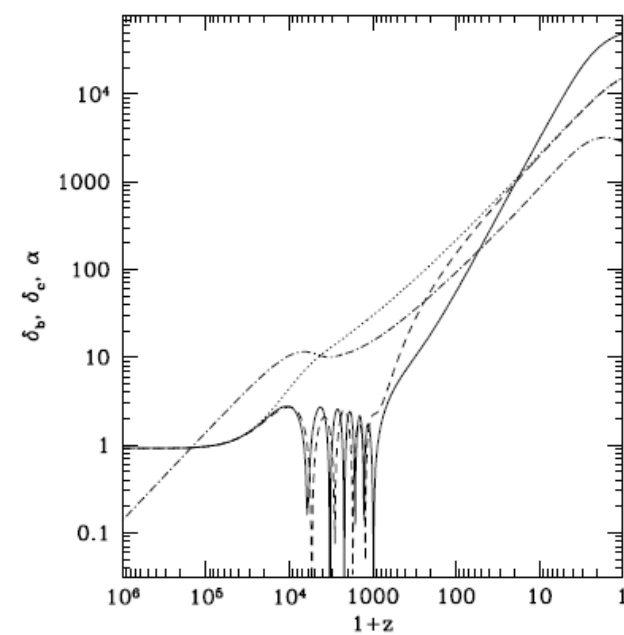


Fit with CDM + Λ

TeVS: CMB and LSS

Skordis 2009

Growth of structures due to the vector field
Scalar field \rightarrow acceleration of expansion, DE



Other possibilities

GEA: Generalized Einstein Ether theories

Zloznik et al 2006, Ferreira et al 2009

From TeVeS, suppression of one degree of freedom,
Suppress the scalar field, in combining with the Vector Field
Which is now no longer unit timelike (but timelike)

Physical metric (no longer Einstein-frame metric)

→ Retrieve the MOND phenomenology
Vector field sourcing potential wells

Many other possibilities to explore

Conclusion: Success and Problems

CDM: great success at large scale, but problems at galaxy scales
MOND solves the problems of galaxies,
but has to solve its own problem at group and cluster scales
(neutrinos, baryons..)

- Observational tests could constrain the various MOND models
- Lorentz covariant theory, TeVeS (Bekenstein 2004)
- Different metric, some free parameters still
[$a_0 \sim c H_0$ today, but does it vary with time?]

Numerous other propositions: Einstein Aether (scalar field),
Vector field, etc..

Tests of General Relativity

- Detection through weak lensing of deviation from GR at cosmic scales *Rachel Bean (2009)*

- ISW (*Integrated Sachs-Wolfe effect*) WMAP

Correlated with 2MASS and SDSS

With COSMOS HST deep field, and weak lensing

Cosmological constant, or quintessence?

Modified gravity: $f(R)$, DGP (Dvali-Gabadadze-Poratti)-branes, TeVeS, Yukawa models, etc..

Not only acceleration of expansion, but effect on LSS growth
Could raise the degeneracy

First detection $\eta < 1$?

$$ds^2 = -a^2(\tau) \{ d\tau^2 [1 + 2\psi(\mathbf{x}, \tau)] + d\mathbf{x}^2 [1 - 2\phi(\mathbf{x}, t)] \}$$

Where ψ and ϕ are the two newtonian potentials for the temporal and spatial perturbations of the metric resp.

