

# Positive evidence for Primordial Black Holes

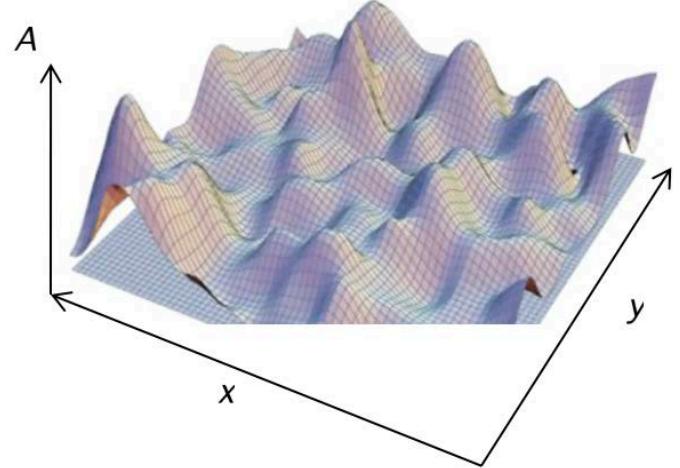
Zooming in on PBH, 4<sup>th</sup> March 2024

Juan García-Bellido  
IFT-UAM/CSIC

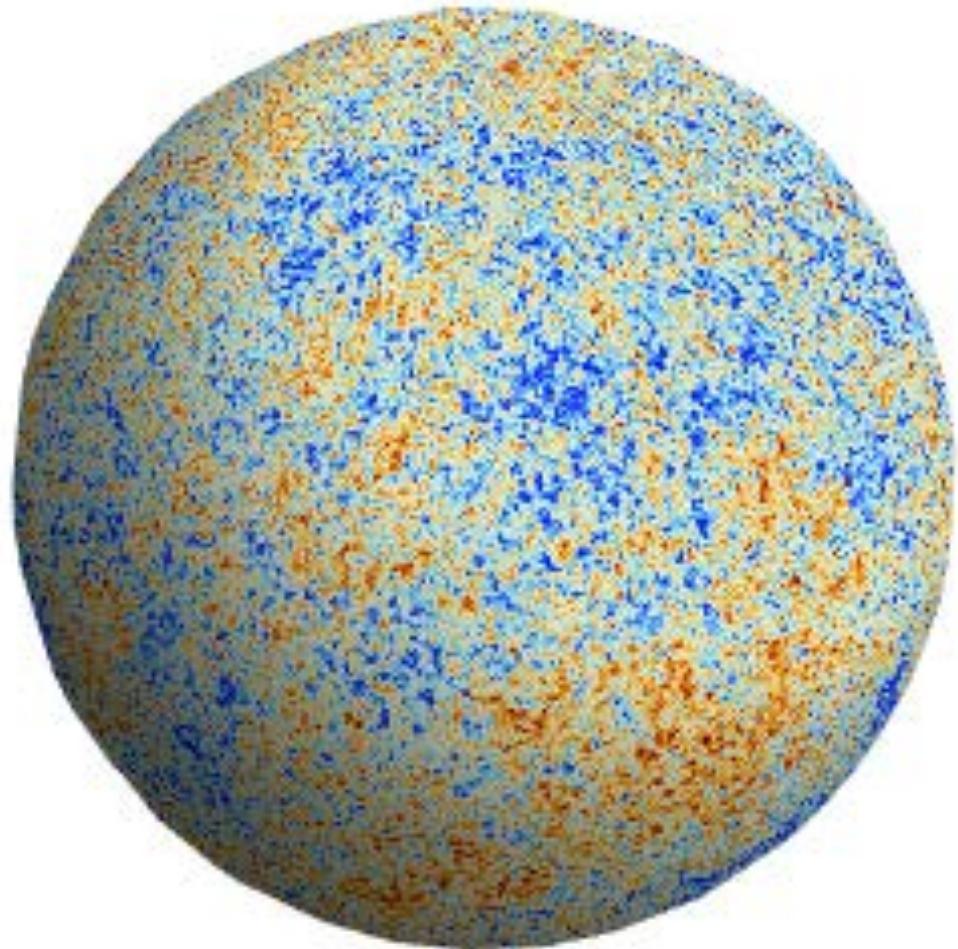
# Outline

- **Theory:**
  - **Critical Higgs Inflation**
  - **Quantum Diffusion**
- **Observational Evidences:**
  - **Gravitational Lensing**
  - **Gravitational Waves**

# Inflation

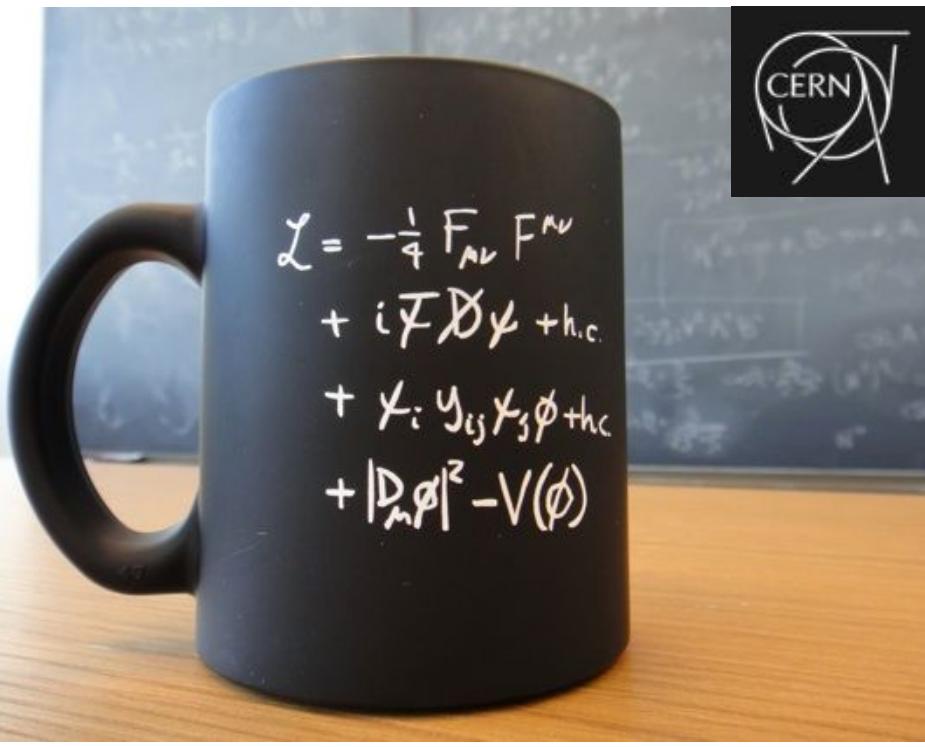


Quantum Fluctuations =  
Space-Time Ripples



Stretched to cosmological scales

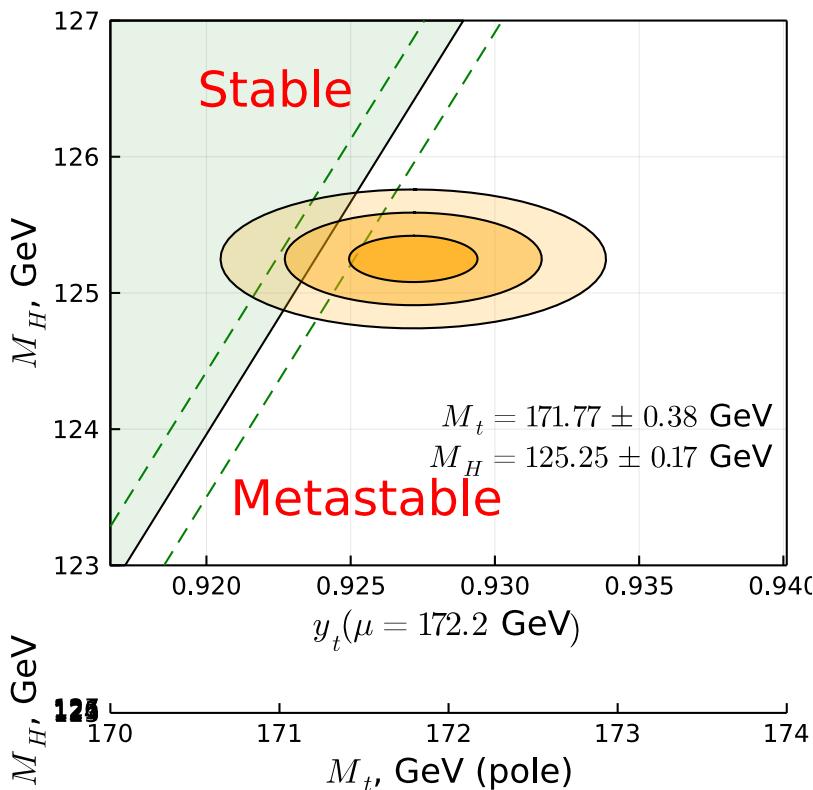
# Standard Model Lagrangian



$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \not{D} \psi + h.c. \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + |\nabla_\mu \phi|^2 - V(\phi) \\ & + \cancel{\Im | \phi |^2 R} \end{aligned}$$
The term  $\Im | \phi |^2 R$  is circled in red.

$$R = 12H^2 + 6\dot{H} \rightarrow R_0 = 9.2 H_0^2 \rightarrow m_H = \sqrt{\xi R_0} = 2 \times 10^{-32} \text{ eV}$$

# EW vacuum metastability



$$m_t^{\text{pole}} = 170.5 \pm 0.8 \text{ GeV}$$

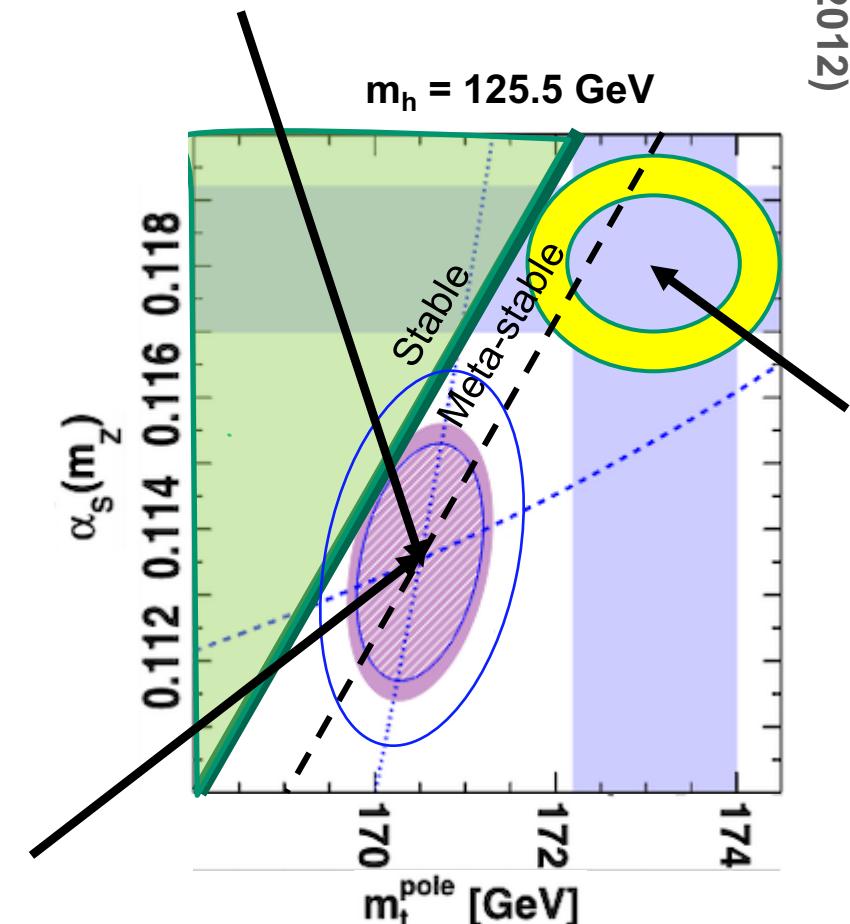
$$\alpha_S(m_Z) = 0.1135^{+0.0021}_{-0.0017}$$

LHC-CMS Collab. (2020)

<https://arxiv.org/abs/1904.05237>

Buttazzo et al.  
(2012)

<https://arxiv.org/pdf/1112.3022.pdf>



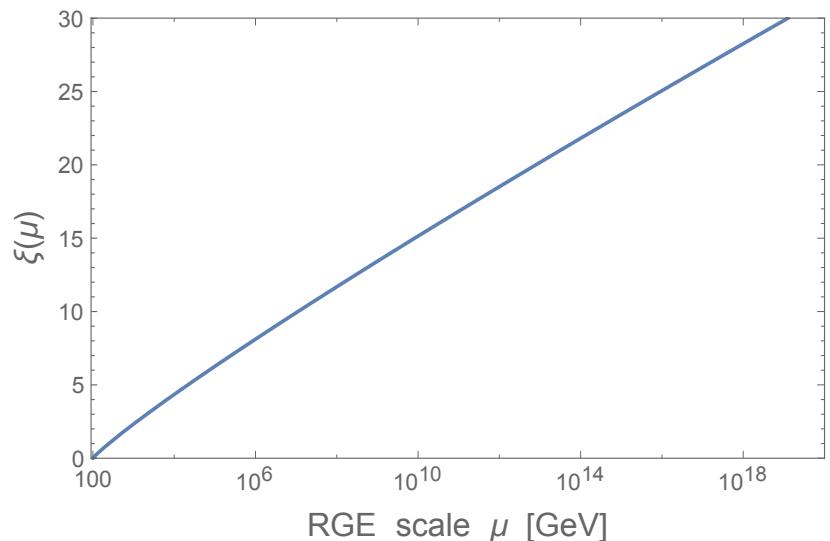
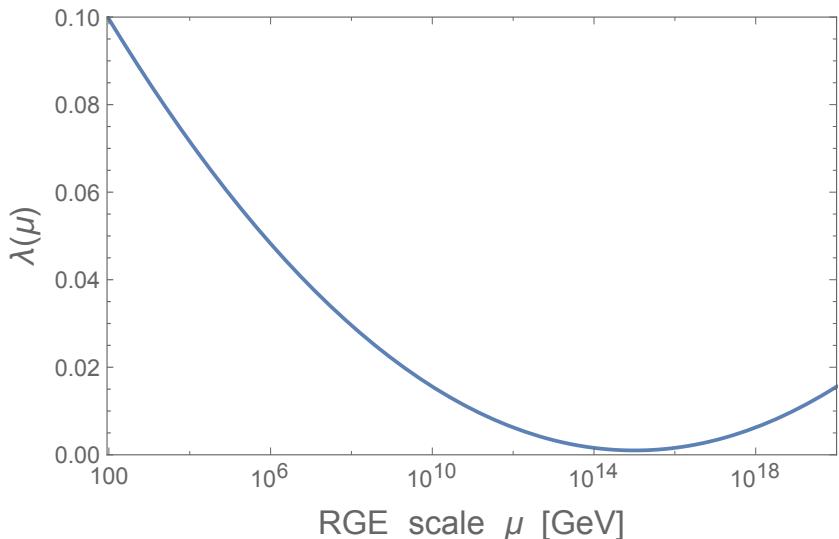
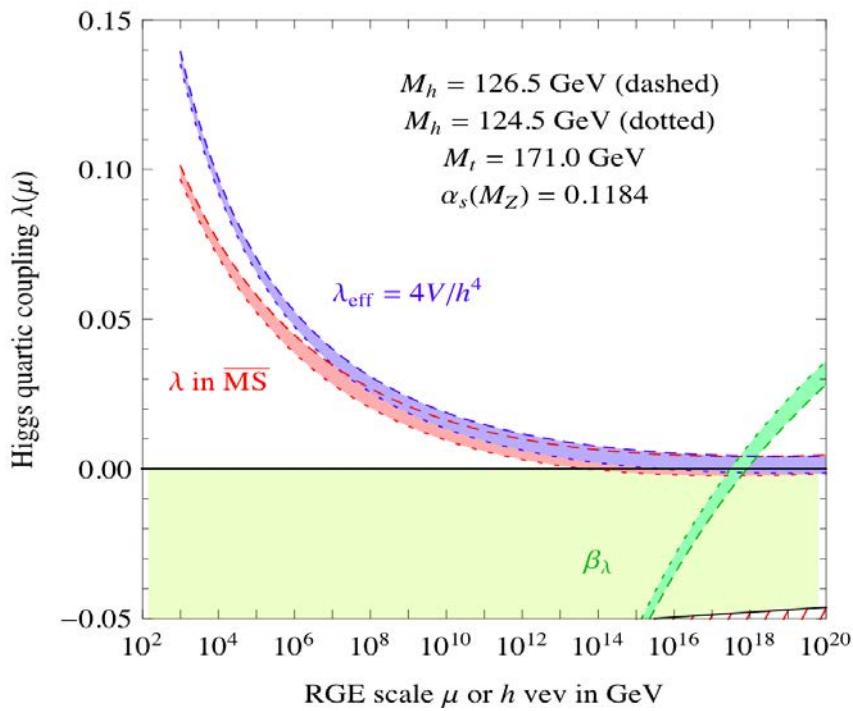
# Renormalization of Higgs couplings

Ezquiaga, JGB, Ruiz [1705.04861]

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu),$$

$$\xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu),$$

Buttazzo et al (2014)



# Critical Higgs Inflation

Ezquiaga, JGB, Ruiz Morales [1705.04861]

$$S = \int d^4x \sqrt{g} \left[ \left( \frac{1}{2\kappa^2} + \frac{\xi(\phi)}{2} \phi^2 \right) R - \frac{1}{2} (\partial\phi)^2 - \frac{1}{4} \lambda(\phi) \phi^4 \right]$$

$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu) ,$$

$$\xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu) ,$$

$$\frac{d\varphi}{d\phi} = \frac{\sqrt{1 + \xi(\phi) \phi^2 + 6 \phi^2 (\xi(\phi) + \phi \xi'(\phi)/2)^2}}{1 + \xi(\phi) \phi^2}$$

---

$$V(x) = \frac{V_0 (1 + a \ln^2 x) x^4}{(1 + c (1 + b \ln x) x^2)^2} \quad x = \phi/\mu$$

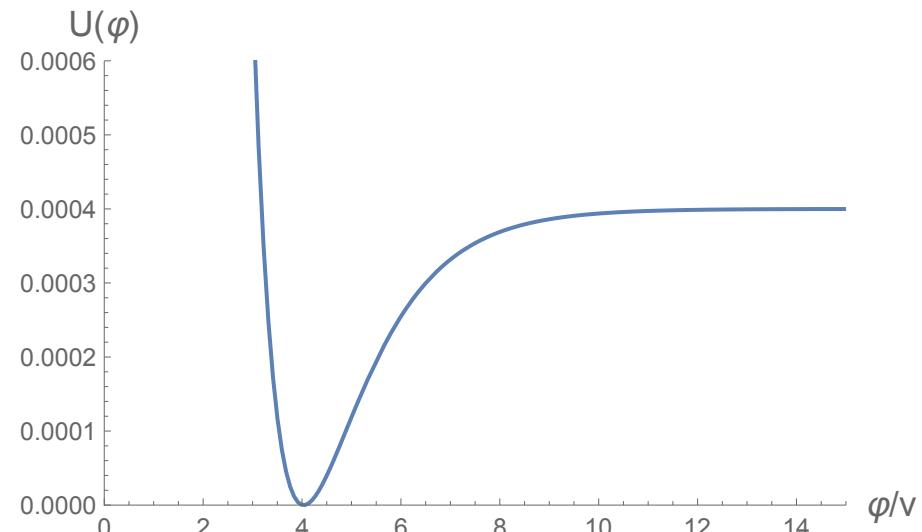
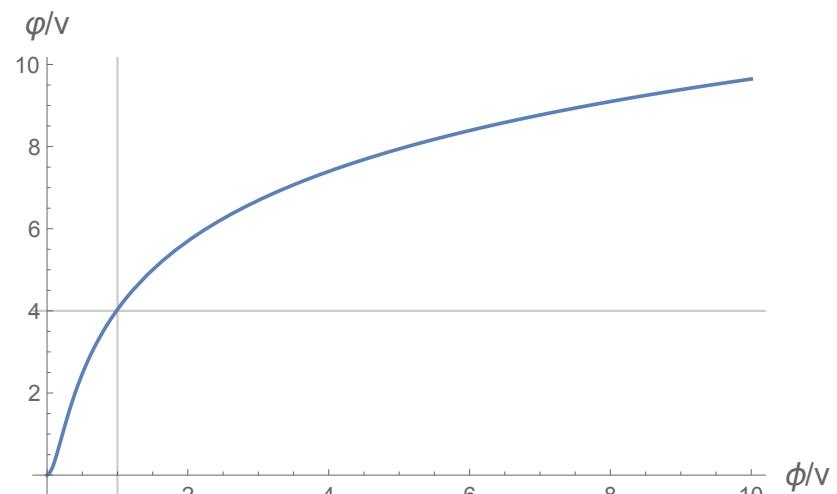
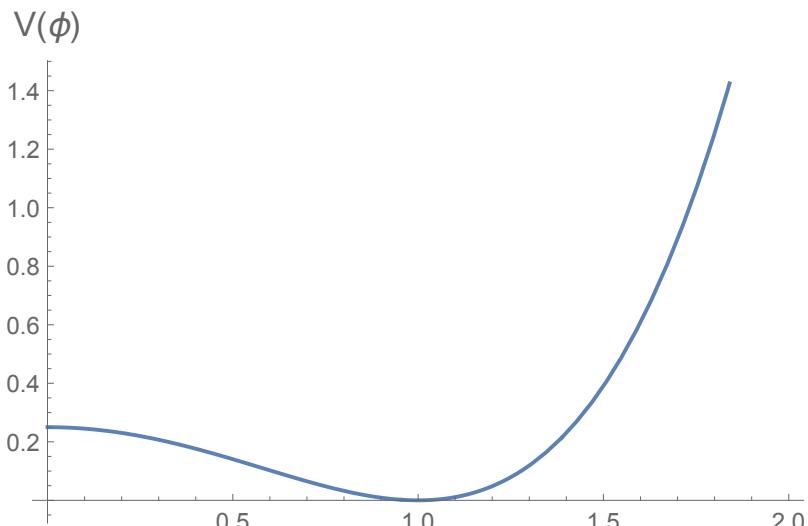
$$V_0 = \lambda_0 \mu^4 / 4, a = b_\lambda / \lambda_0, b = b_\xi / \xi_0 \text{ and } c = \xi_0 \kappa^2 \mu^2$$

# Conformal redefinition of metric and Higgs

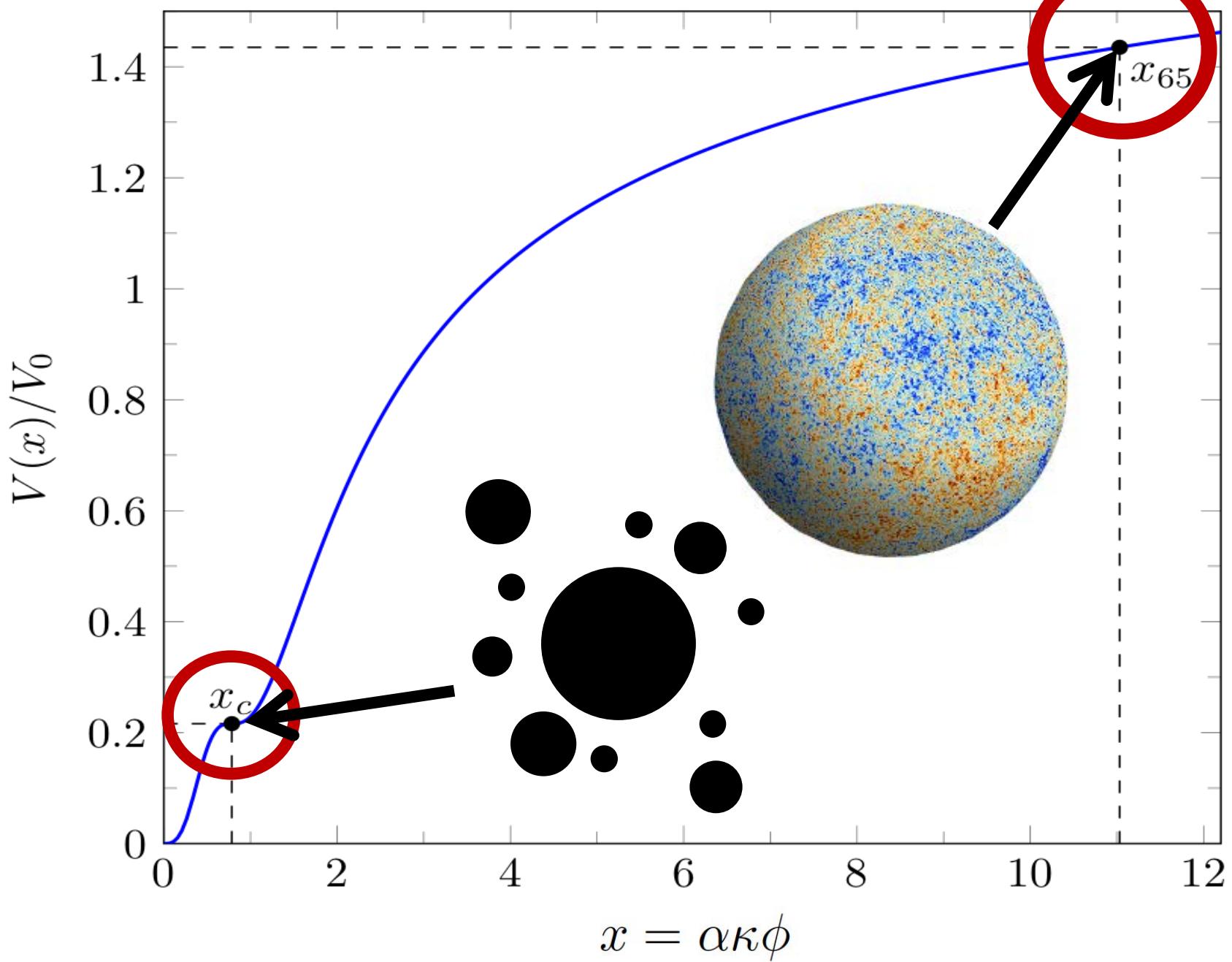
$$g_{\mu\nu} \rightarrow h_{\mu\nu} = (1 + \xi\phi^2)g_{\mu\nu}$$

$$\phi \rightarrow \varphi = \int \frac{\sqrt{1 + \xi(1 + 6\xi)\phi^2}}{1 + \xi\phi^2} d\phi$$

