



# Quantum Gravity in LAB

Andrea Addazi,  
College of Physics, Sichuan University  
INFN LNFN (Italy)

Summer Conferences 2023

# Based on a series of recent works

A. Addazi, P. Belli, R. Bernabei, A. Marciano,  
arXiv:1712.08082, CPC

A. Addazi, A. Marciano, arXiv:1811.06425, IJMPA 2019

A. Addazi, R. Bernabei, MPLA 2019

A. Addazi, H. Shababi, arXiv: 2005.14000v1, IJGMPA

A. Addazi, P. Belli, R. Bernabei, A. Marciano, H. Shababi,  
*Eur.Phys.J.C* 80 (2020) 8, 795

K. Pisticchia et al, arXiv:2209.00074, Phys.Rev.Letters, PRD,  
MDPI

# “Santo Graal” of Theoretical Physics

## Quantum Gravity!

UV completion of General Relativity



# Top-Down QG

String theory, M-theory

Super-renormalizable non-local theories

Loop Quantum Gravity

Asymptotic Safety

Causal Sets

Asymptotic Darkness/Classicalization

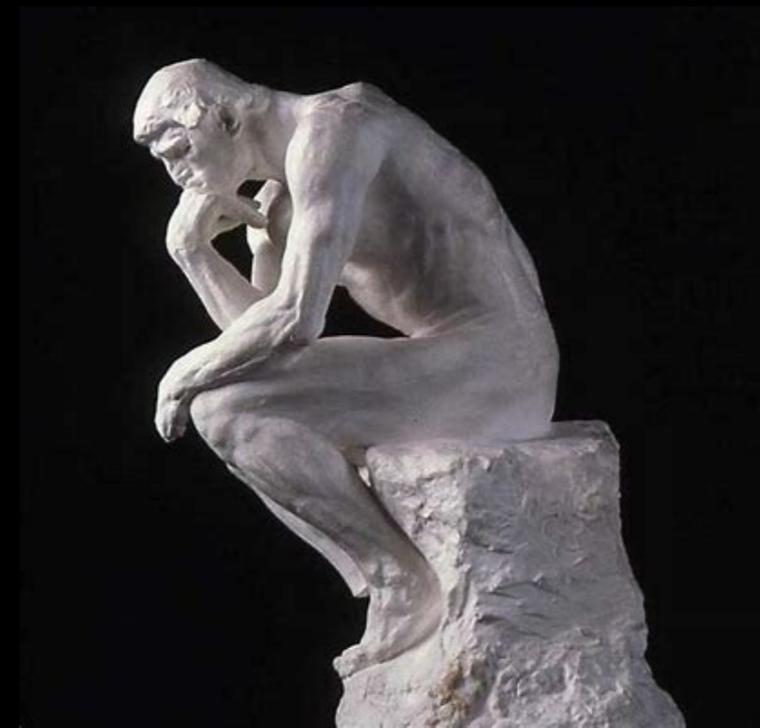
Dynamical Triangulation

Gauge reformulations of gravity

Some of the previous theories may be “dual”  
of having common hidden theoretical features



Quantum gravity phenomenology is commonly considered as a sort of metaphysics chimera or even an oxymoron... common pessimistic approach



# Bottom-up: QG phenomenology

## Effective theories and parametrization of our “ignorance” on UV completion

Quantum Field Theory in  
Non-commutative space-time;  
Theta- and kappa-Poincare

Higher derivatives actions

Modified Gravity

Quantum Groups

Generalized Uncertainty Principle (GUPs)

Modified Dispersion Relations (MDRs)