$$\eta(k, a) \equiv \frac{\phi(k, a)}{\psi(k, a)}$$

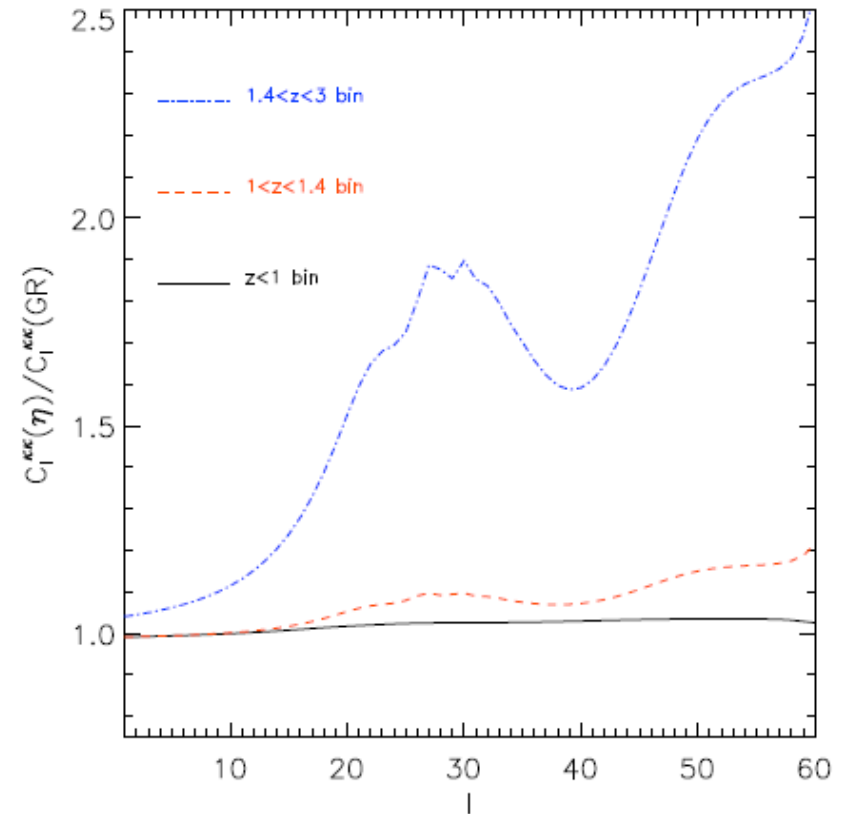
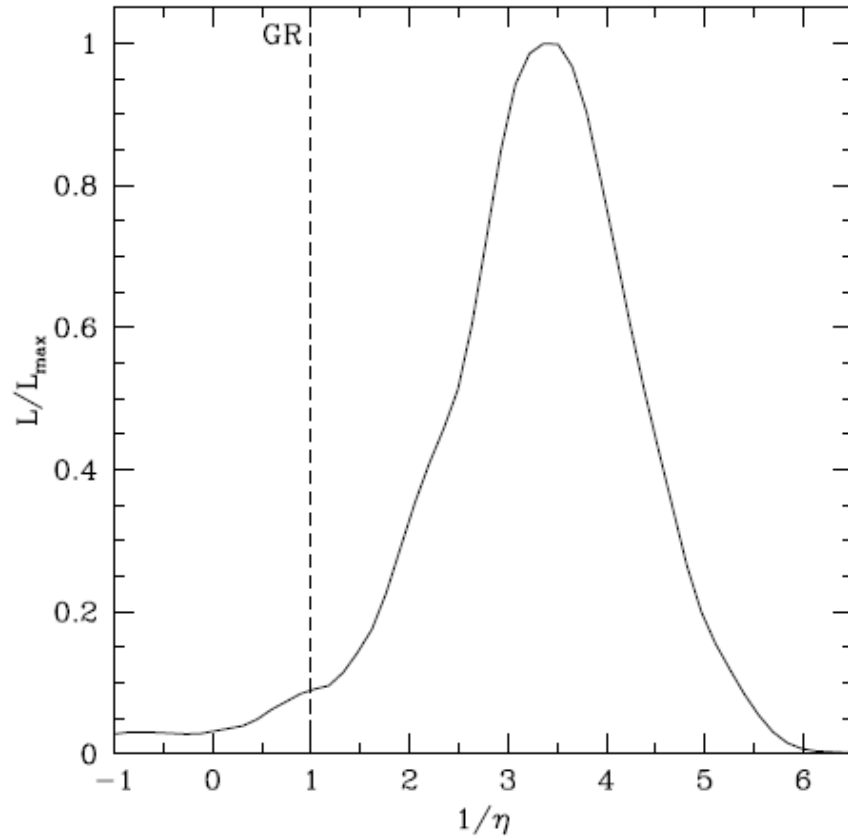
$$\gamma(k, a) \equiv \frac{\ln(\dot{\delta}_c / \mathcal{H} \delta_c)}{\ln \Omega_m(a)}$$

$\eta = 1$, if GR is verified even if γ the growth rate can be modified

Analysis of all data, BAO, CMB, Union SNIa, Cosmos, WL..
And ISW from WMAP and surveys (2MASS, SDSS)

→ GR disfavored at 98% level

Evidence of deviation from GR



COSMOS WL brings evidence that DE is a modification of GR
More than a cosmological constant (Bean 2009)
To be confirmed with DES, LSST, etc..