$$V(\phi) \rightarrow U(\varphi) = \frac{V(\phi)}{1 + \xi\phi^2}$$

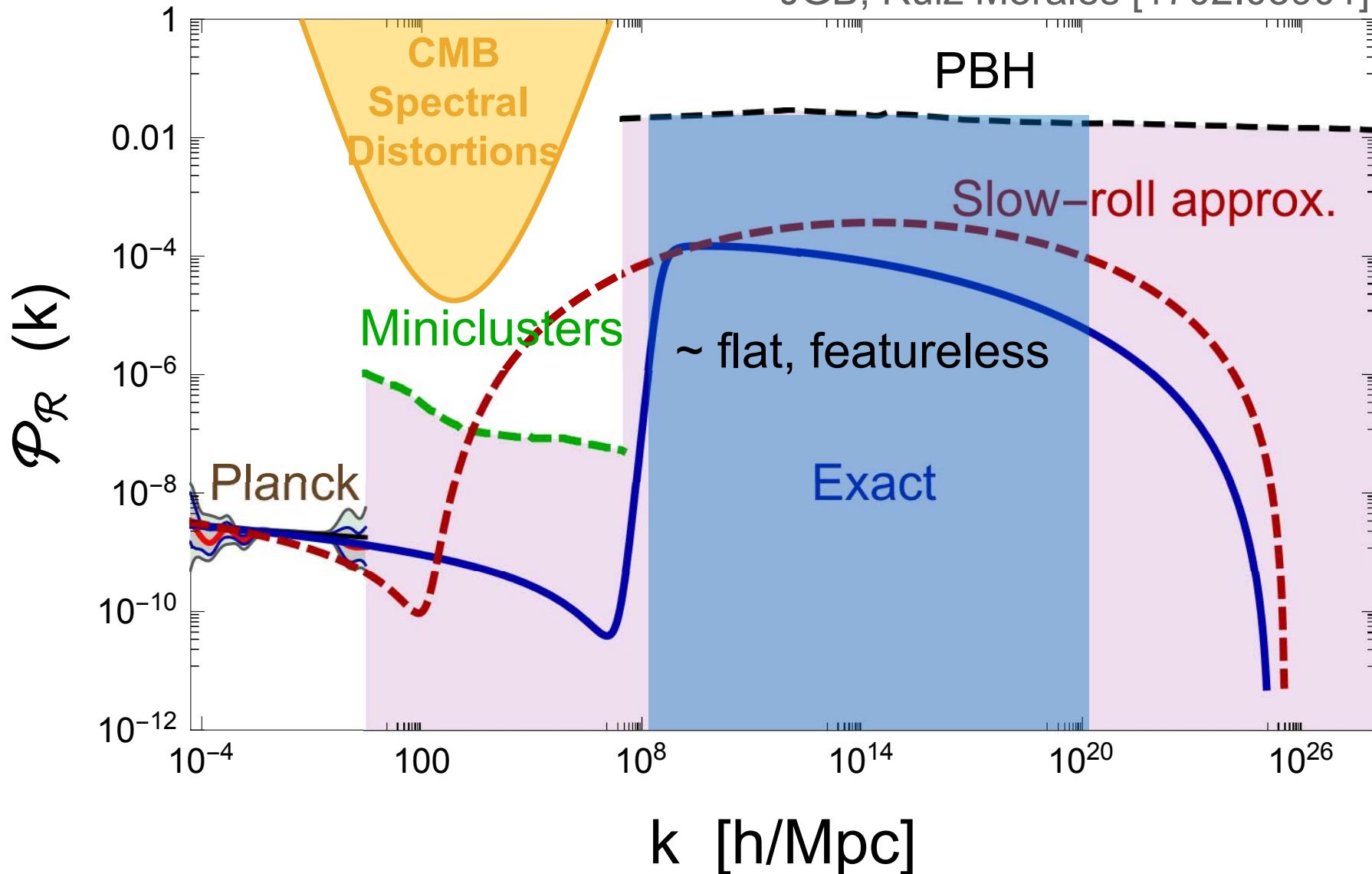


# JGB, Ruiz Morales [1702.03901]



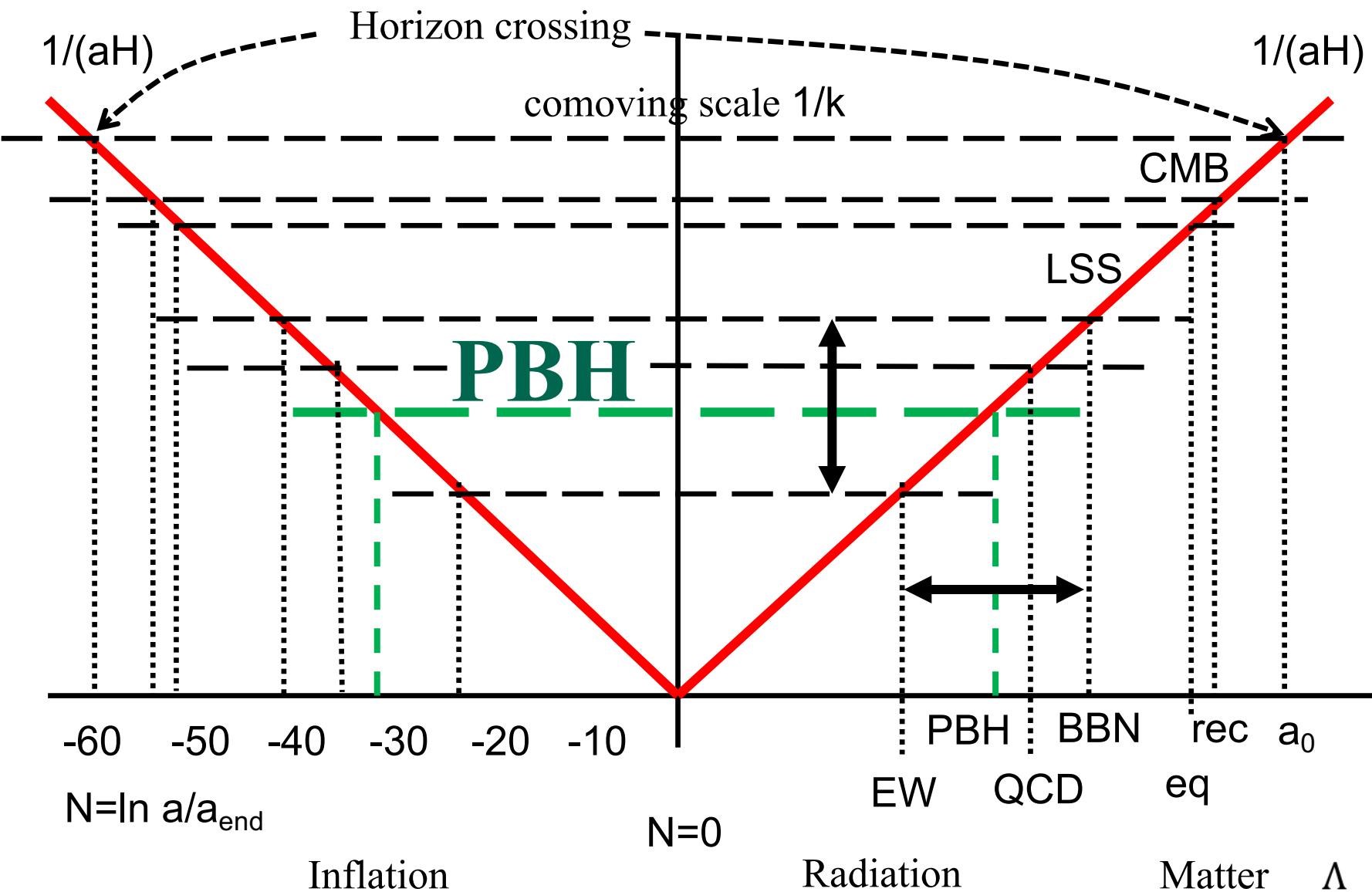
# Primordial Power Spectrum

JGB, Ruiz Morales [1702.03901]

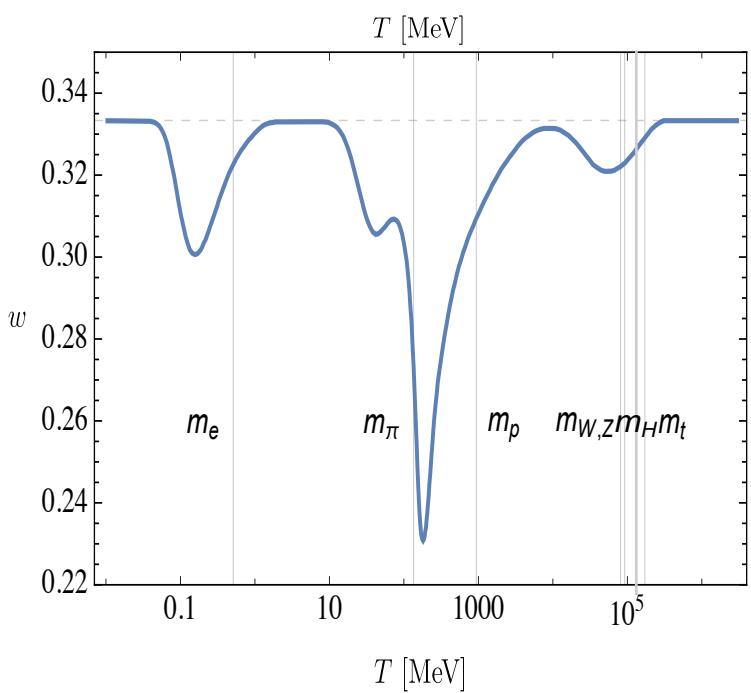
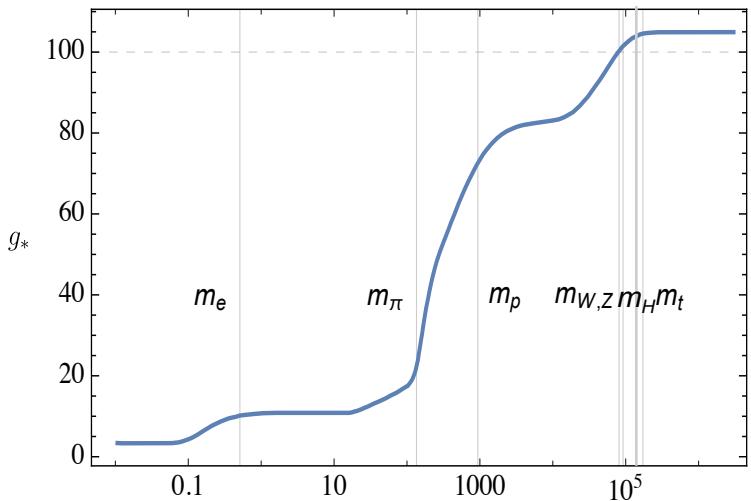


# Inflation

JGB [1702.08275]

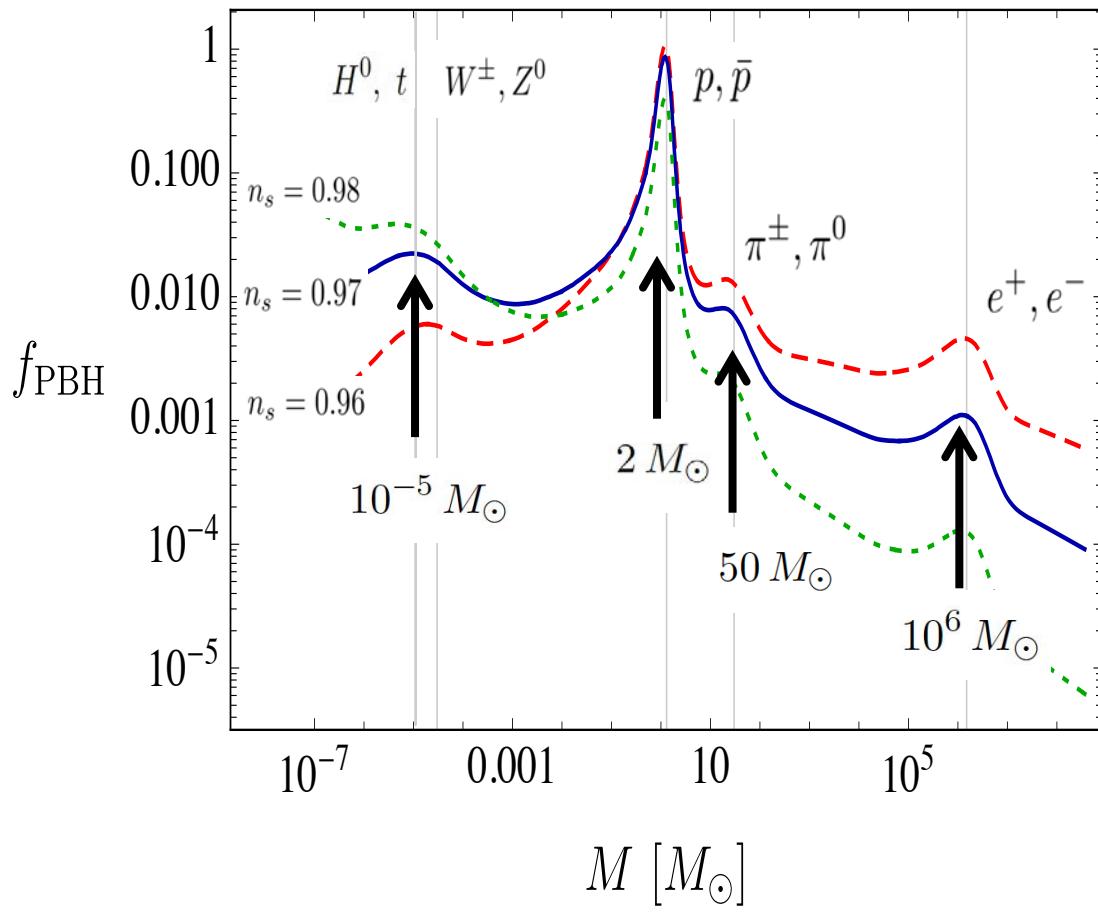


# Thermal history of the universe

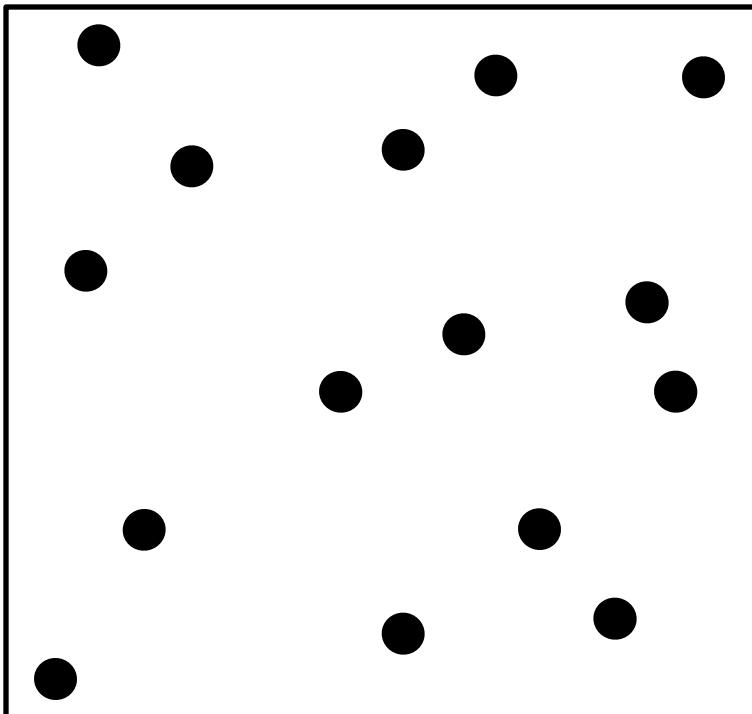


Carr, Clesse, JGB, Kühnel [1906.08217]

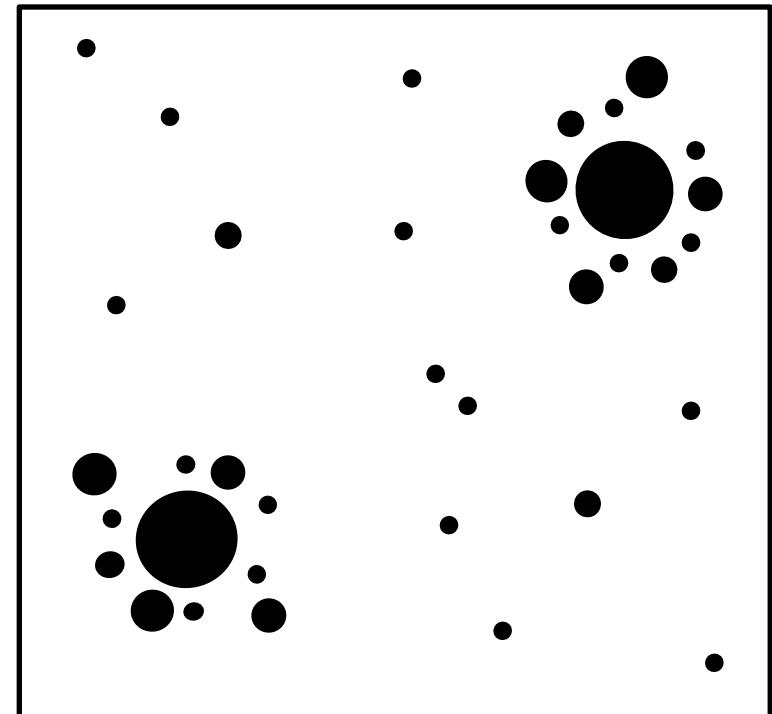
## PBH mass spectrum



# Spatial Distribution PBH



- Monochromatic
- Uniformly distributed



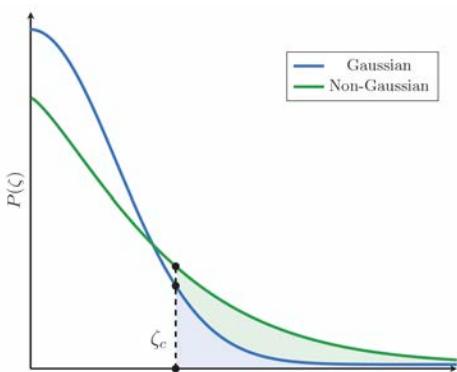
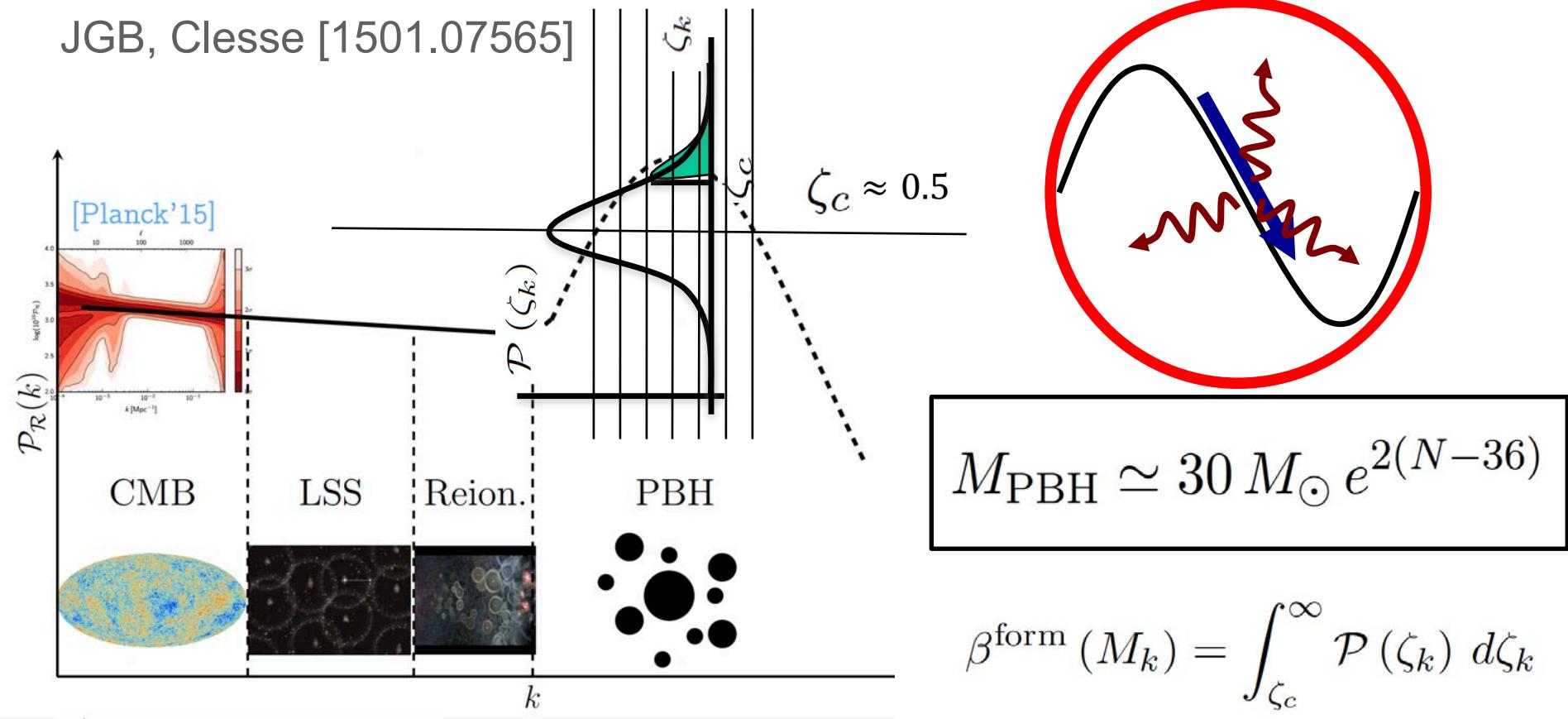
- Broad range of masses
- PBH in clusters

JGB [1702.08275]



# Extended Mass Function of PBH

JGB, Clesse [1501.07565]



$$\beta(N) = \begin{cases} \text{Erfc}\left(\frac{\zeta_c}{\sqrt{2P_\zeta(N)}}\right), & \text{Gaussian statistics ,} \\ \text{Erfc}\left(\sqrt{\frac{1}{2} + \frac{\zeta_c}{\sqrt{2P_\zeta(N)}}}\right), & \chi^2 \text{ statistics} \end{cases}$$

$$\beta^{\text{form}}(M_k) = \int_{\zeta_c}^{\infty} \mathcal{P}(\zeta_k) d\zeta_k$$

# Stochastic $\delta N$ -formalism

## Coarse-grained curvature perturbation

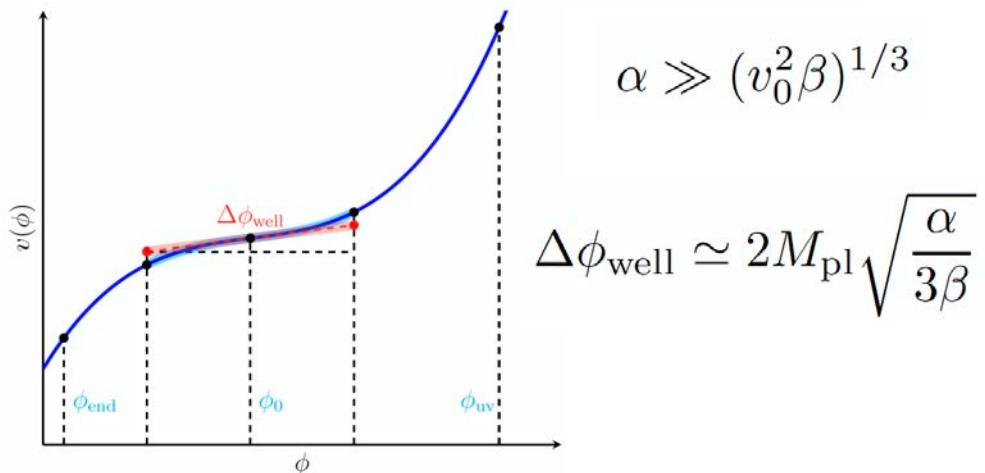
$$ds^2 = -dt^2 + a^2(t)e^{2\zeta(t,\mathbf{x})}\delta_{ij}dx^i dx^j \quad \zeta_{cg}(\mathbf{x}) = \delta N_{cg}(\mathbf{x}) = \mathcal{N}(\mathbf{x}) - \langle \mathcal{N} \rangle$$

$$\frac{1}{M_{pl}^2} \frac{d}{d\mathcal{N}} P_\Phi(\mathcal{N}) = \left( - \sum_i \frac{v_{\phi_i}}{v} \frac{\partial}{\partial \phi_i} + v \sum_i \frac{\partial^2}{\partial \phi_i^2} \right) \cdot P_\Phi(\mathcal{N}) \quad \text{Fokker-Planck Diffusion Eq.}$$

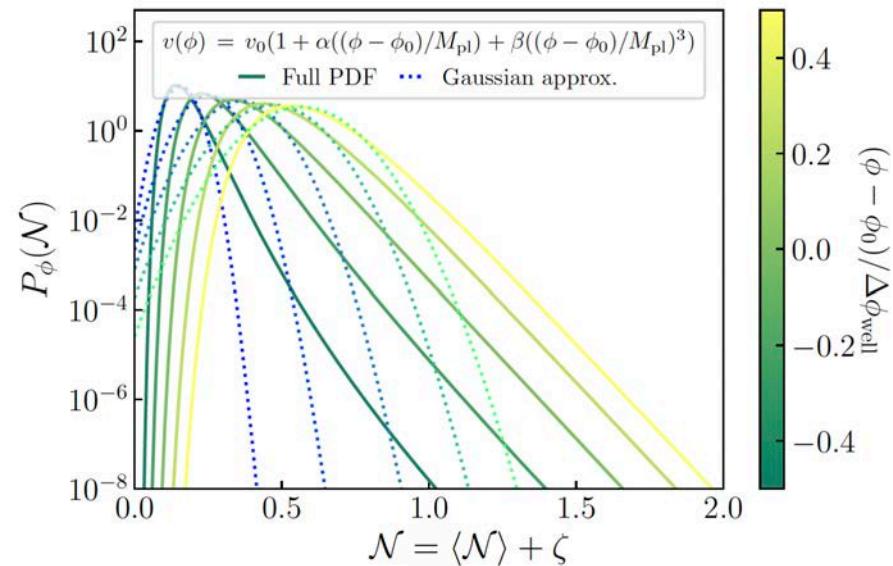
Determined by the poles of the characteristic function

$$P_\phi(\mathcal{N}) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-it\mathcal{N}} \chi_{\mathcal{N}}(t, \phi) dt = \sum_n a_n(\phi) e^{-\Lambda_n \mathcal{N}}$$

$$\chi_{\mathcal{N}}(t, \phi) = \sum_n \frac{a_n(\phi)}{\Lambda_n - it} + \text{regular func.}$$

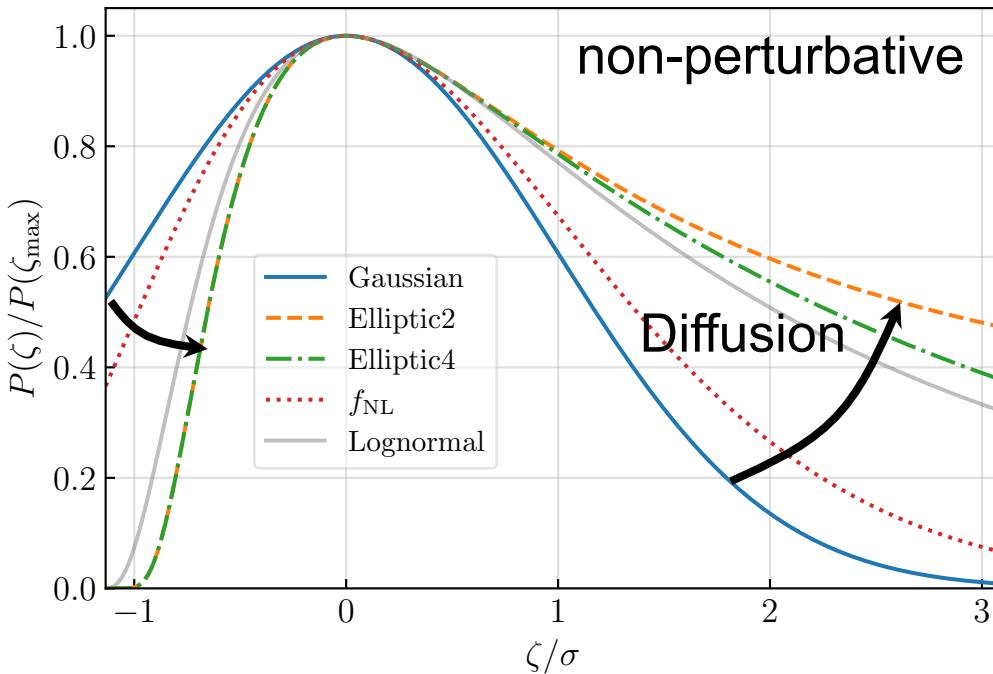


Ezquiaga, JGB, Vennin [1912.05399]



# Quantum Diffusion @ CMB & LSS

Ezquiaga, JGB, Vennin [2207.06317]



Lognormal distributions

$$\text{LN}(x, \rho, \sigma) = \frac{1}{\rho \sigma \sqrt{2\pi}} \exp \left[ -\frac{\ln(x/\rho)^2}{2\sigma^2} - \frac{\sigma^2}{2} \right]$$

$$G(x, \rho, \sigma_G) = \frac{1}{\sigma_G \sqrt{2\pi}} \exp \left[ -\frac{(x - \rho)^2}{2\sigma_G^2} \right]$$

Elliptic Functions

$$P_2(\zeta_k) = -\frac{\pi}{2\mu^2} \vartheta'_2 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2}\mathcal{N}_k} \right)$$

$$P_4(\zeta_k) = \frac{\pi}{2\mu^2\alpha_k} \vartheta'_4 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2}\mathcal{N}_k} \right)$$

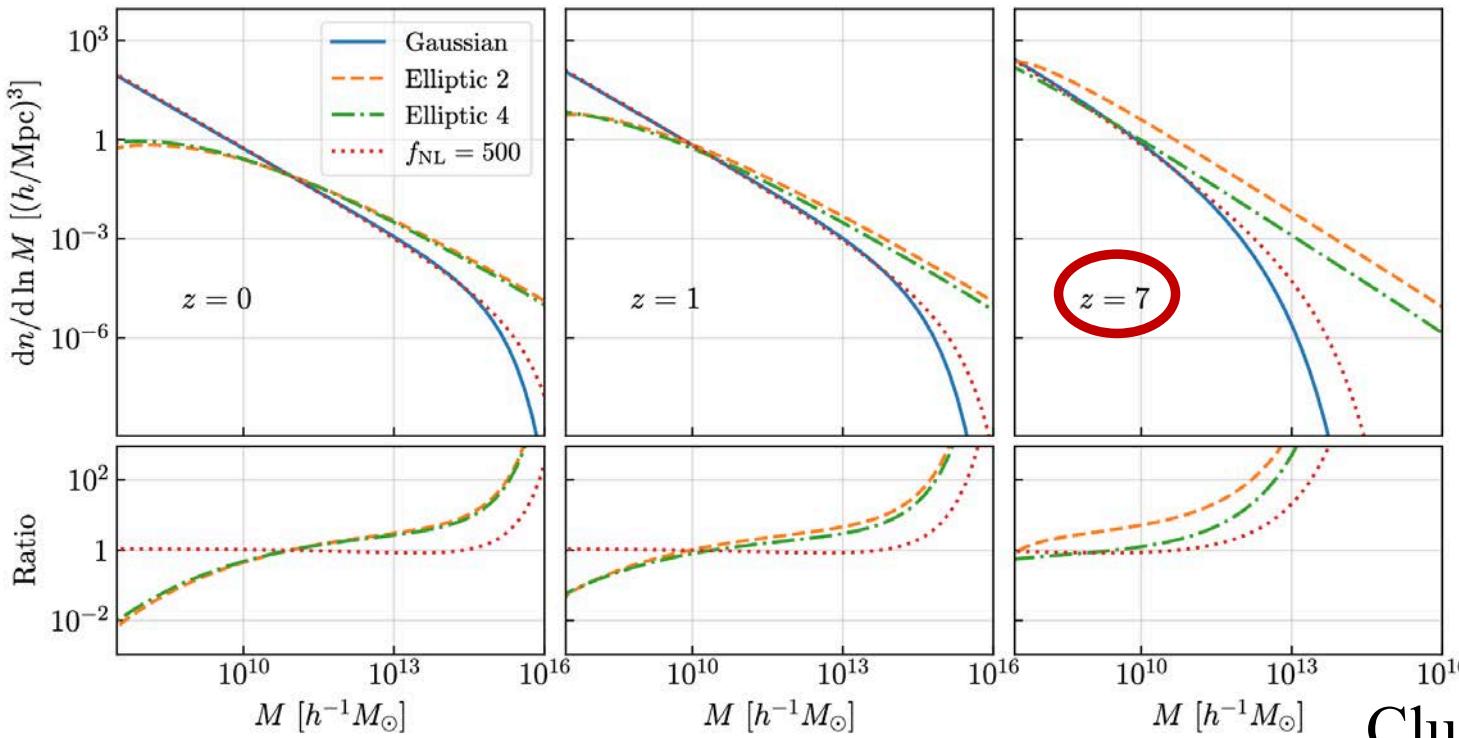
$f_{\text{NL}}$  – expansion (not enough)

$$\zeta(x) = \zeta_G(x) + \frac{3}{5} f_{\text{NL}} \left[ \zeta_G^2(x) - \sigma_G^2(x) \right]$$

$$P_{\text{NL}}(\zeta) = \frac{1}{\sqrt{2\pi\sigma_G^2\Delta}} \left[ e^{-\frac{25(\sqrt{\Delta}-1)^2}{72f_{\text{NL}}^2\sigma_G^2}} + e^{-\frac{25(\sqrt{\Delta}+1)^2}{72f_{\text{NL}}^2\sigma_G^2}} \right]$$

$$\text{where } \Delta(\zeta) = 1 + \frac{12}{5} f_{\text{NL}} \zeta + \frac{36}{25} f_{\text{NL}}^2 \sigma_G^2.$$

# Quantum Diffusion @ CMB & LSS



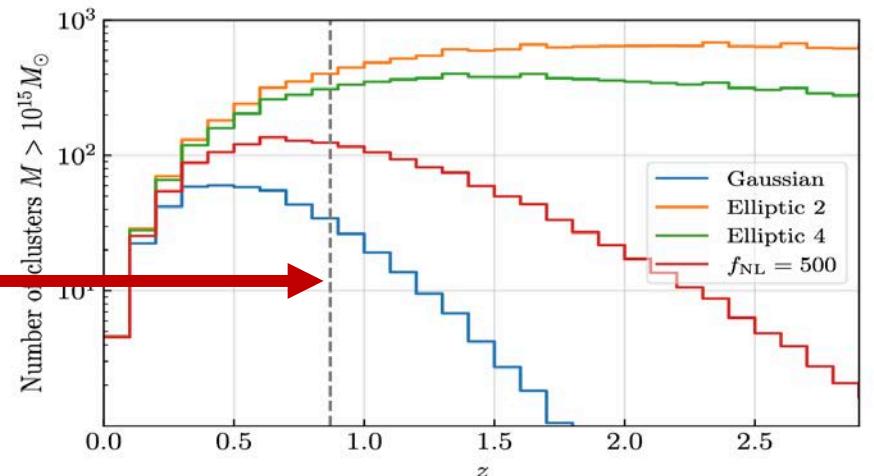
Halo  
Mass  
Function

Cluster Abundance

Ezquiaga, JGB, Vennin [2207.06317]

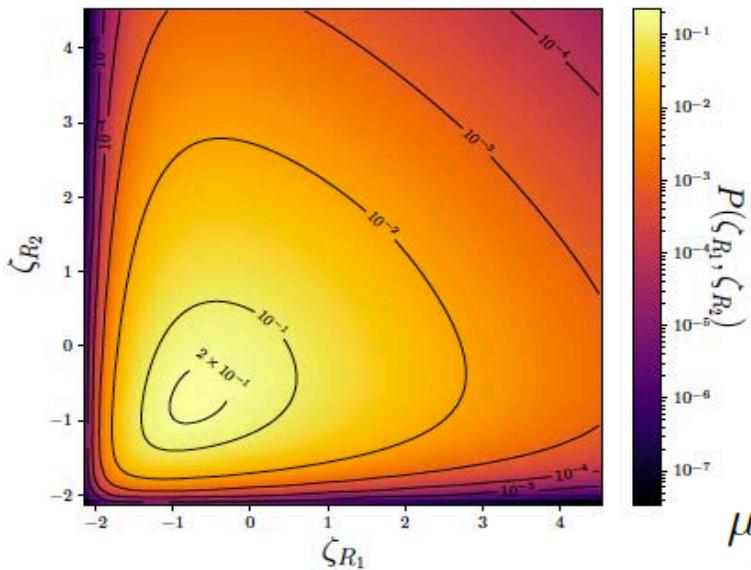
El Gordo

$M \sim 3 \cdot 10^{15} M_\odot$  at  $z = 0.87$

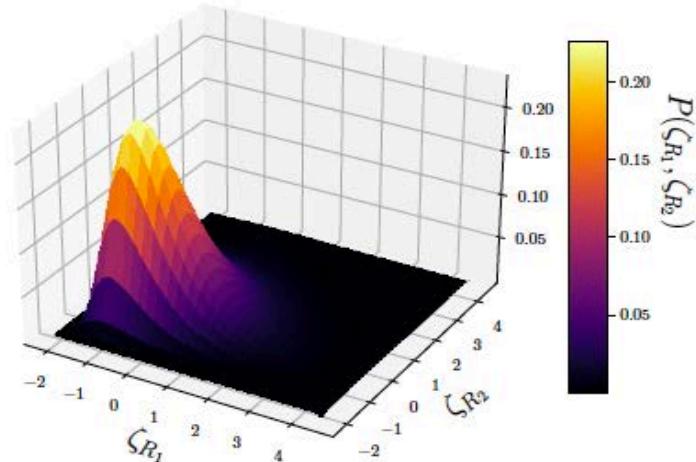


# Clustering from Quantum Diffusion

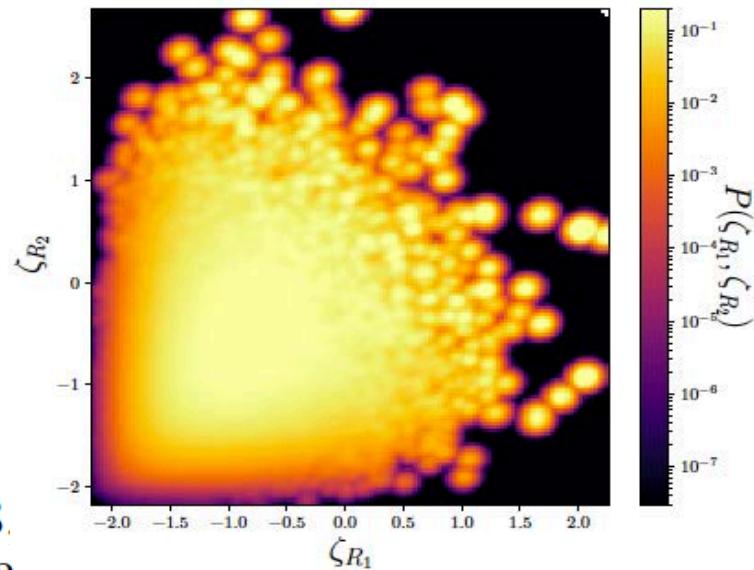
2-pt distribution function



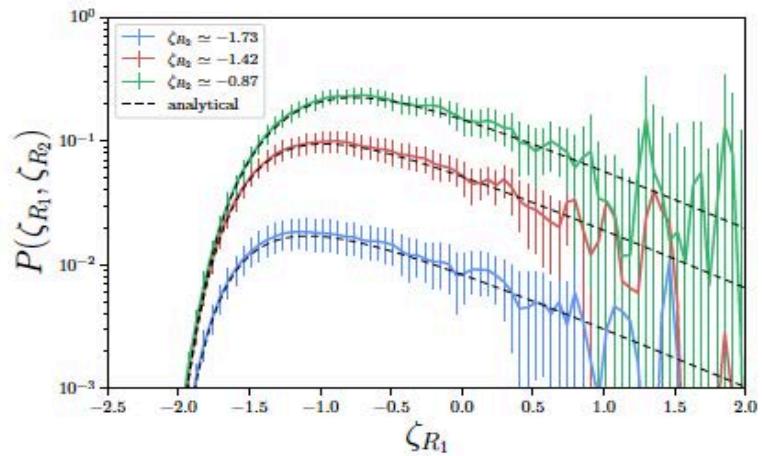
Tilted-well potential



Animali, Vennin [2402.08642]

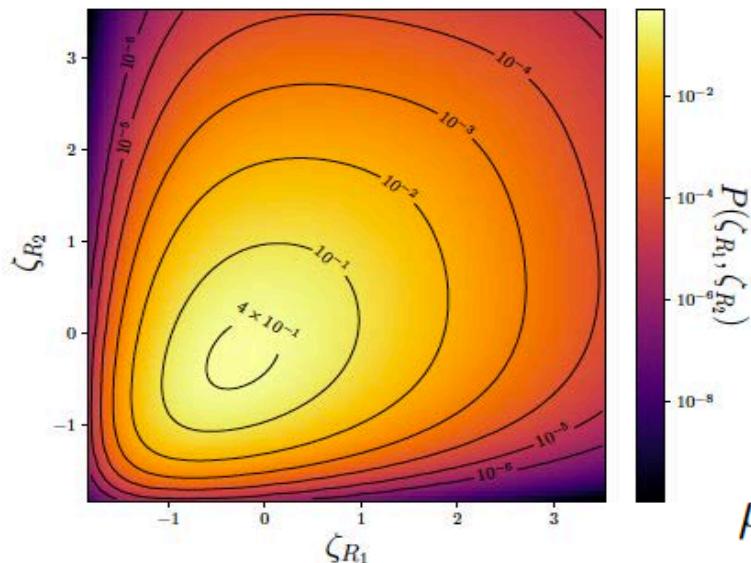


$10^6$  numerical simulations

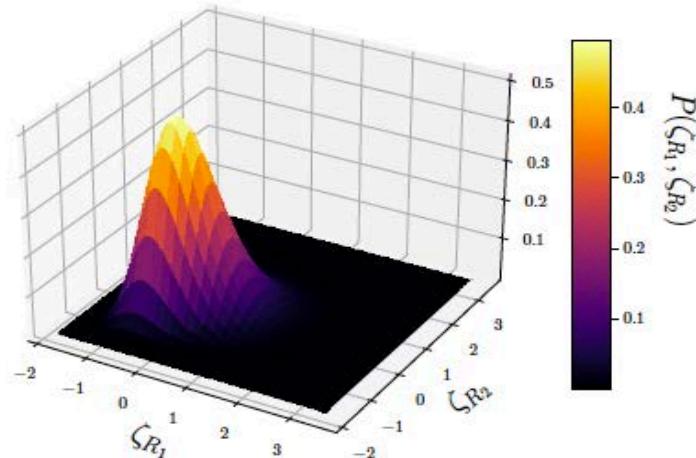


# Clustering from Quantum Diffusion

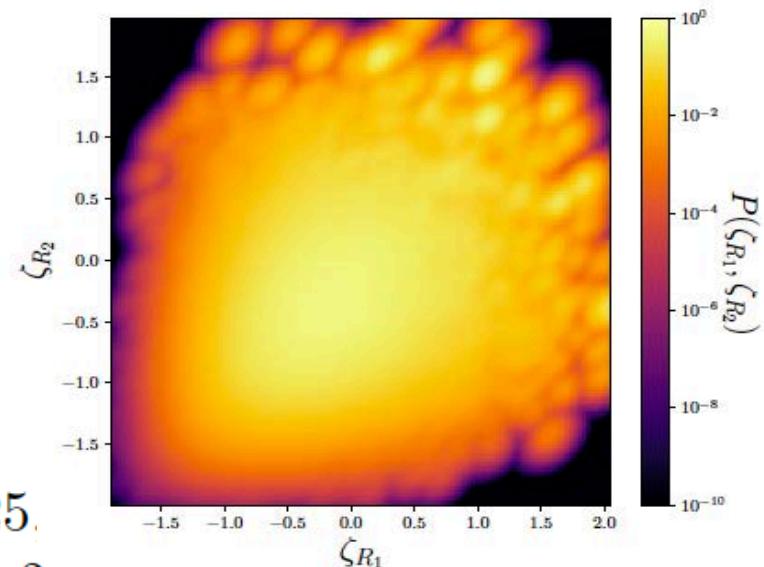
2-pt distribution function



Tilted-well potential



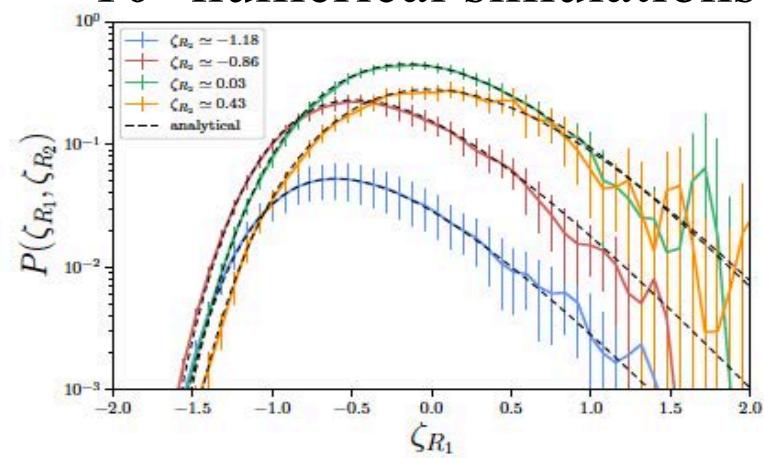
Animali, Vennin [2402.08642]



$$\mu = 25$$

$$d = 0.2$$

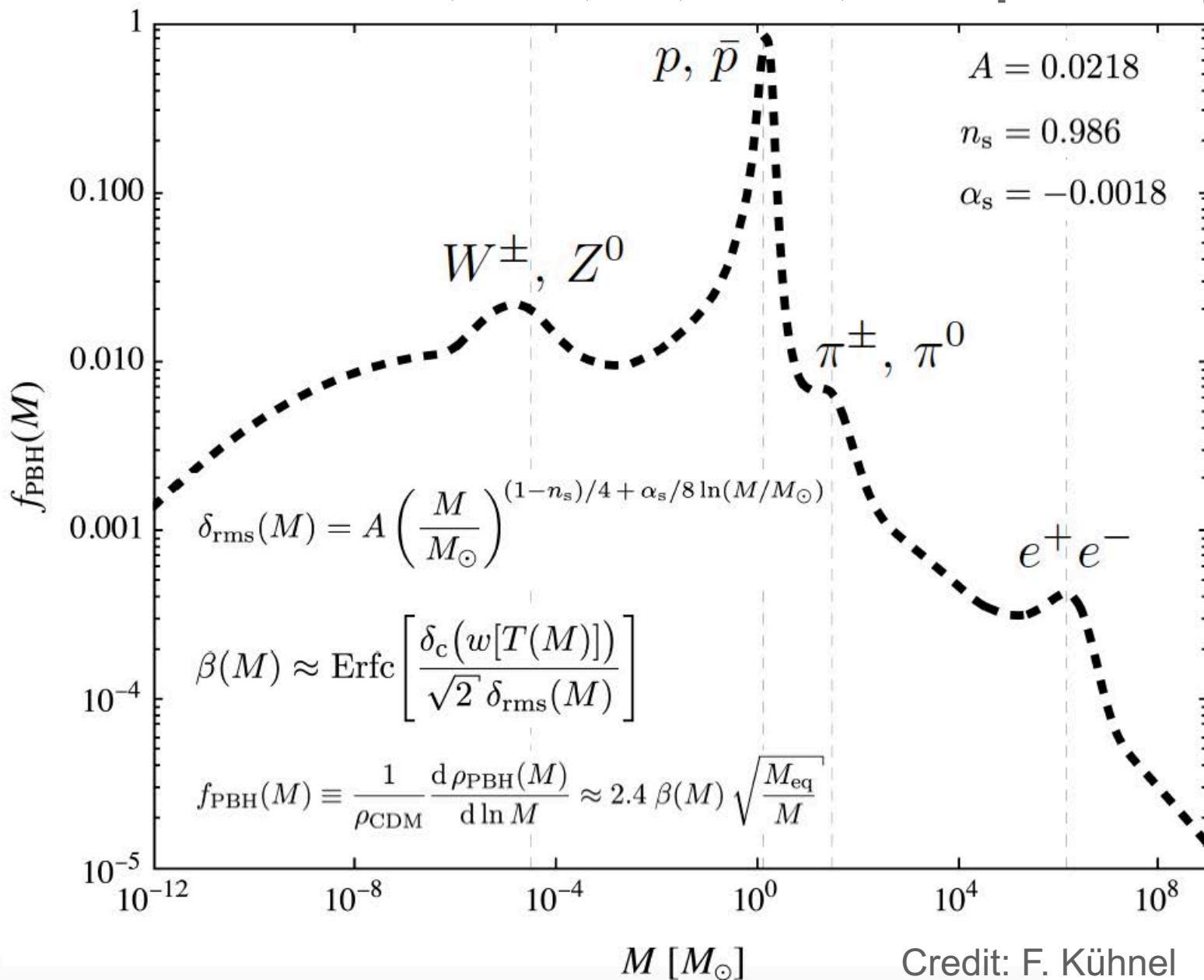
$10^6$  numerical simulations



# Observational Evidences

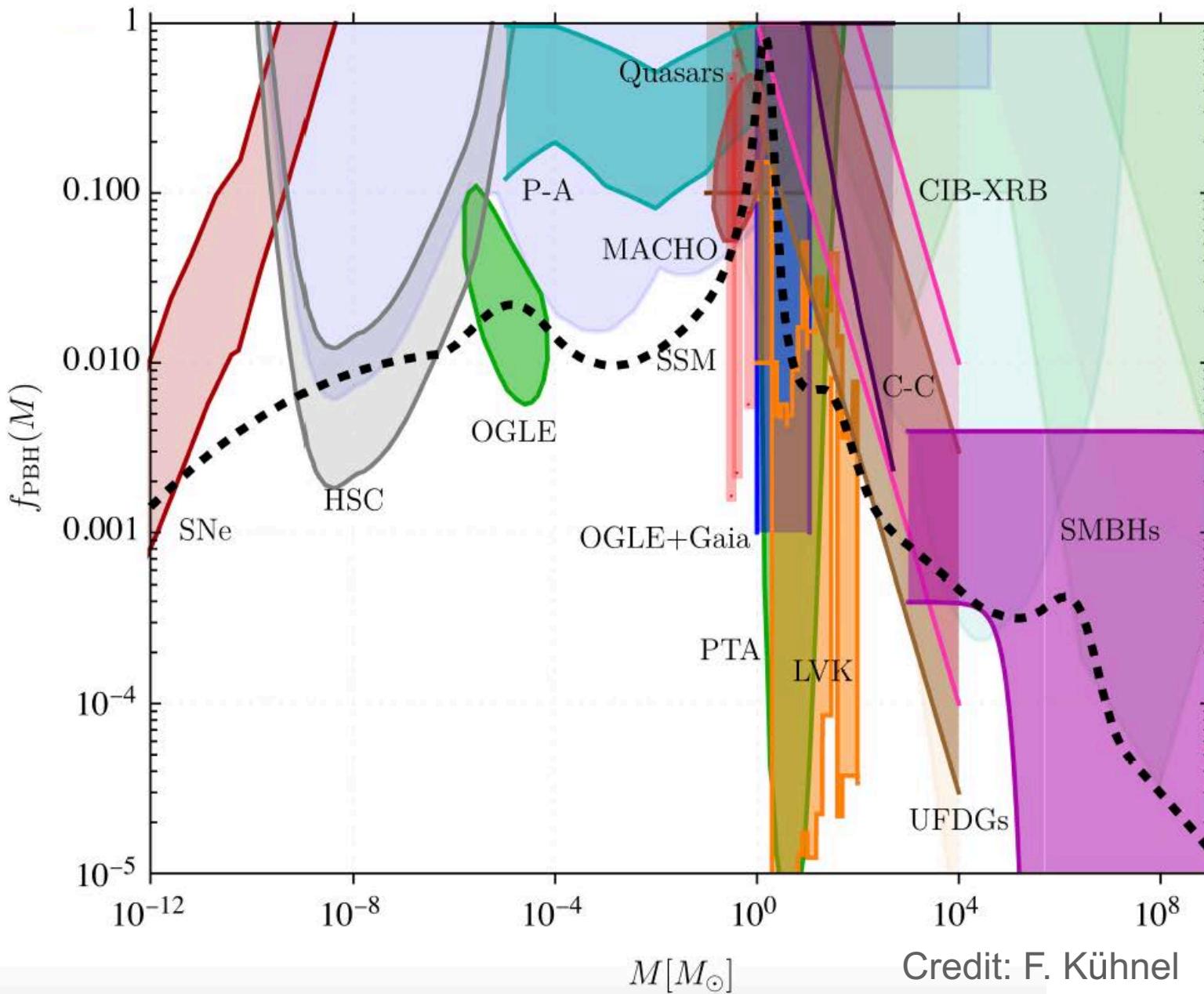
# Observational evidence for primordial black holes

Carr, Clesse, JGB, Hawkins, Kühnel [2306.03903]



# Observational evidence for primordial black holes

Carr, Clesse, JGB, Hawkins, Kühnel [2306.03903]



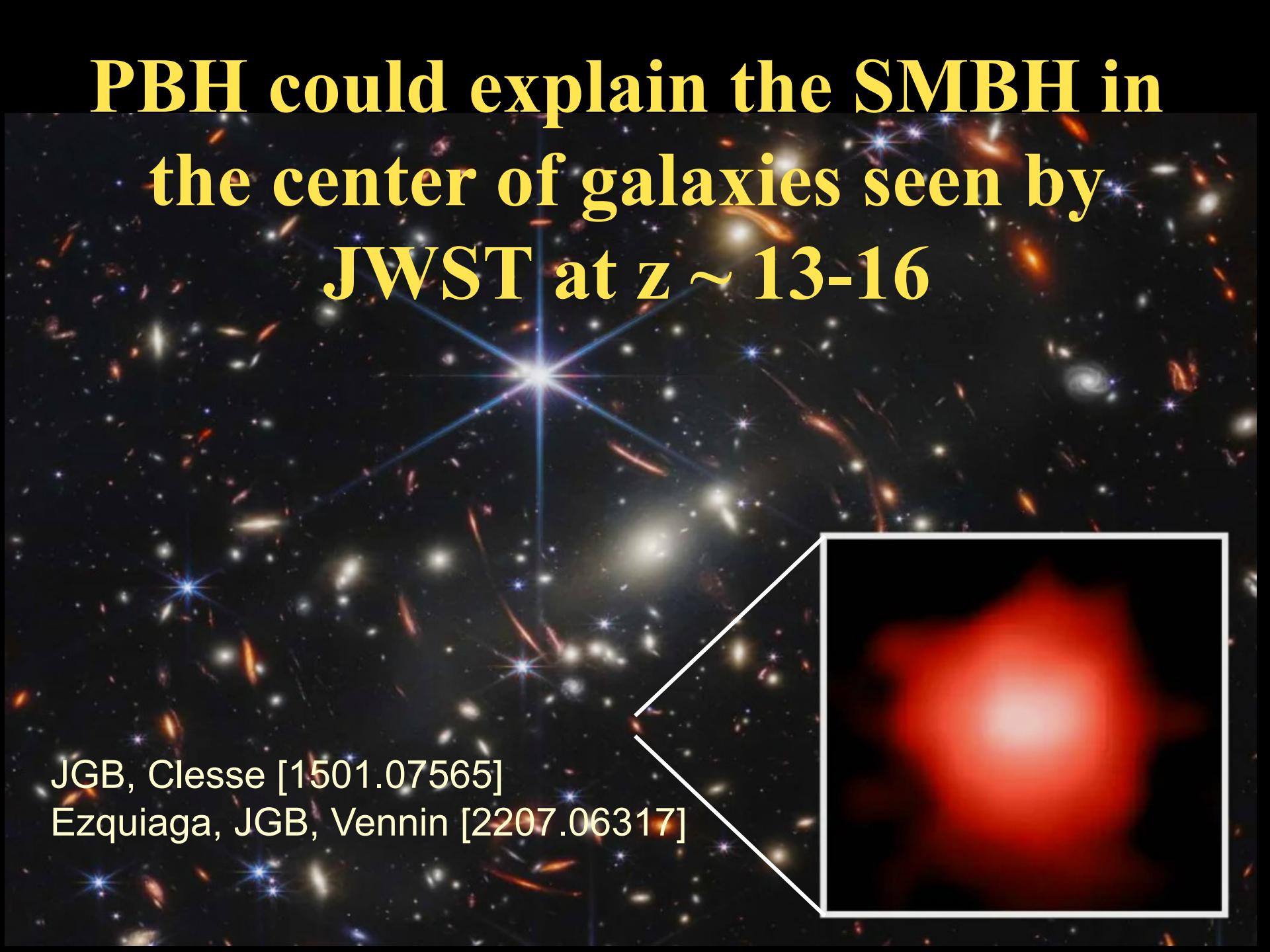
$M[M_\odot]$

Credit: F. Kühnel

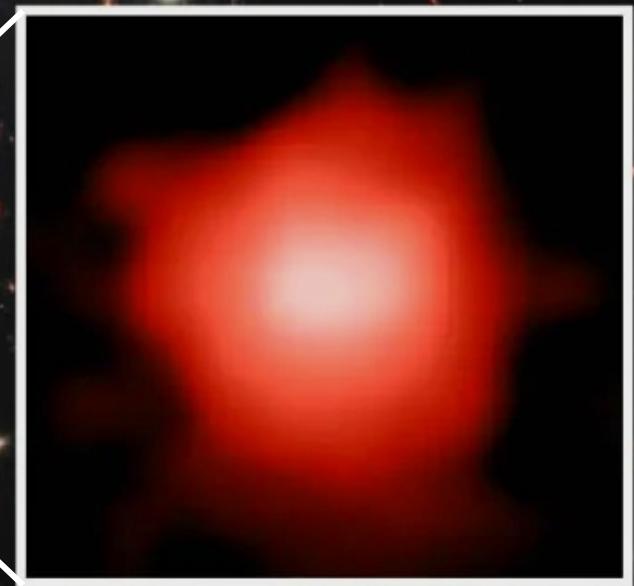
# Observational evidence for primordial black holes

- Microlensing of Quasars
- **MACHO events to LMC (Gaia DR3)**
- Andromeda M31 pixel lensing
- **OGLE+Gaia (solar-mass)**
- OGLE+HSC (planetary-mass)
- MW ultra-high-velocity stars (Gaia DR2)
- MW tidal stream's perturbations
- UFDG min size
- UFDG mass-to-light ratio
- MW Disk heating
- Core-cusp in dwarf spheroidals
- **SMBH seed accretion (JWST)**
- **high-z galaxies (HST/JWST)**
- CIB - XRB source-subtracted correlations
- Radio background
- exploding white dwarfs SN (Goobar)
- **SSM black hole candidates (LVK)**
- **LVK - GWTC-3 - (mass+spin+merger rates)**
- PTAs – ISGW (Nanograv-IPTA)
- Dark Matter halos - rotation curves
- Matter-antimatter asymmetry

# PBH could explain the SMBH in the center of galaxies seen by JWST at $z \sim 13-16$



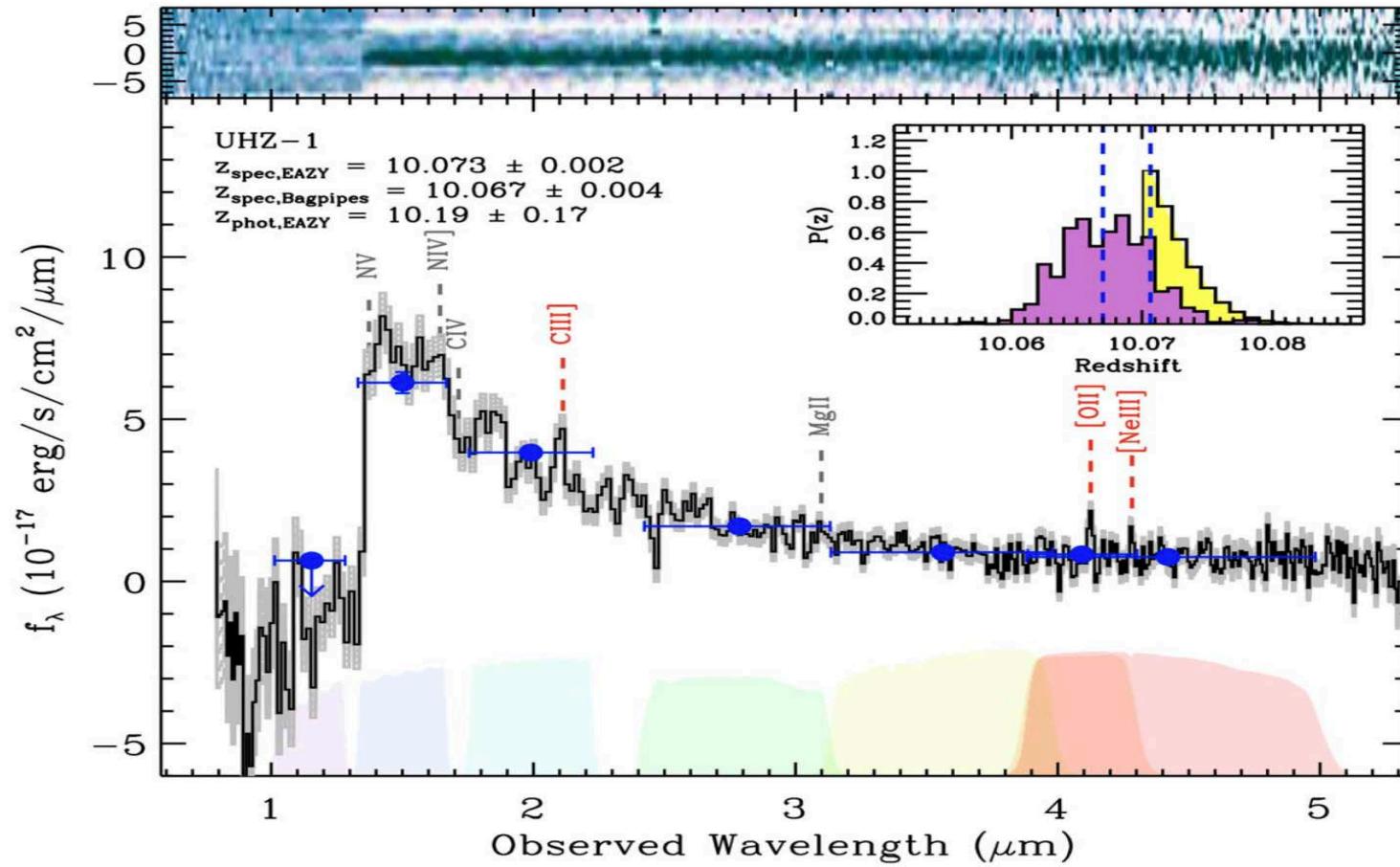
JGB, Clesse [1501.07565]  
Ezquiaga, JGB, Vennin [2207.06317]



# PBH could explain SMBH in AGN seen by JWST+Chandra at $z \sim 10$

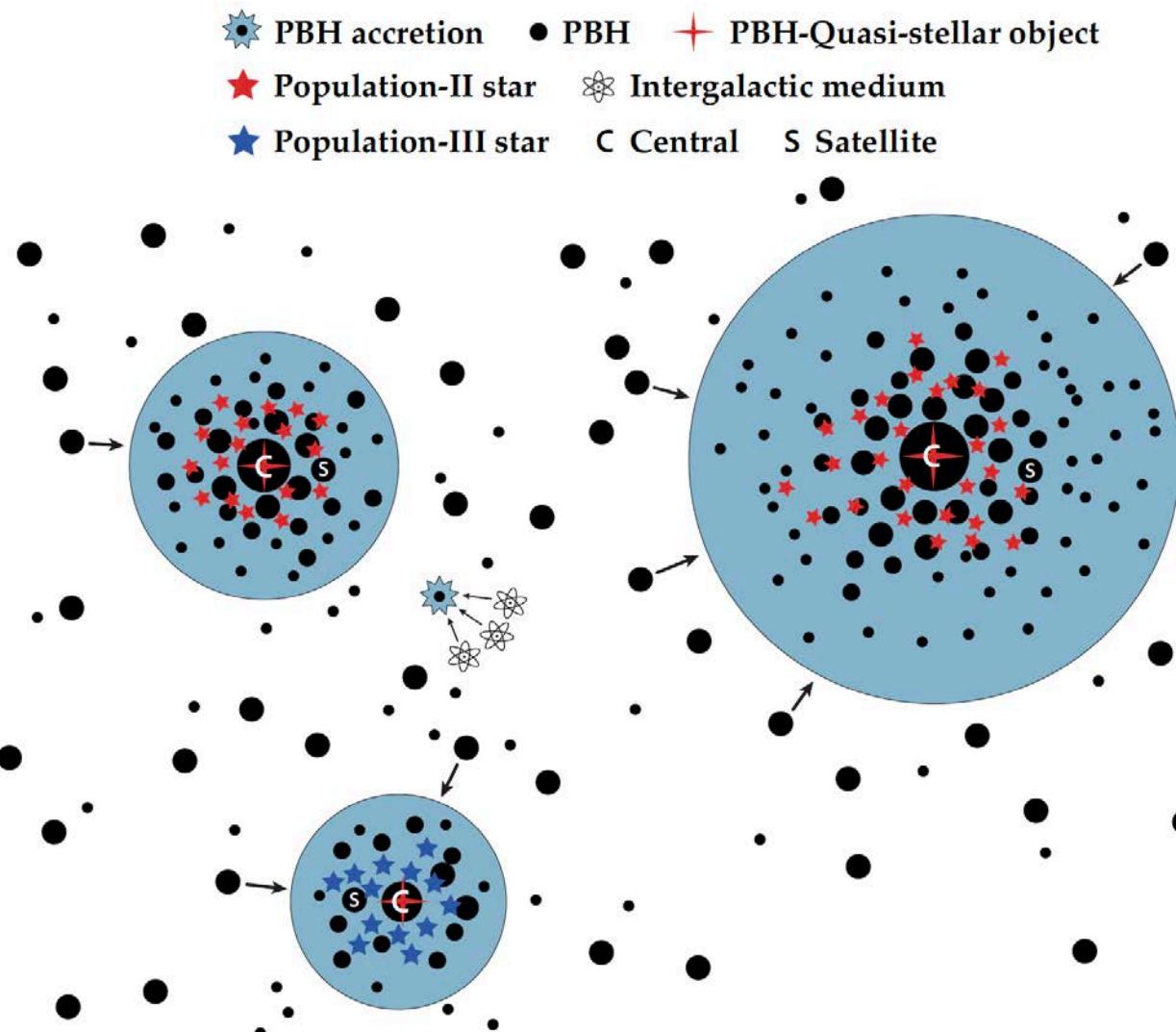
THE ASTROPHYSICAL JOURNAL LETTERS, 955:L24 (8pp), 2023 September 20

Goulding et al.



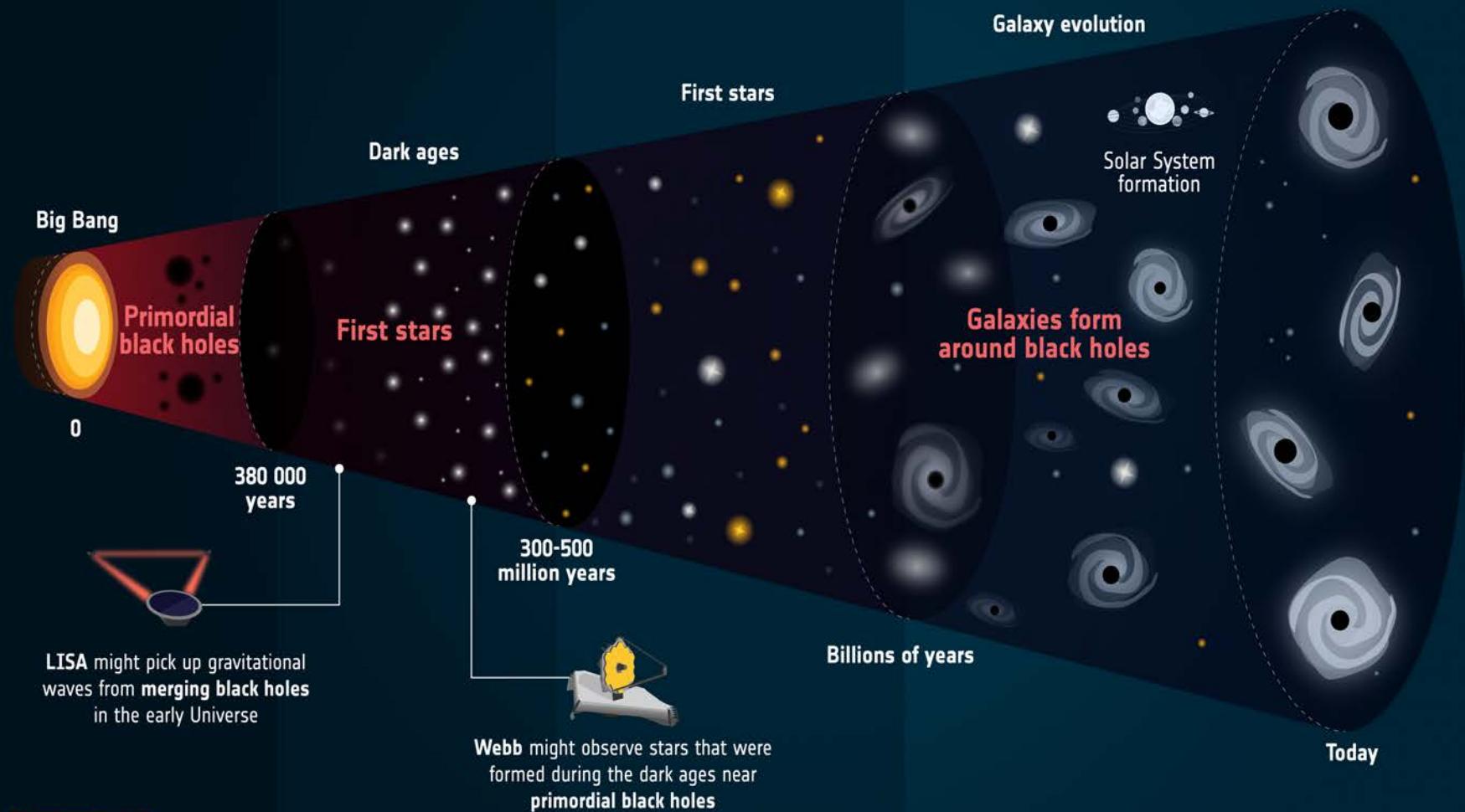
**Figure 2.** JWST/NIRSpec Prism spectroscopy of UHZ-1. Upper panel: 2D MSA Prism spectroscopy produced by `msaexp`. Lower panel: 1D spectral extraction in  $f_\lambda$  (in units of  $10^{-17}$  erg s $^{-1}$  cm $^{-2}$  μm $^{-1}$ ) with associated statistical uncertainties (gray shaded region). Slit-loss corrections are defined by convolution of the JWST photometry with the Prism spectrum (see Section 2). Prominent and/or expected emission features are highlighted assuming  $z_{\text{spec}} = 10.07$  with significant  $>3\sigma$  detections and nondetections labeled in red and gray, respectively. Overlaid are the JWST/NIRCam photometry (blue circles) with associated filter responses highlighted. Inset panel: redshift probability distributions for fits to the NIRSpec spectroscopy produced by EAZY (yellow) and BAGPIPES (purple) packages.

# Cappelluti, Hasinger, Natarajan [2109.08701]



**Figure 22.** Illustration of PBH clustering at redshifts 10 – 15. Initially, PBHs (black dots) capture baryons while accreting, thereby contributing to the cosmic X-ray background. Lighter PBHs later form halos around more massive ones and initiate star formation; the lowest mass halos first form Population III stars, which generate a faint cosmic infrared background, and the higher mass ones then yield Population II stars. The most massive (central) supermassive PBH continues to accrete and merge with other PBHs. It appears as the central source in the infrared and X-ray emission, with the smaller PBHs and stars filling the halo as satellites.

# HISTORY OF THE UNIVERSE WITH PRIMORDIAL BLACK HOLES

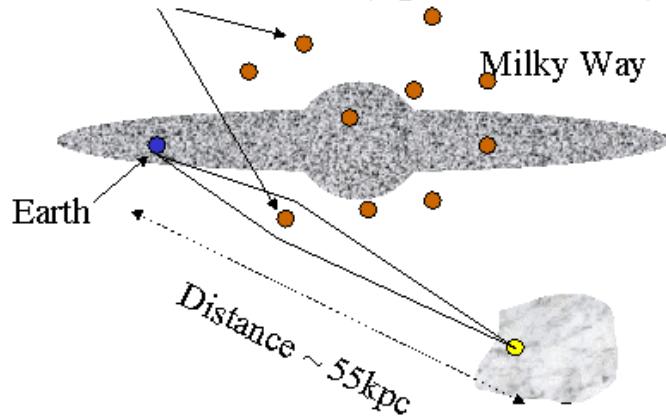


#ExploreFarther

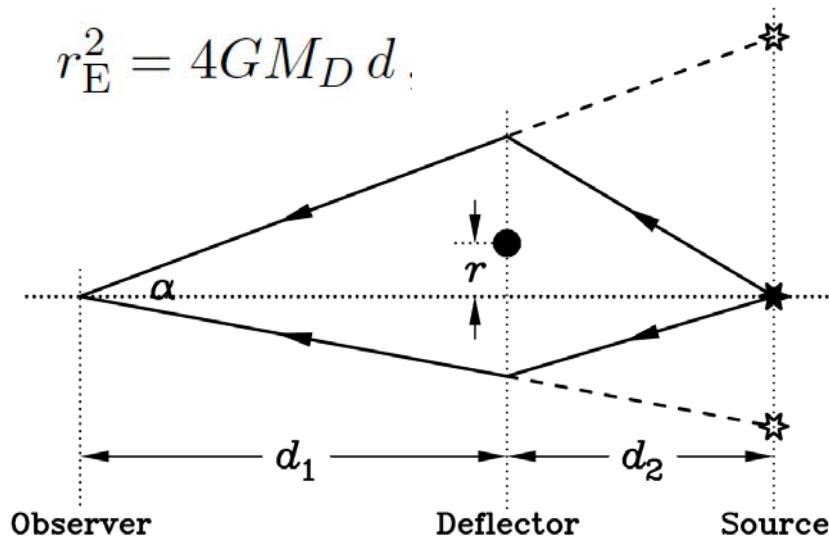
# Microlensing

# Microlensing

Gravitational lenses (e.g., brown dwarfs)



$$r_E^2 = 4GM_D d$$



$$d = \frac{d_1 d_2}{d_1 + d_2}$$

$$A = \frac{2+u^2}{u\sqrt{4+u^2}} \quad u = \frac{r}{r_E} \quad \text{amplification}$$

$$\frac{1}{2} \overline{Dt} = \frac{r_E}{v} = \frac{\sqrt{4GM_D d}}{v} \quad \text{average crossing}$$

$$M_D = 100 M_{\odot} \Rightarrow \overline{Dt} = 4 \text{ years}$$

$$M_D = 10 M_{\odot} \Rightarrow \overline{Dt} = 1.23 \text{ years}$$

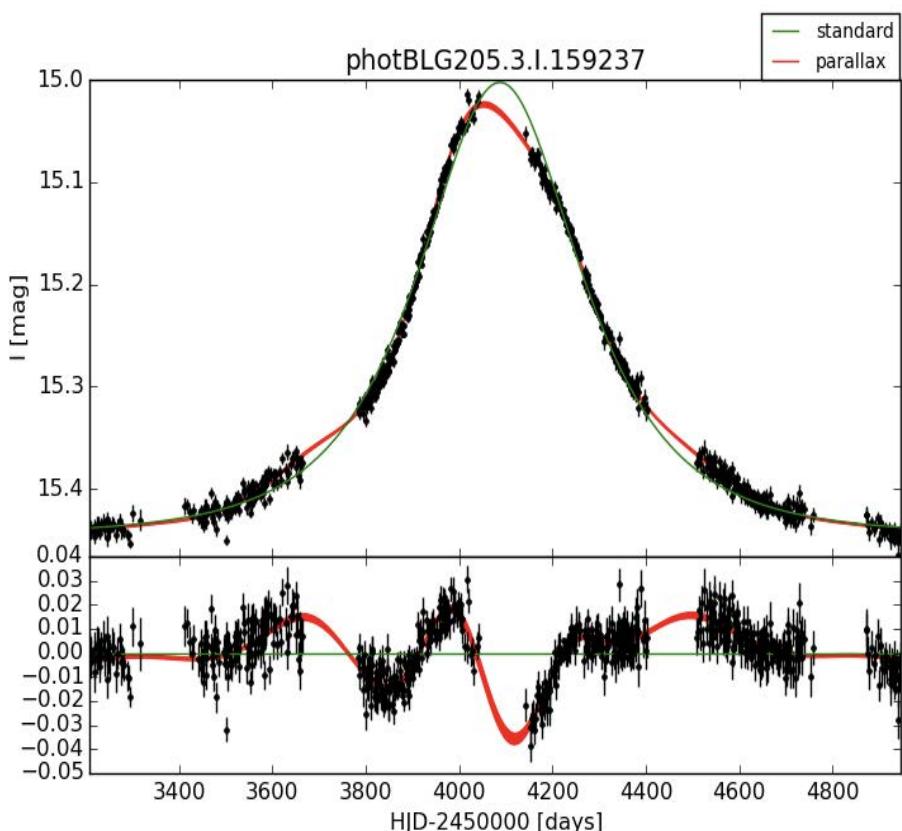
$$M_D = 1 M_{\odot} \Rightarrow \overline{Dt} = 5 \text{ months}$$

$$M_D = 0.1 M_{\odot} \Rightarrow \overline{Dt} = 1.5 \text{ months}$$

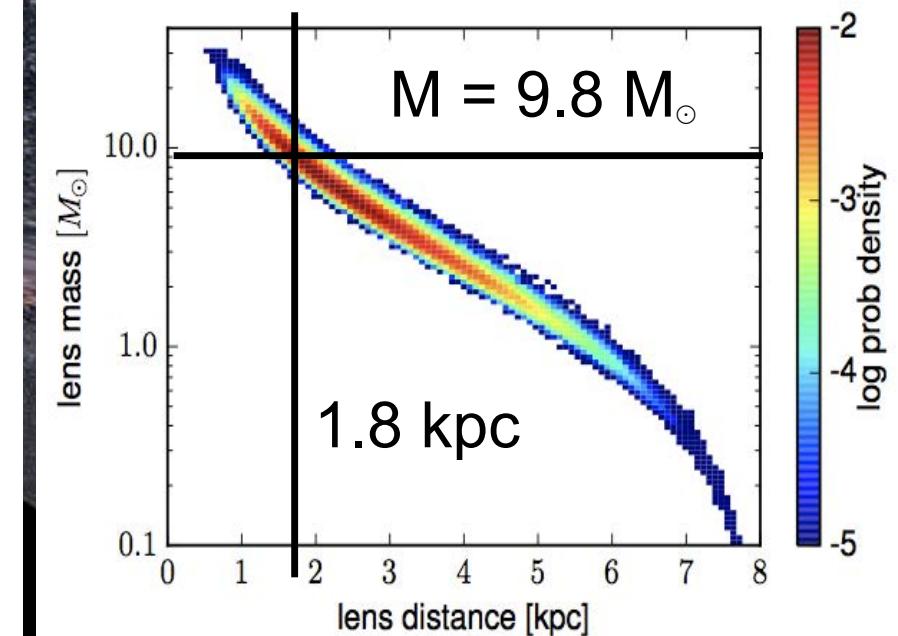
$$M_D = 0.01 M_{\odot} \Rightarrow \overline{Dt} = 2 \text{ weeks}$$

# OGLE E3-UL-PAR-02 - candidate BH

Credit: L. Wyrzykowski



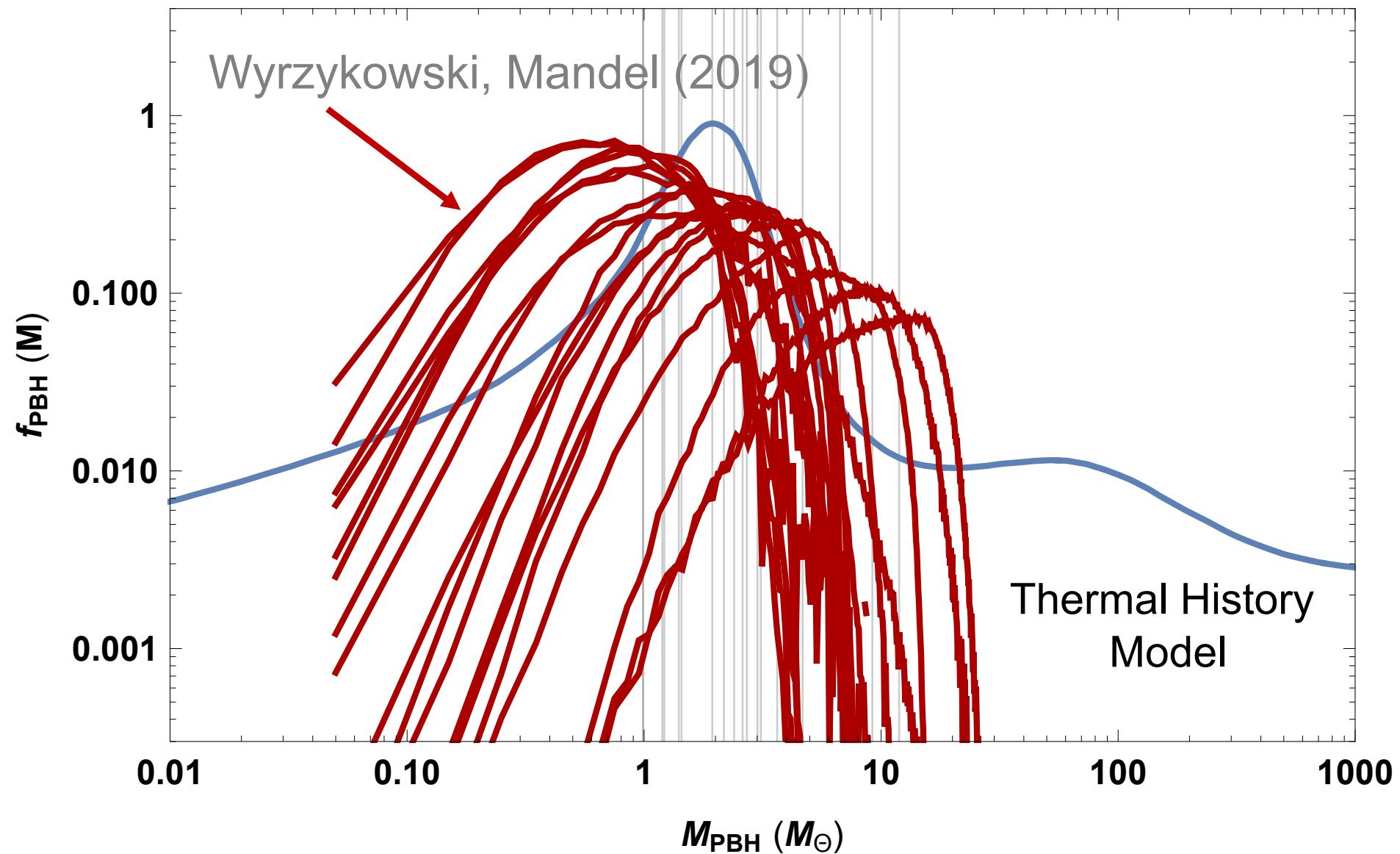
OGLE photometry  
from 2001-2008  
and microlensing model



$$\frac{1}{2} \overline{Dt} = \frac{r_E}{v} = \frac{\sqrt{4GM_D d}}{v}$$

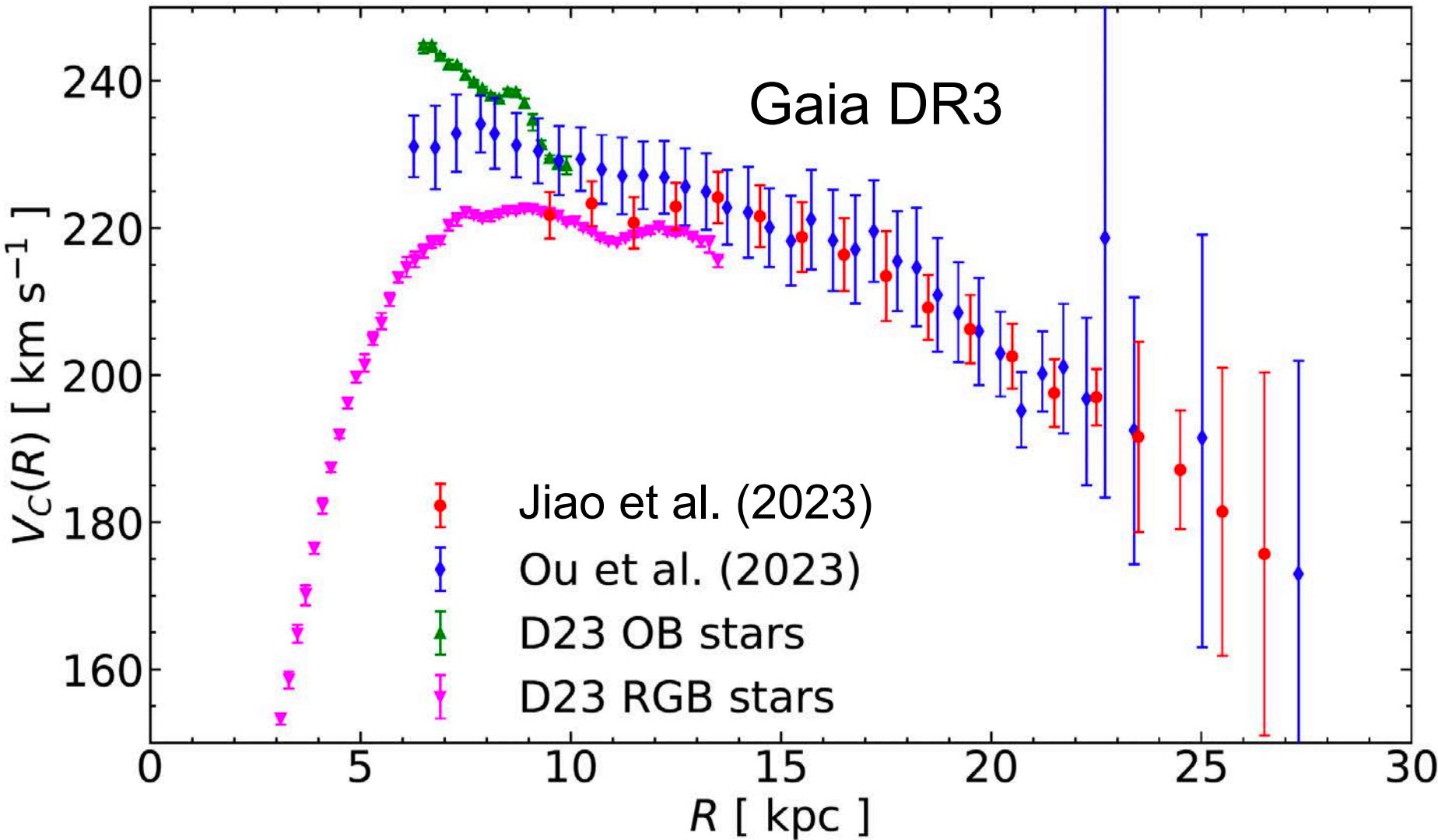
**Mass, Distance**

(degenerated estimate)



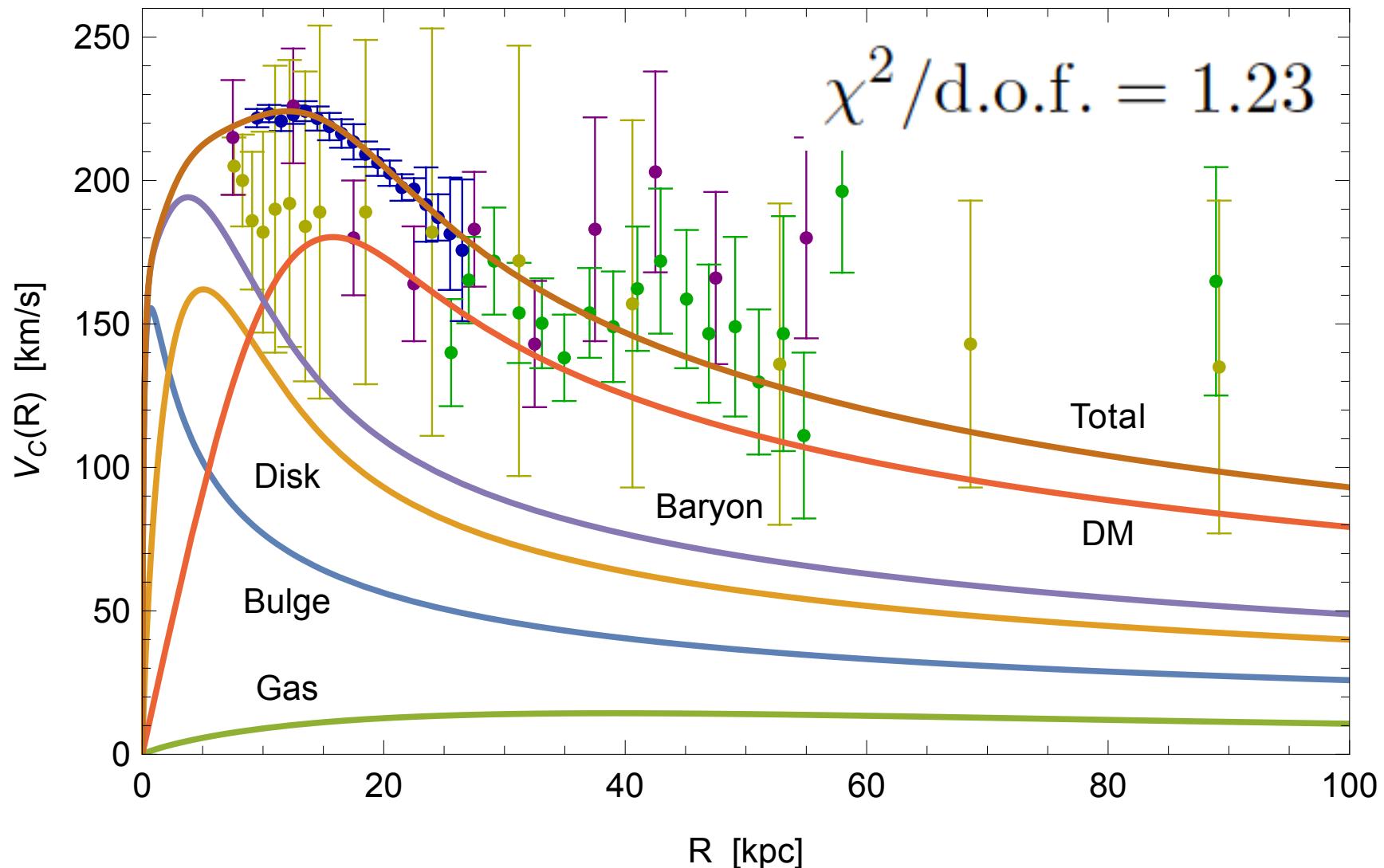
# MW rotation curves

J. Jiao et al. (2023)  
X. Ou et al. (2023)



# MW rotation curves

JGB, Hawkins [2402.00212]



# Optical depth

JGB, Hawkins [2402.00212]

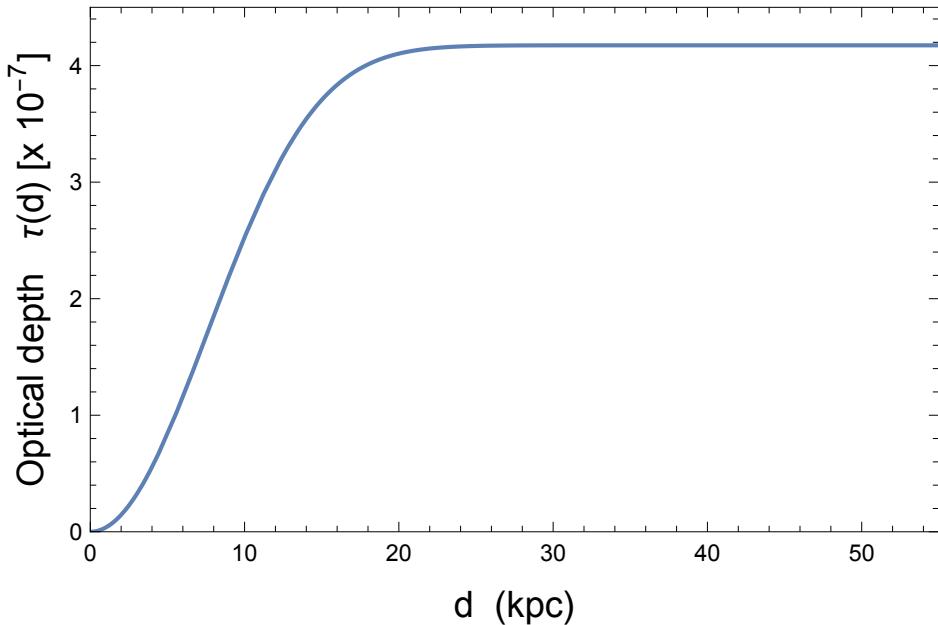
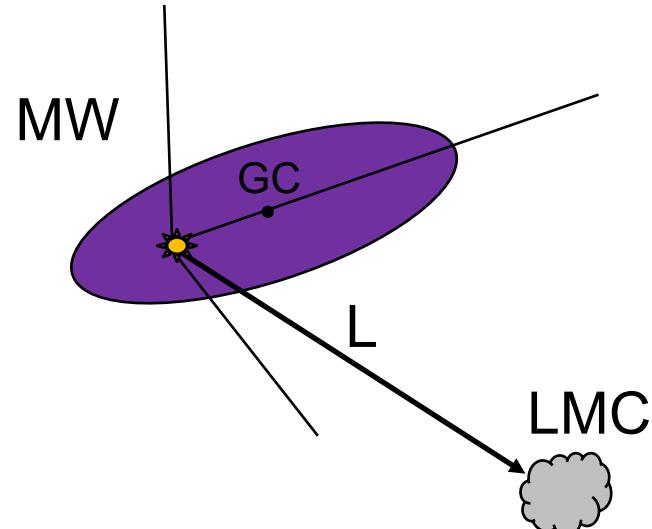
$$r_E^2(x) = \frac{4GML}{c^2} \cdot x(1-x)$$

$$\tau = \frac{4\pi GL^2}{c^2} \int_0^1 \rho(R) x(1-x) dx$$

$$R = L(x_0^2 - 2x_0x \cos b \cos l + x^2)^{1/2}$$

$$(b = -33^\circ, l = 280^\circ)$$

$$x_0 = R_\odot/L$$



# Expected No. events

JGB, Hawkins [2402.00212]

$$N_{\text{exp}}(M) = E \int_0^\infty \frac{d\Gamma}{d\hat{t}}(M) \xi(\hat{t}) d\hat{t}$$

MACHO survey  $E = 6.12 \times 10^7$  objects · years

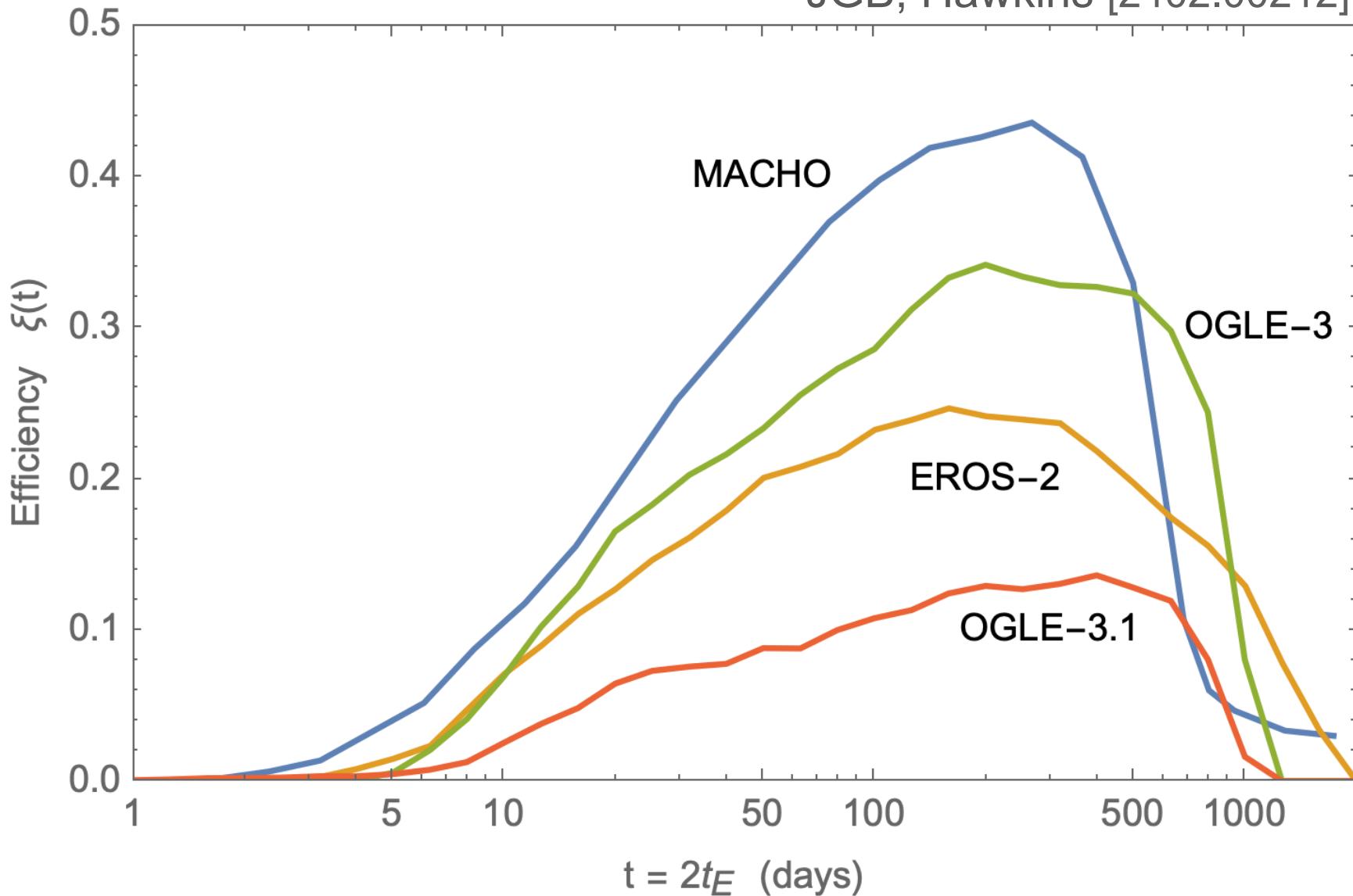
EROS-2 survey  $E = 3.8 \times 10^7$  objects · years

$$\frac{d\Gamma}{d\hat{t}}(M) = \frac{32L}{\hat{t}^4 v_c^2 M} \int_0^1 \rho(R) r_E^4(x) \exp\left[-\frac{4r_E^2(x)}{\hat{t}^2 v_c^2}\right] dx$$

efficiency function  $\xi(\hat{t})$

# Efficiency Function

JGB, Hawkins [2402.00212]



# Microlensing Statistics

JGB, Hawkins [2402.00212]

the number of *observed* events is Poisson distributed.

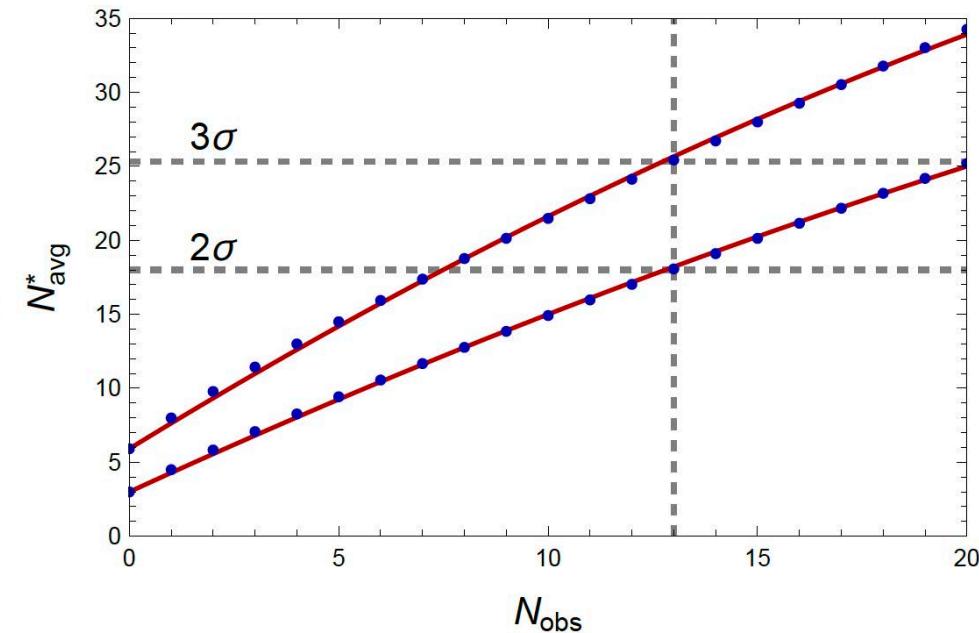
$$P(N_{\text{obs}}) = \frac{e^{-N_{\text{avg}}} N_{\text{avg}}^{N_{\text{obs}}}}{N_{\text{obs}}!} = 0.05 \quad N_{\text{obs}} = z$$

$$N_{\text{avg}} \leq N_{\text{avg}}^* \simeq 3 + \ln \left( \frac{N_*^z}{z!} \right) \simeq 3 + 1.3z - 0.01z^2$$

95% confident ( $2\sigma$ )

$$N_{\text{avg}}^* \simeq 5.9 + 1.74z - 0.017z^2$$

99.73% confidence ( $3\sigma$ )



# Constraints

JGB, Hawkins [2402.00212]

$$C(M) = \frac{N_{\text{avg}}}{N_{\text{exp}}(M)} \leq \frac{N_{\text{avg}}^*}{N_{\text{exp}}(M)} \quad \text{monochromatic}$$

extended mass distribution

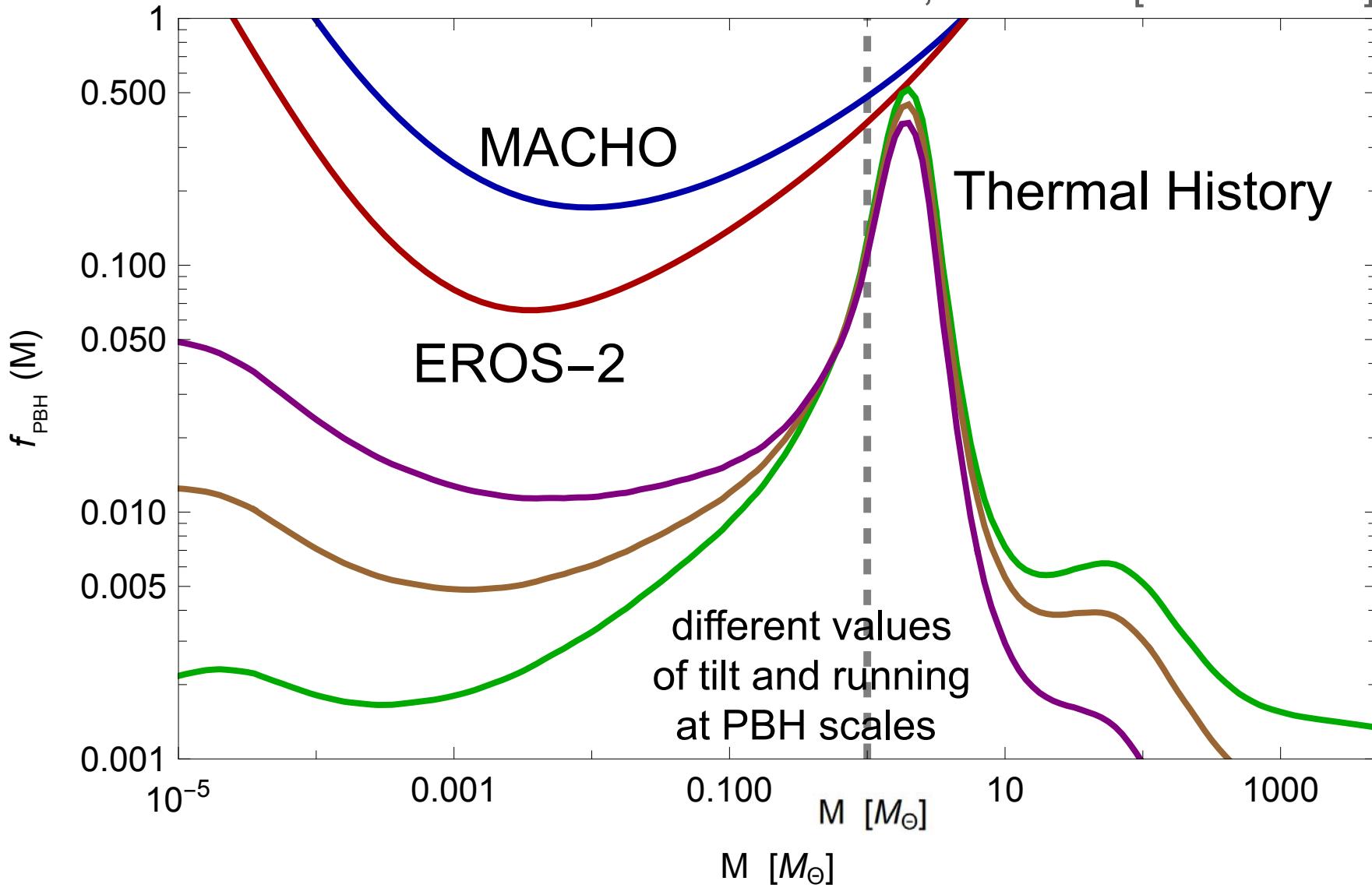
$$\int_0^\infty \frac{dM}{M} f(M) N_{\text{exp}}(M) \leq N_{\text{avg}}^*$$

$$\int_0^\infty \frac{dM}{M} f(M) = f_{\text{PBH}} \quad \text{normalized}$$

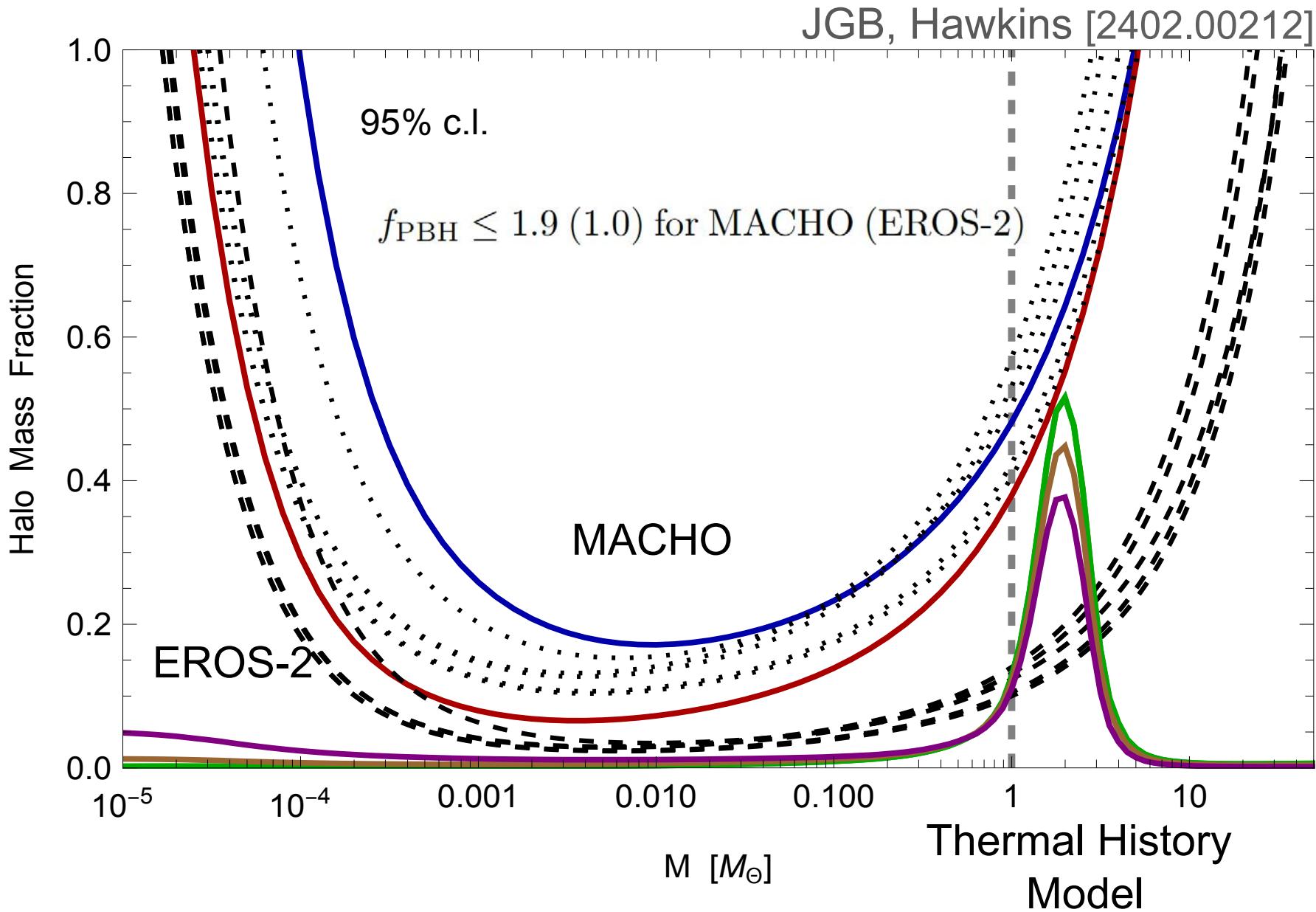
$$f_{\text{PBH}} \leq \left[ \int_0^\infty \frac{dM}{M} \frac{f(M)}{C(M)} \right]^{-1}$$

# PBH Constraints

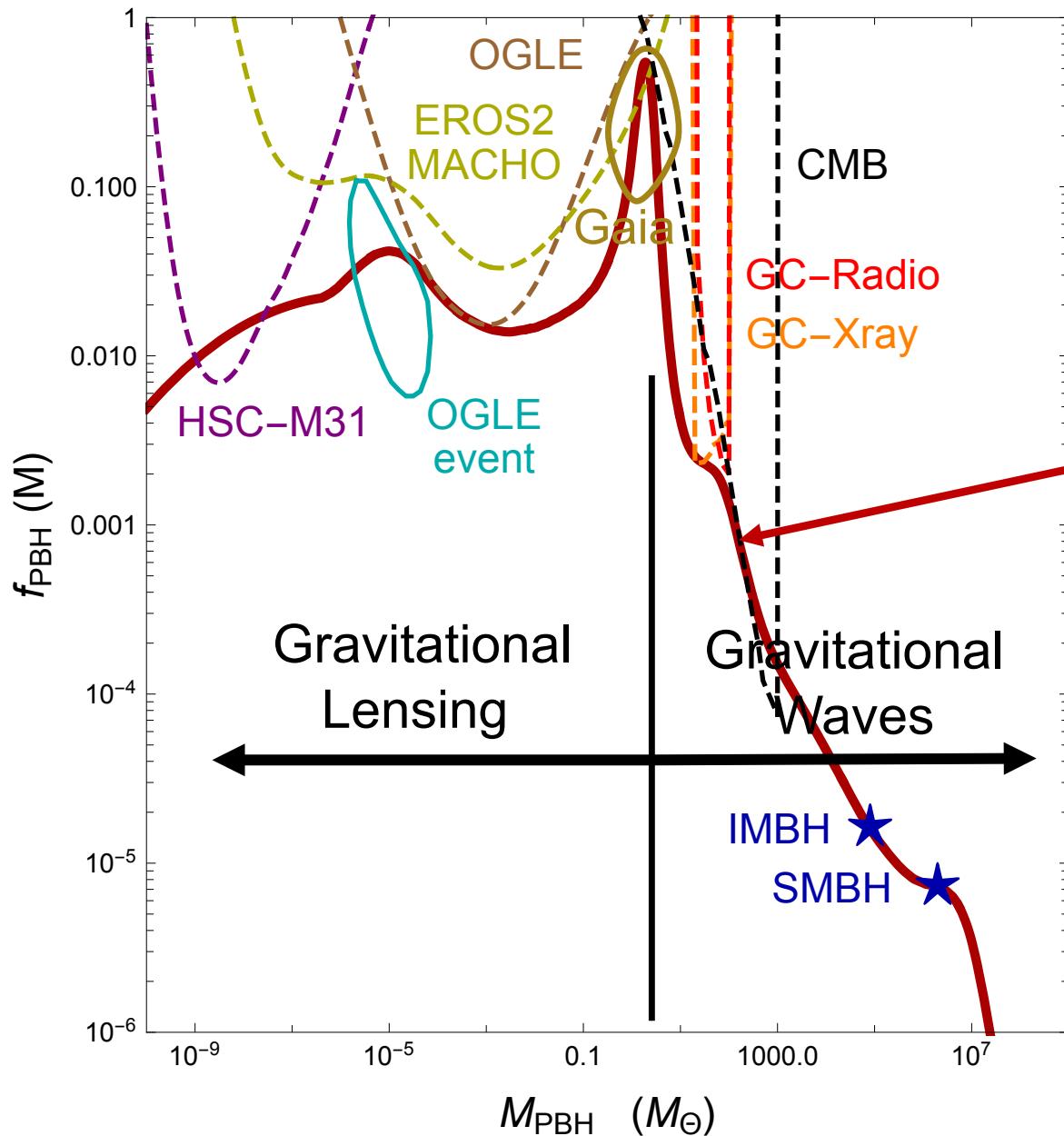
JGB, Hawkins [2402.00212]



# Halo Mass Fraction



# PBH could be all of the DM

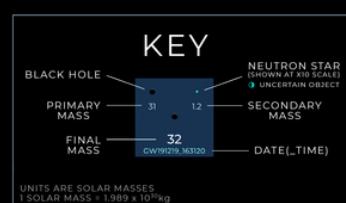
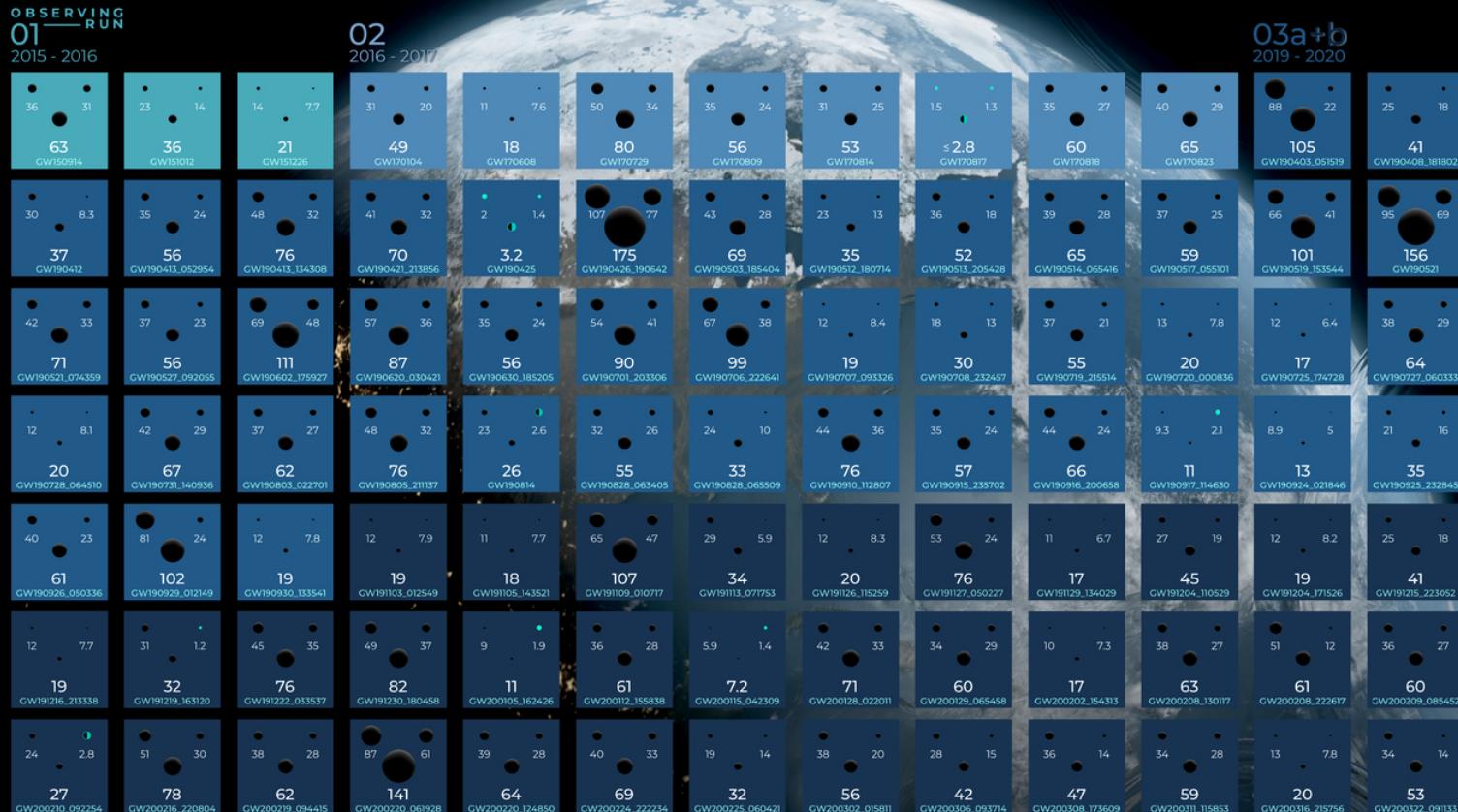


Cappelluti  
Hasinger  
Natarajan  
(2022)

JGB  
Private  
communication

# Gravitational Waves

# GWTC-3 LVK Coll. (2022)



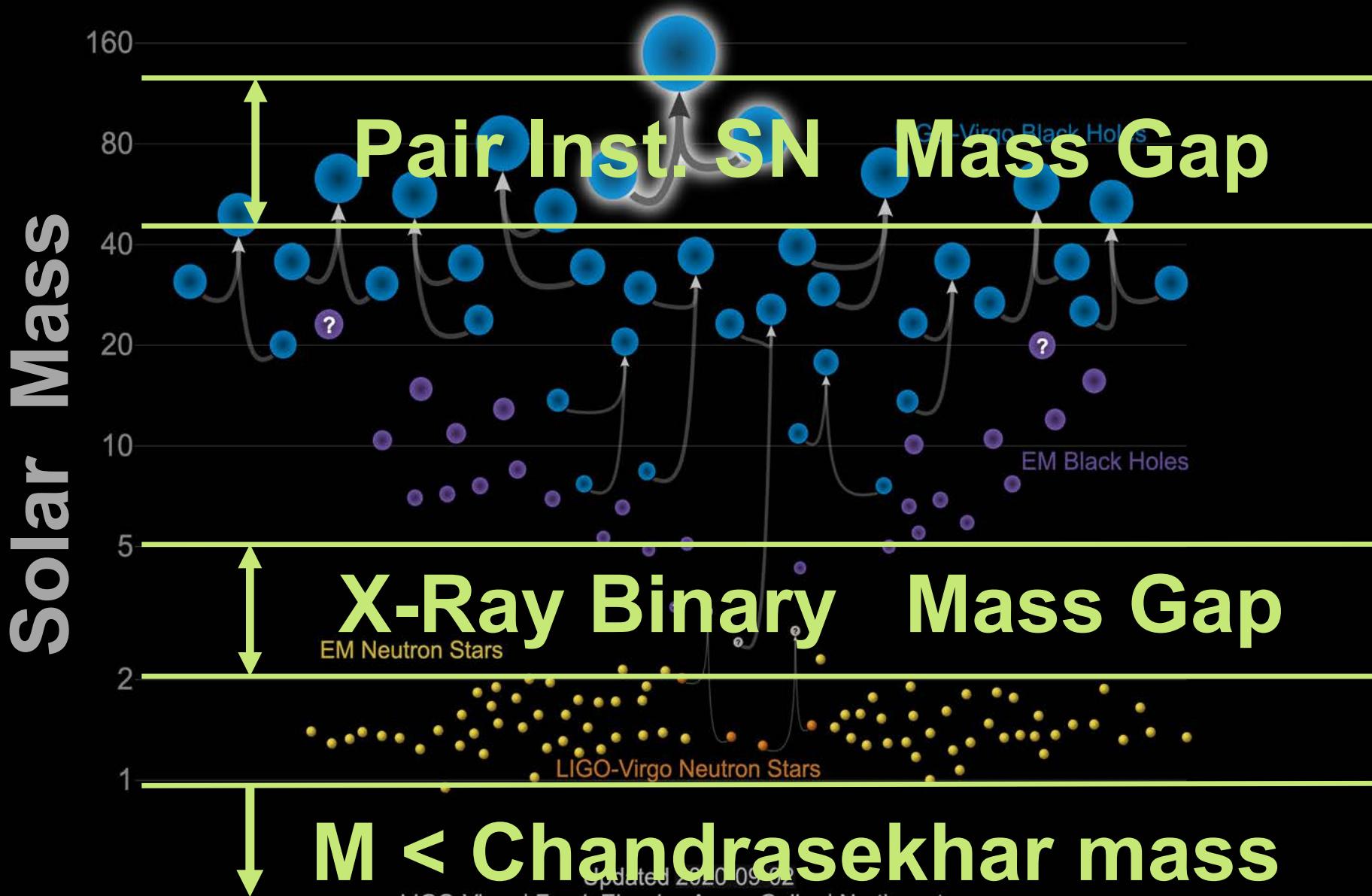
GRAVITATIONAL WAVE  
**MERGER**  
DETECTIONS  
SINCE 2015

OzGrav

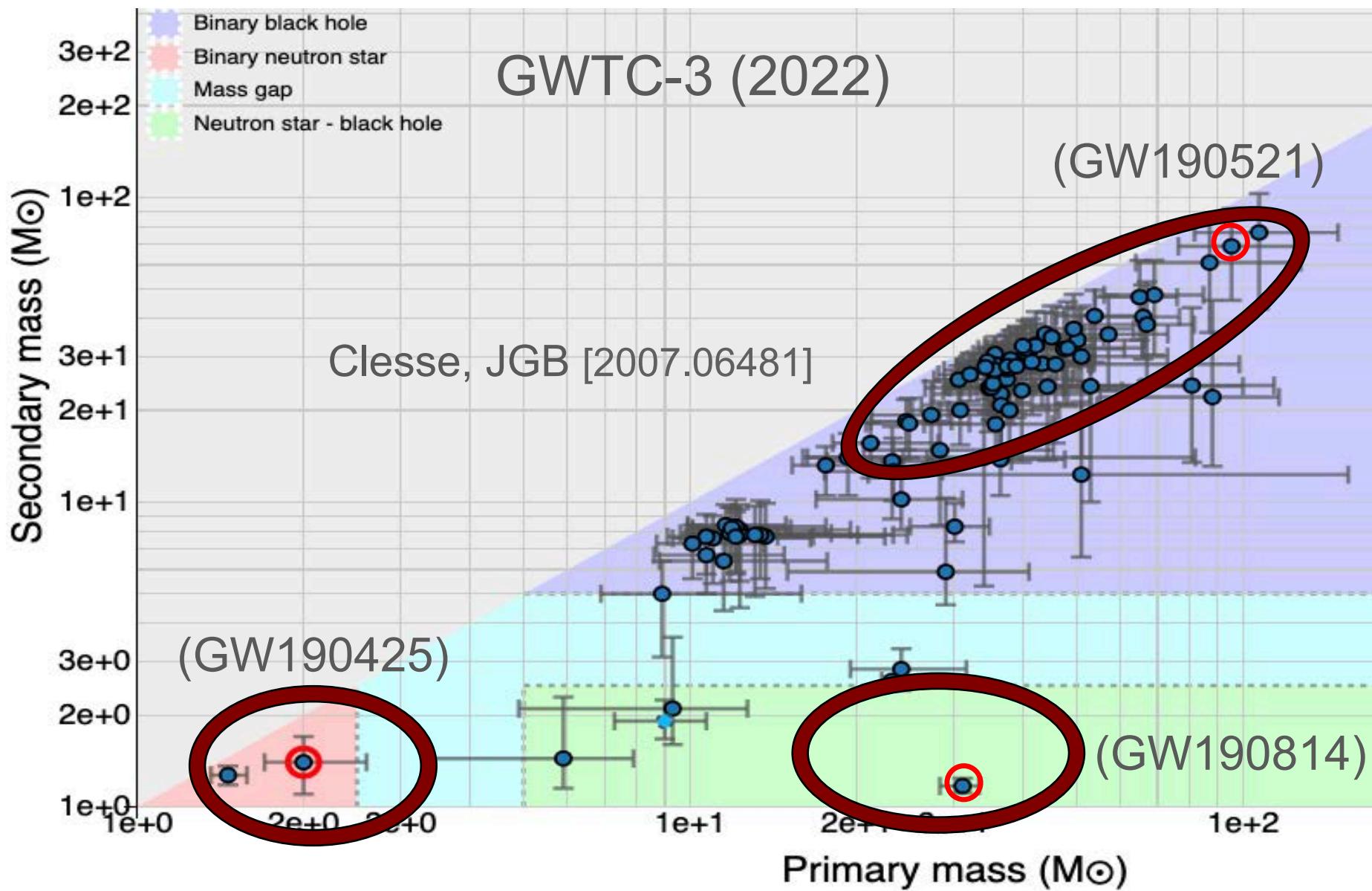
AAC Centre of Excellence for Gravitational Wave Discovery



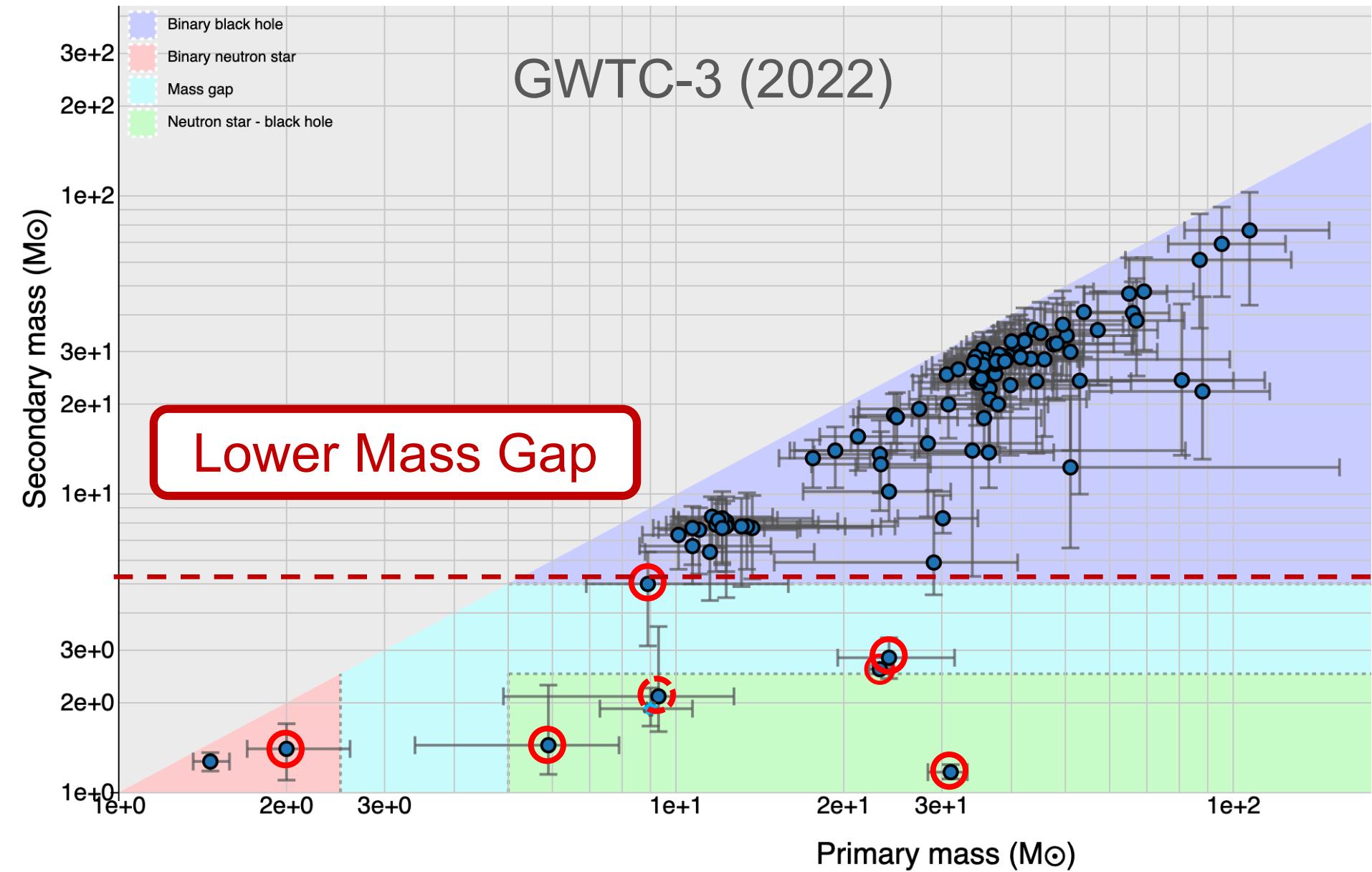
# Black Holes and Neutron Stars



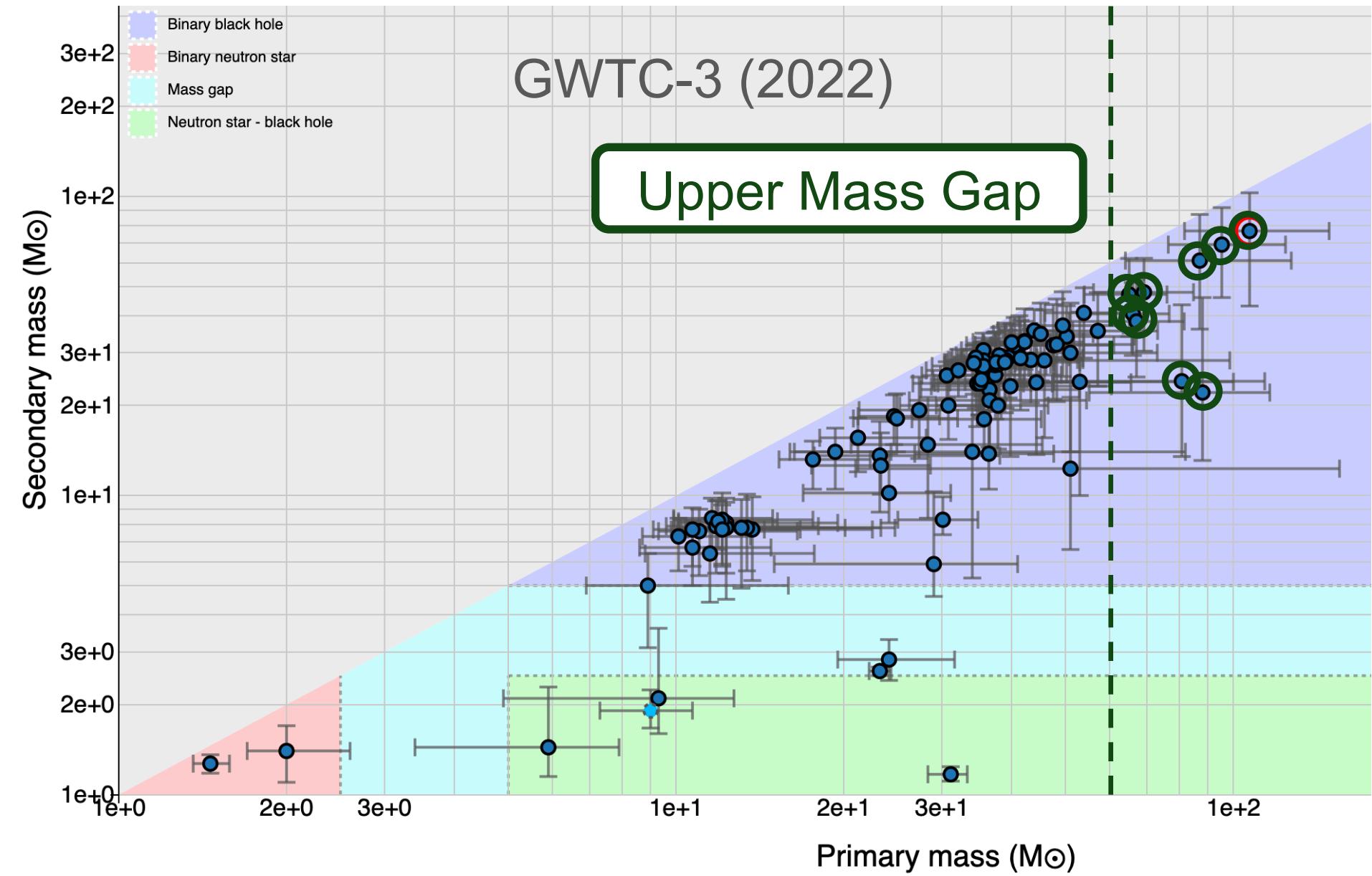
# Primary and secondary masses



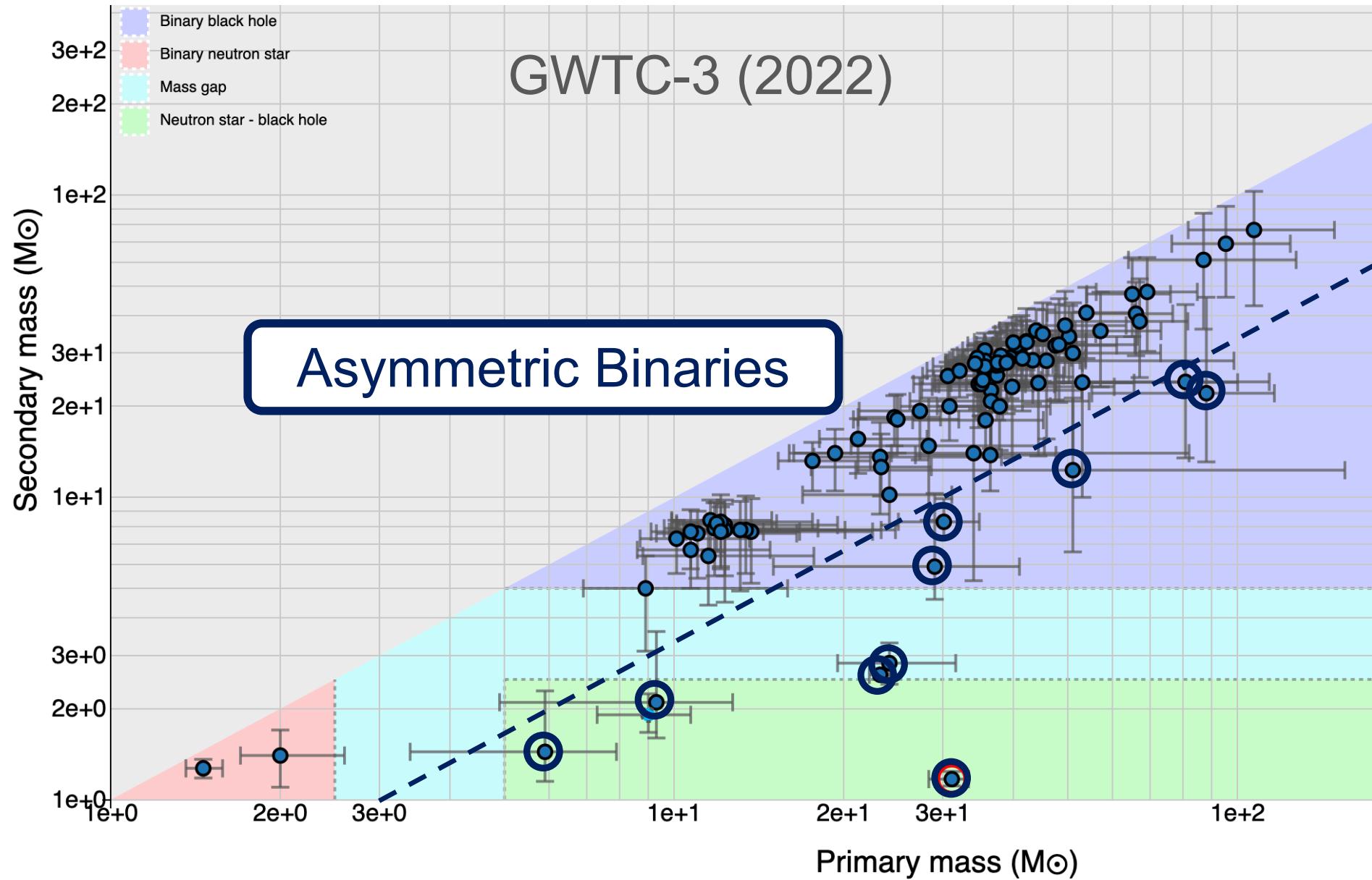
# Are LIGO/Virgo BH Primordial?



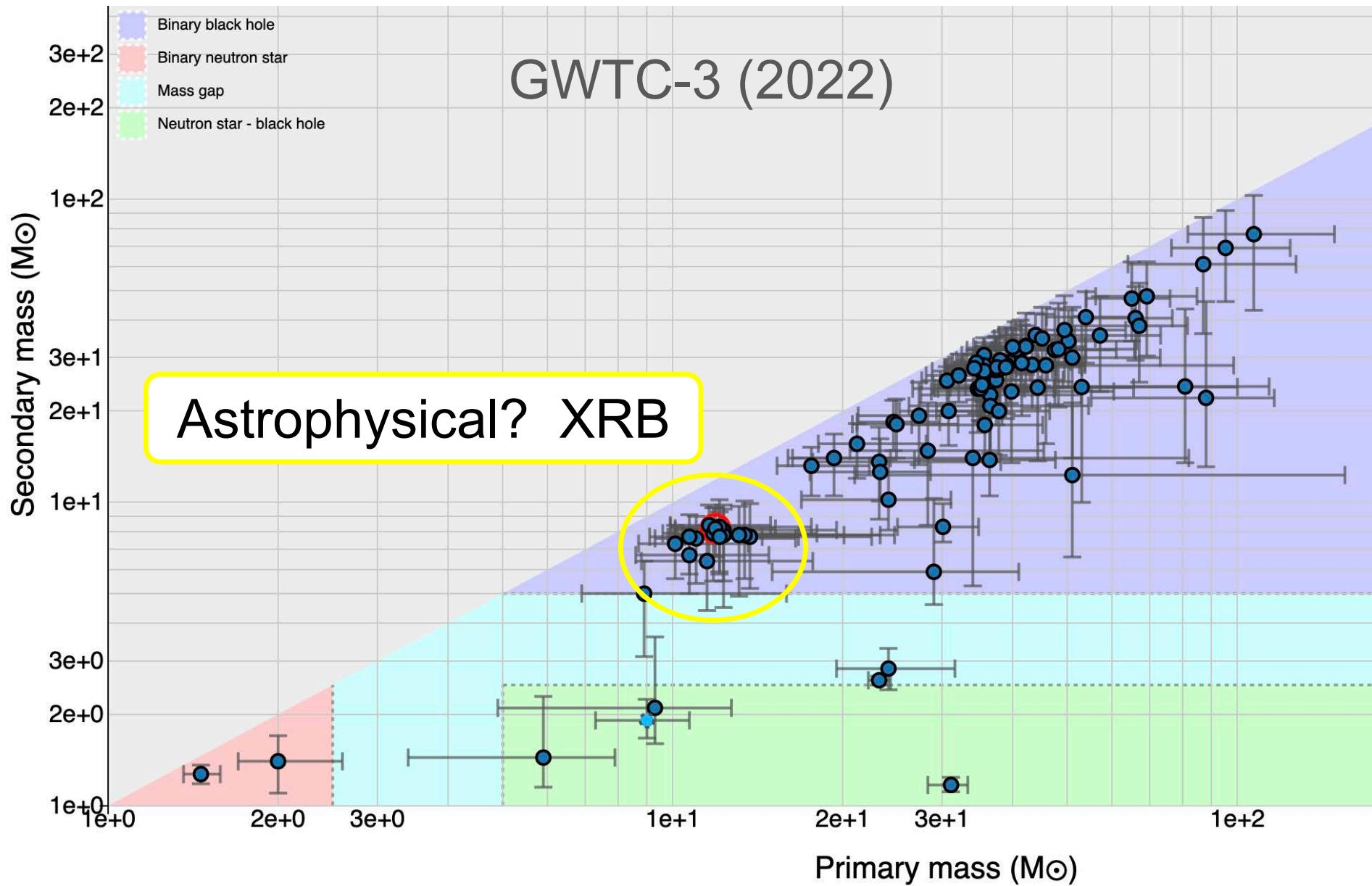
# Are LIGO/Virgo BH Primordial?



# Are LIGO/Virgo BH Primordial?

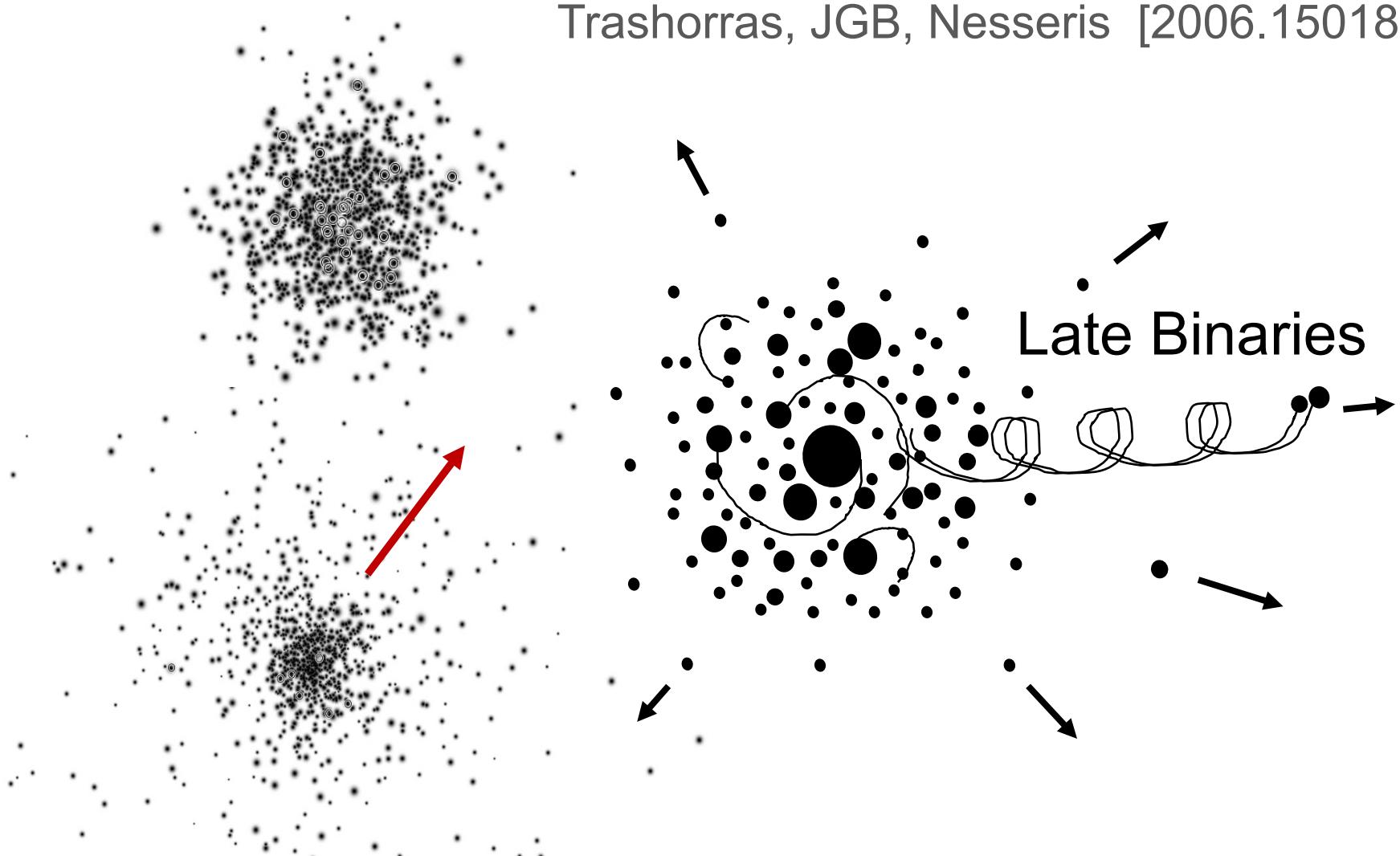


# Are LIGO/Virgo BH Primordial?

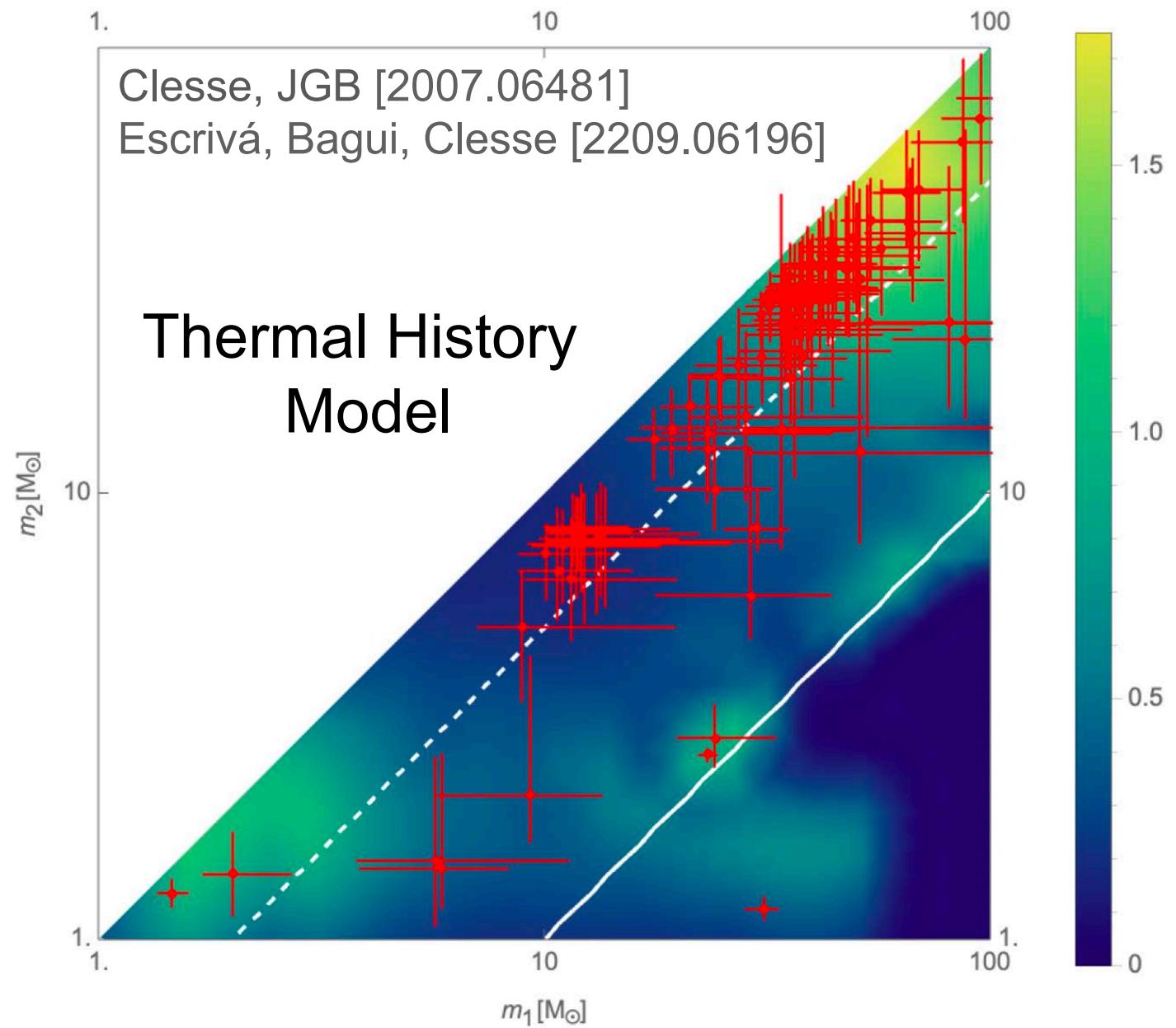


# PBH clusters' merger rates

Trashoras, JGB, Nesseris [2006.15018]

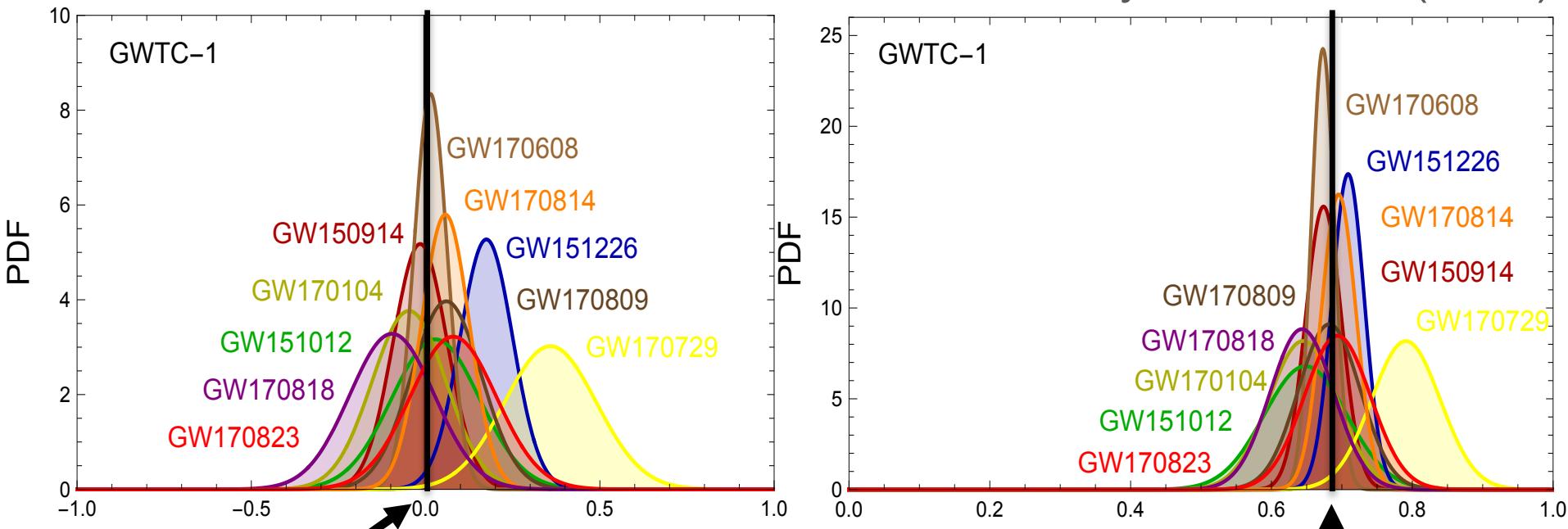


# Are LIGO/Virgo BH Primordial?



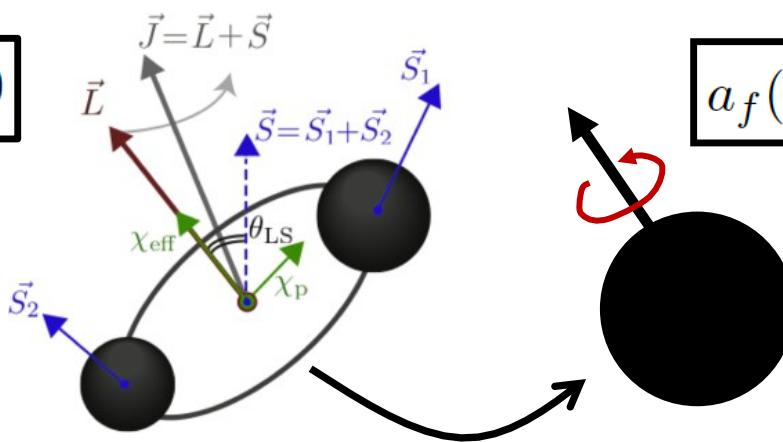
# Effective and Final Spin

JGB – Phil.Trans.Roy.Soc.A 0091 (2019)



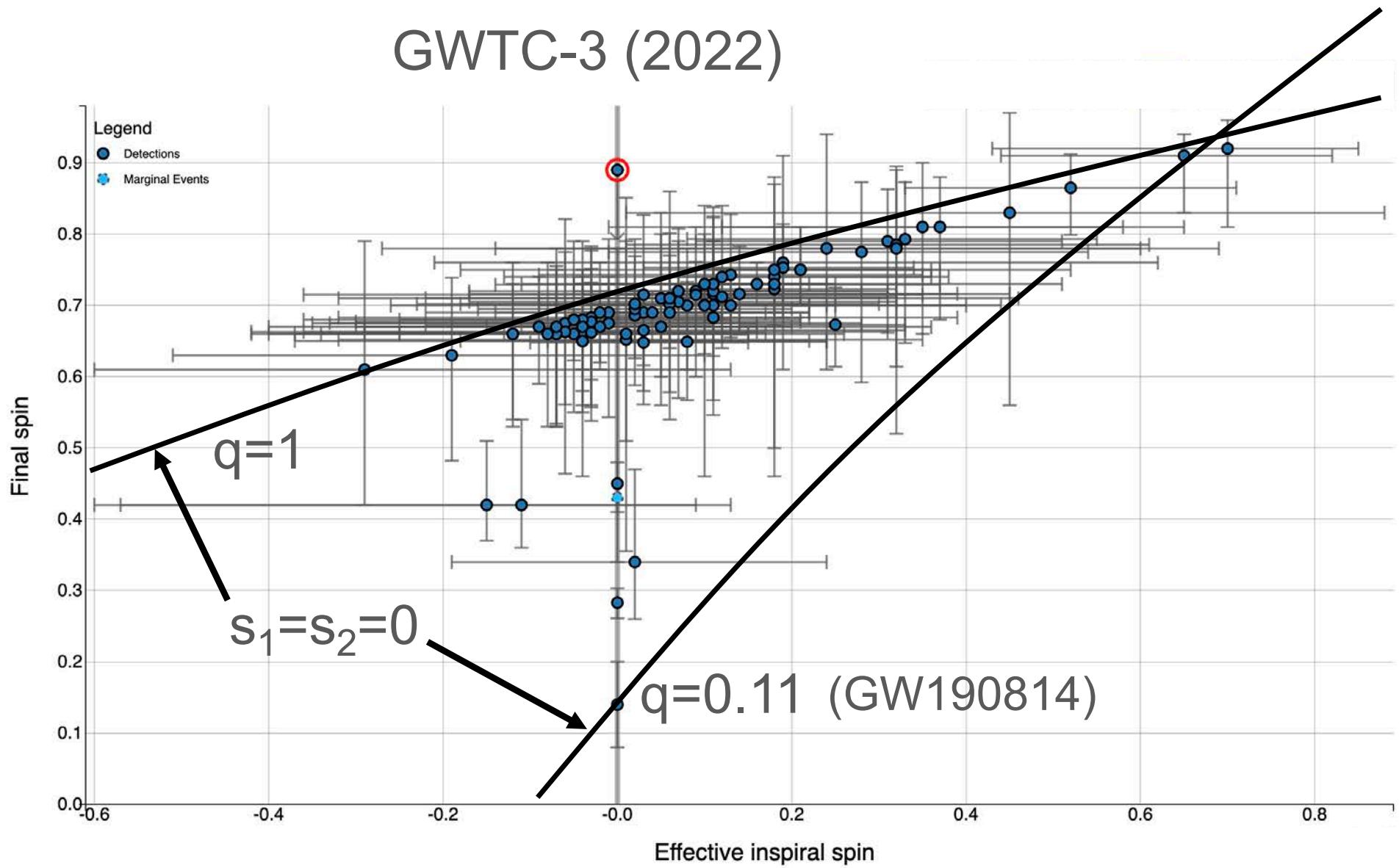
$$\chi_{\text{eff}}(S_1 = S_2 = 0) = 0$$

$$a_f(S_1 = S_2 = 0) = 0.686$$



# Effective and Final Spin

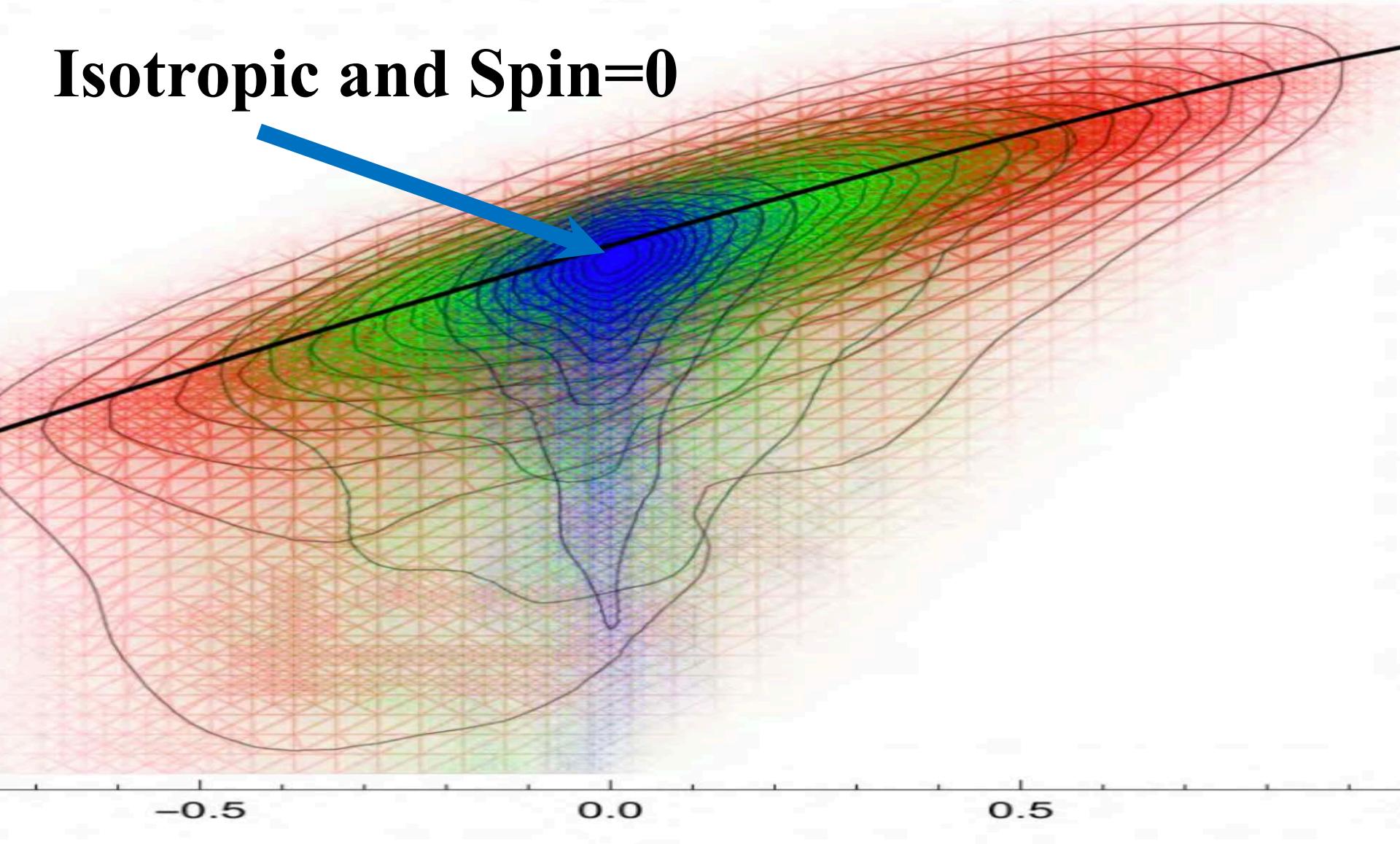
GWTC-3 (2022)



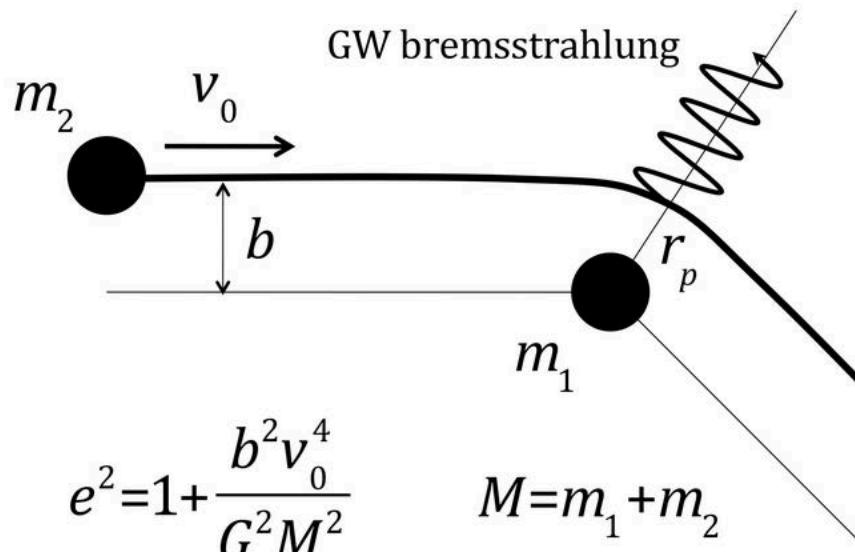
# Effective and Final Spin

JGB, Nuño-Siles, Ruiz Morales [2010.13811]

Isotropic and Spin=0



# Spin induction in dense clusters



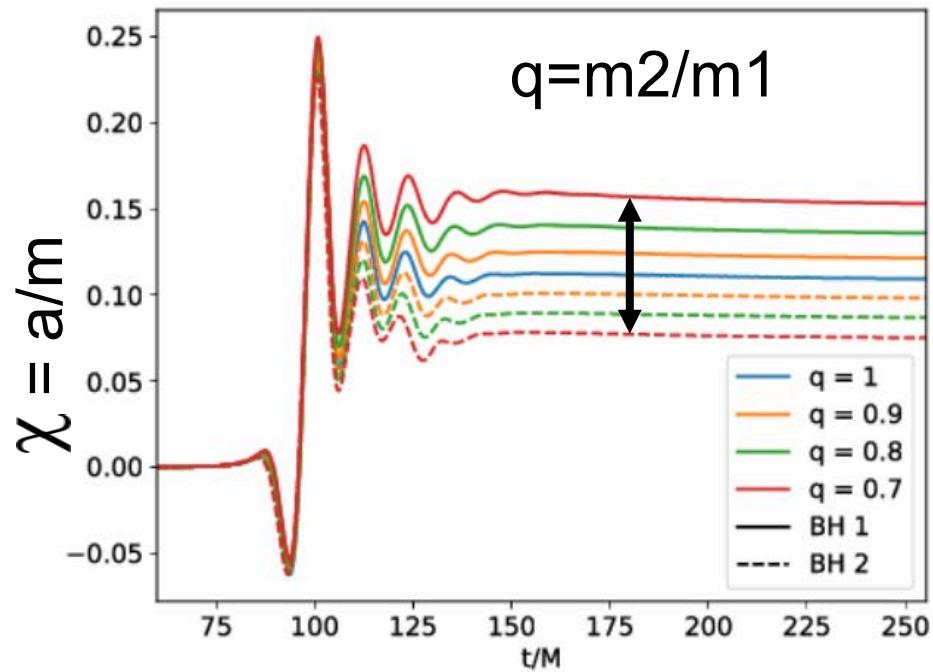
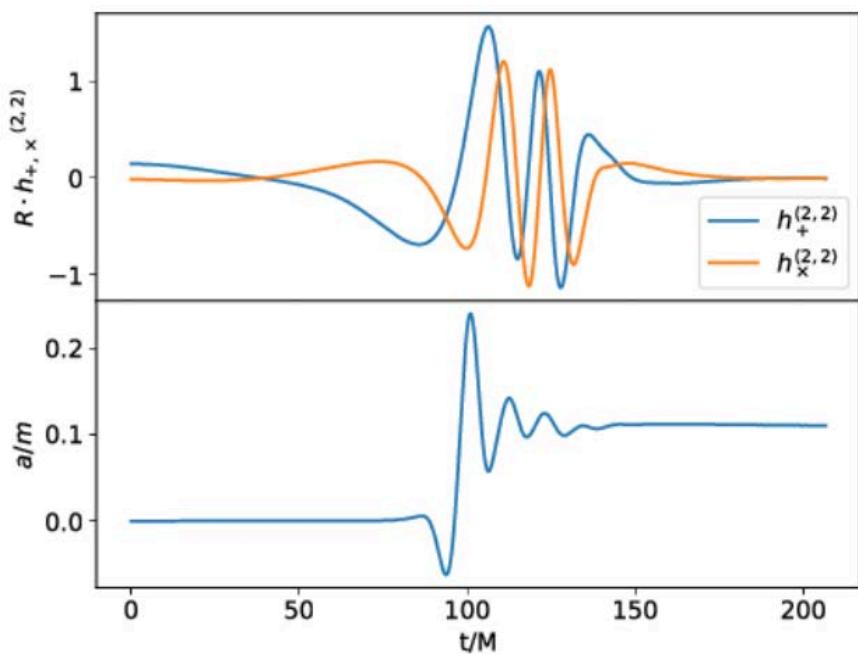
$$e^2 = 1 + \frac{b^2 v_0^4}{G^2 M^2}$$

$$M = m_1 + m_2$$

JGB, Nesseris [1706.02111]  
“”  
[1711.09702]

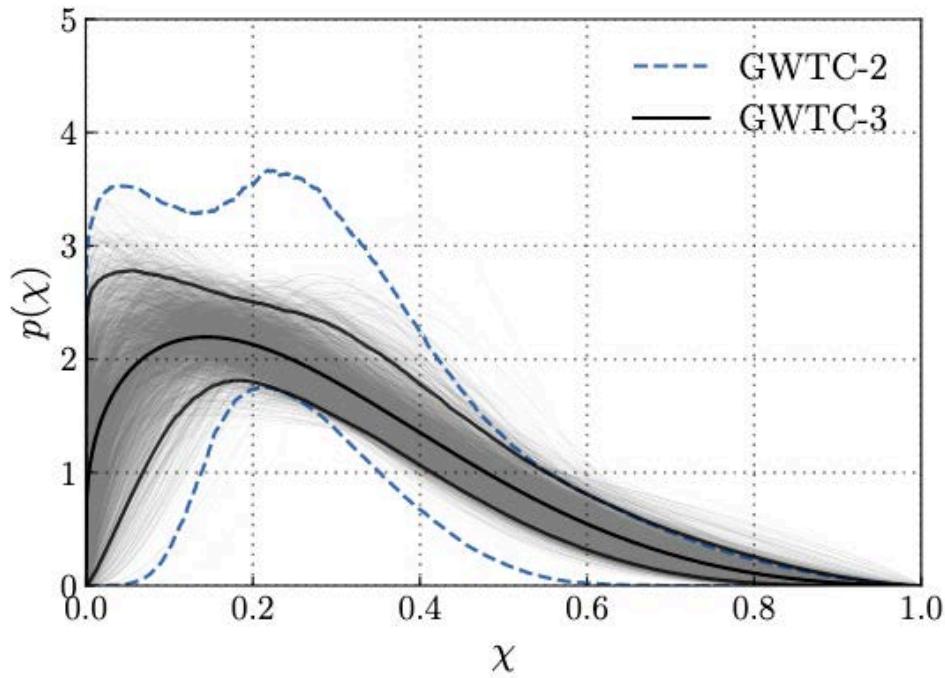
Hyperbolic Encounters  
(GW bursts)

Jaraba, JGB [2106.01436]

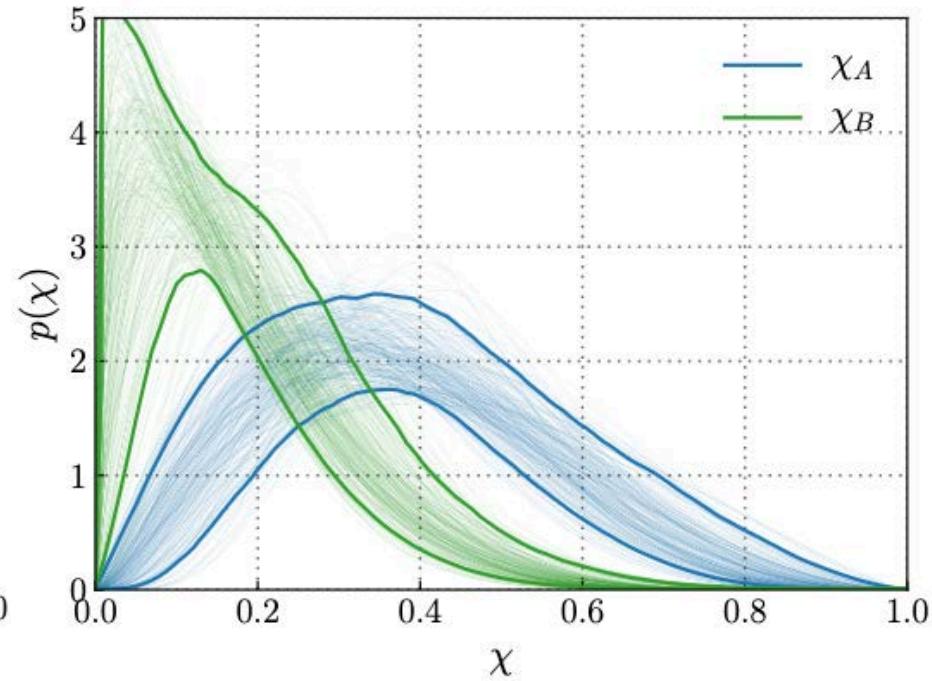


# Spin distributions GWTC-3

LVK Collaboration [2111.03634]



All component spins  $\chi_1$  and  $\chi_2$



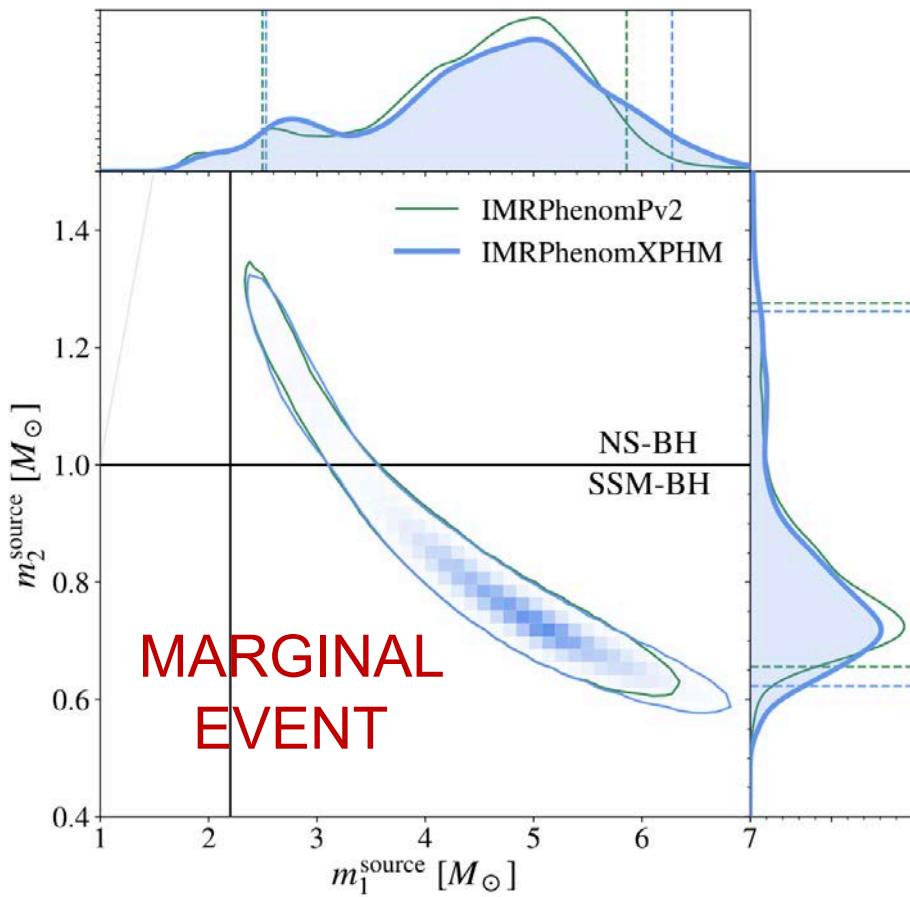
$$\chi_A = \max_{|\chi|} (\chi_1, \chi_2)$$

$$\chi_B = \min_{|\chi|} (\chi_1, \chi_2)$$

# Are LIGO/Virgo BH Primordial?

SSM170401

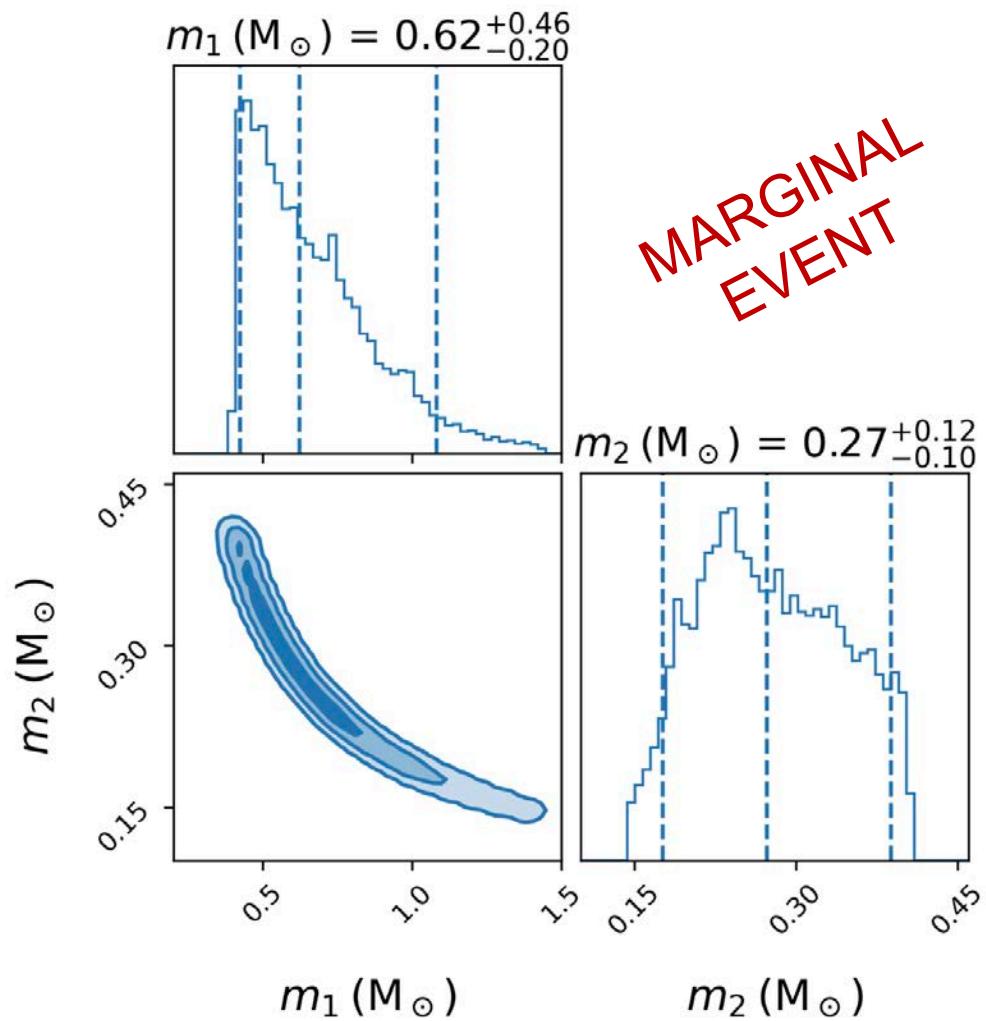
Morras et al. [2301.11619]



Parameter	IMRPhenomPv2	IMRPhenomXPHM
Signal to Noise Ratio	$7.98^{+0.62}_{-1.03}$	$7.94^{+0.70}_{-1.05}$
Primary mass ( $M_{\odot}$ )	$4.65^{+1.21}_{-2.15}$	$4.71^{+1.57}_{-2.18}$
Secondary mass ( $M_{\odot}$ )	$0.77^{+0.50}_{-0.12}$	$0.76^{+0.50}_{-0.14}$
Primary spin magnitude	$0.32^{+0.47}_{-0.26}$	$0.36^{+0.46}_{-0.30}$
Secondary spin magnitude	$0.48^{+0.46}_{-0.43}$	$0.47^{+0.46}_{-0.42}$
Total mass ( $M_{\odot}$ )	$5.42^{+1.10}_{-1.65}$	$5.47^{+1.43}_{-1.68}$
Mass ratio ( $m_2/m_1 \leq 1$ )	$0.17^{+0.34}_{-0.05}$	$0.16^{+0.34}_{-0.06}$
$\chi_{\text{eff}}$ [51, 52]	$-0.06^{+0.17}_{-0.32}$	$-0.05^{+0.22}_{-0.35}$
$\chi_p$ [53]	$0.28^{+0.34}_{-0.21}$	$0.33^{+0.33}_{-0.26}$
Luminosity Distance (Mpc)	$119^{+82}_{-48}$	$124^{+82}_{-48}$
Redshift	$0.028^{+0.018}_{-0.010}$	$0.028^{+0.017}_{-0.011}$
Ra (°)	$-2^{+34}_{-35}$	$-1^{+34}_{-37}$
Dec (°)	$47^{+14}_{-26}$	$46^{+14}_{-29}$
Final mass ( $M_{\odot}$ )	$5.34^{+1.11}_{-1.70}$	$5.40^{+1.45}_{-1.73}$
Final spin	$0.39^{+0.24}_{-0.07}$	$0.42^{+0.22}_{-0.10}$
$P(m_2 < 1 M_{\odot})$	85%	84%

# Are LIGO/Virgo BH Primordial?

SSM200308

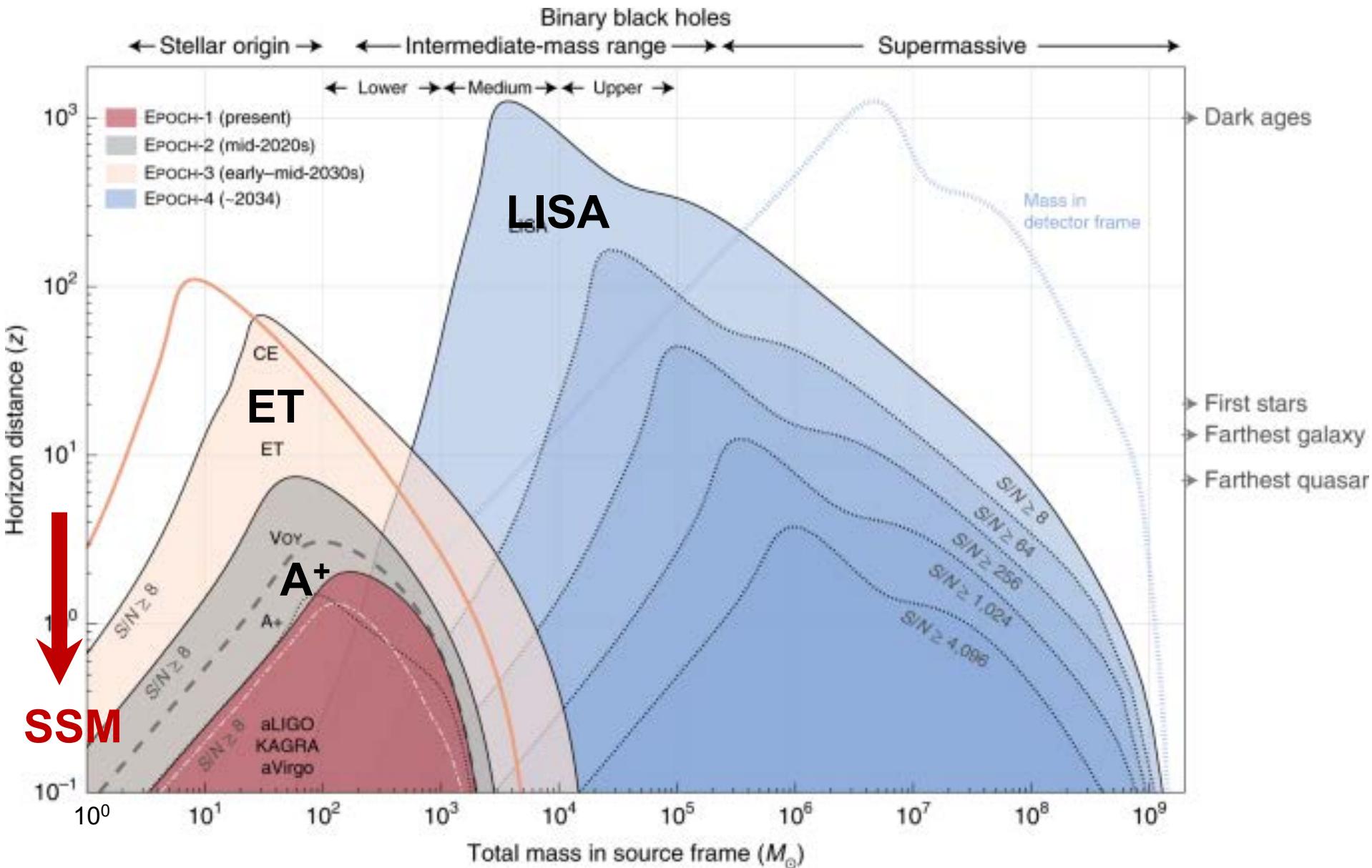


Prunier et al. [2311.16085]

## Parameter

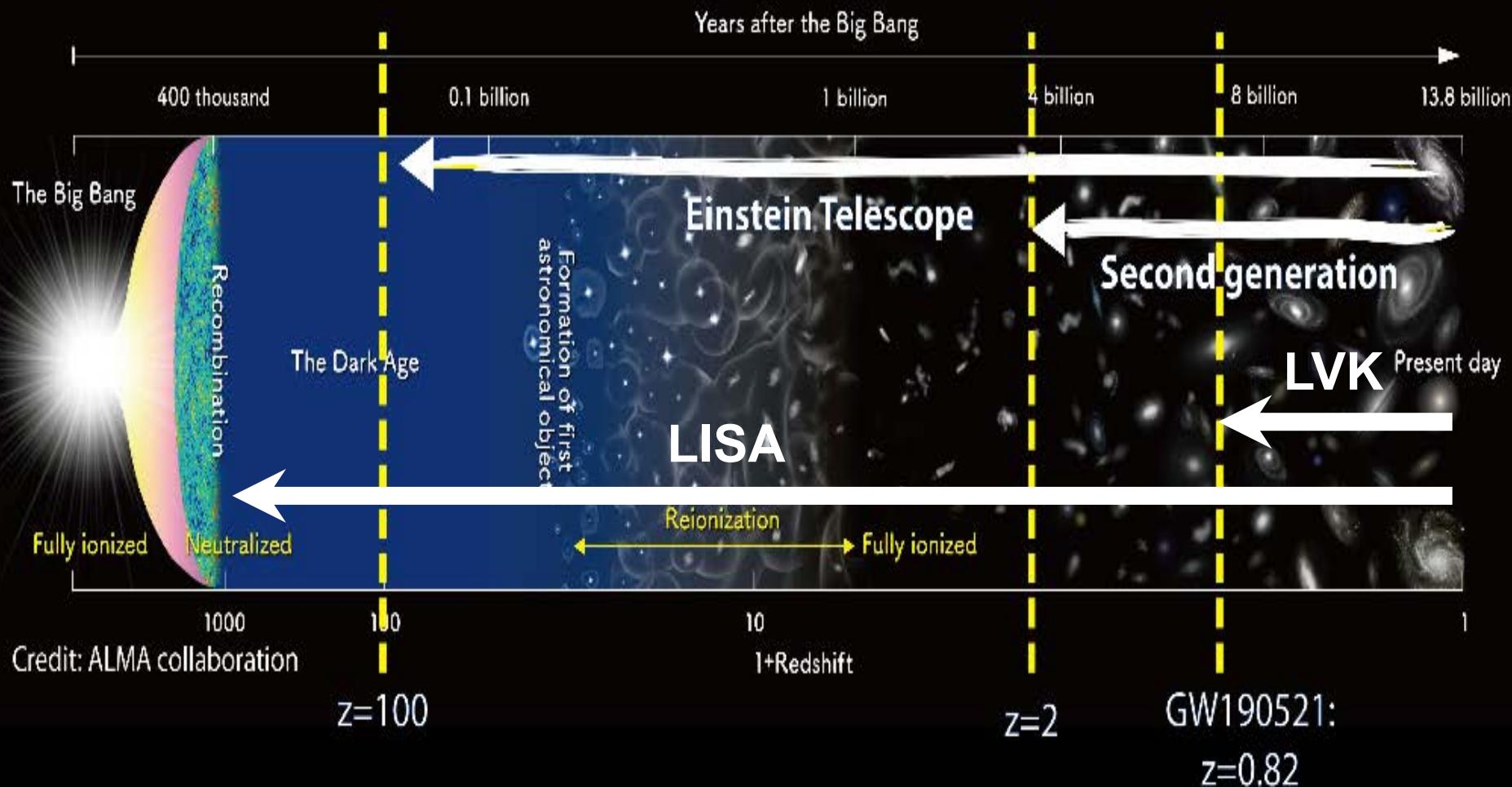
Matched Filter SNR	$8.02^{+0.49}_{-0.85}$
Primary mass ( $M_\odot$ )	$0.62^{+0.46}_{-0.20}$
Secondary mass ( $M_\odot$ )	$0.27^{+0.12}_{-0.10}$
Primary spin magnitude	$0.66^{+0.13}_{-0.25}$
Secondary spin magnitude	$0.44^{+0.33}_{-0.39}$
Total mass ( $M_\odot$ )	$0.88^{+0.35}_{-0.08}$
Detector-frame chirp mass ( $M_\odot$ )	$0.3527^{+0.0003}_{-0.0001}$
Mass ratio ( $m_2/m_1 \leq 1$ )	$0.44^{+0.48}_{-0.28}$
$\chi_{\text{eff}}$ [27, 28]	$0.41^{+0.08}_{-0.04}$
$\chi_p$ [29]	$0.37^{+0.24}_{-0.24}$
Luminosity Distance (Mpc)	$90^{+43}_{-39}$
Redshift	$0.02^{+0.01}_{-0.01}$
$P(m_1 < 1 M_\odot)$	92%
$P(m_2 < 1 M_\odot)$	100%

# BBH sensitivity in future G3 GW



# The future of GW (G3)

Detection horizon for black-hole binaries



# Conclusions

- Quantum diffusion inevitably generates PBH
- Thermal history predicts PBH with multimodal mass distribution  $\sim 10^{-5}, 1, 100, 10^5 M_\odot$  ( $10^{-10} M_\odot$  also?)
- The predicted PBH spin and mass distribution has been measured by LIGO/Virgo + OGLE/Gaia around  $1-100 M_\odot$  (features: peak & plateau)
- Other peaks could be explored with LSST microlensing
- PBH scenario can explain various cosmic conundra
- Paradigm shift in Structure Formation of the Universe
- Very rich phenomenology: multiscale, multiepoch, multiprobe => Future G3 detectors (ET, CE, LISA)