Large Extra Dimensions

Lorentz Violations, CPT violations

Decoherence, density matrix

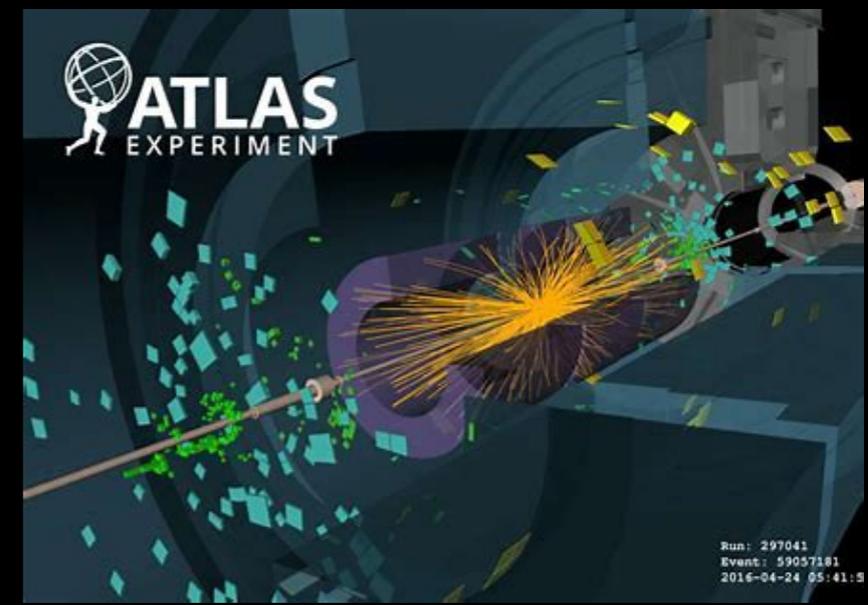
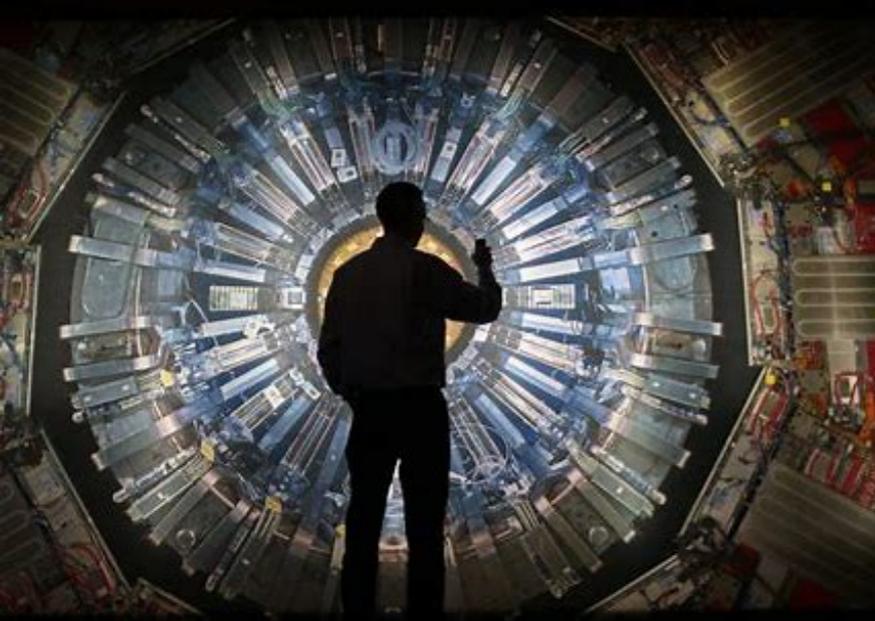
Extended Standard Model

Effective Theory  
*N free parameters*

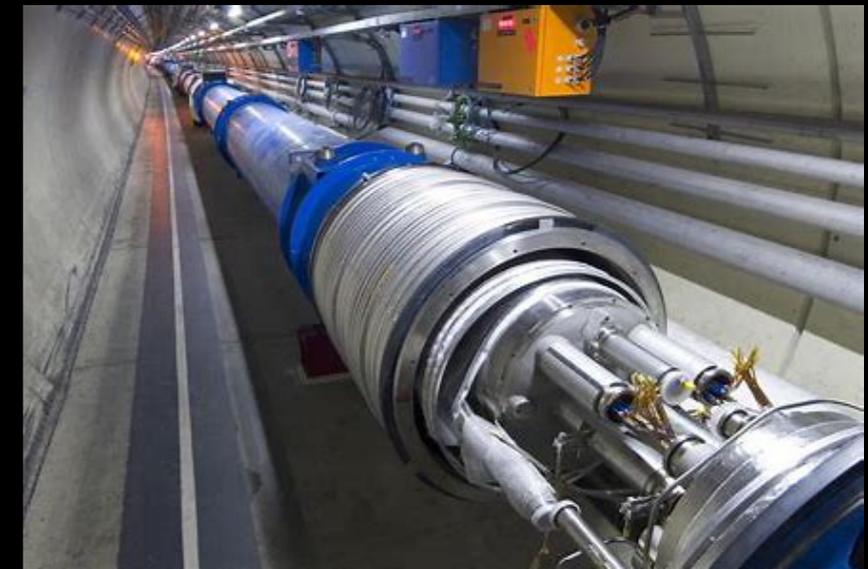
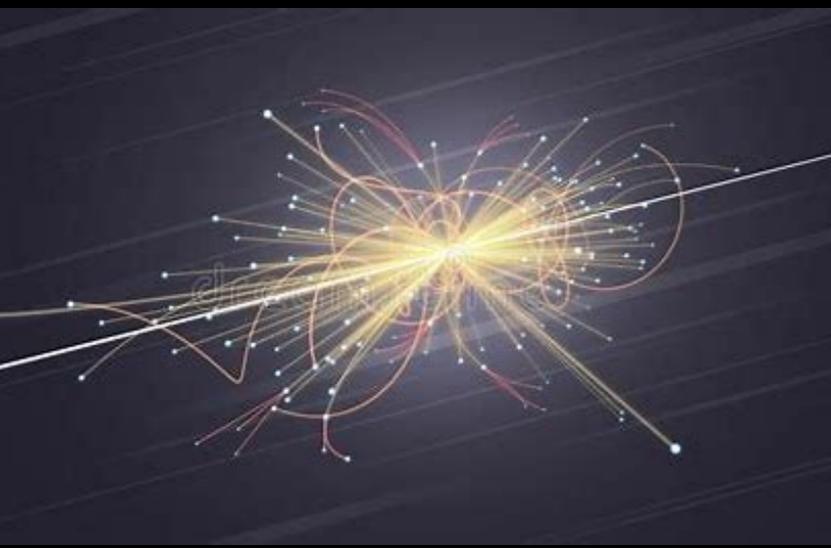
Vs

Low (in Planck unit) energy physics  
Observations



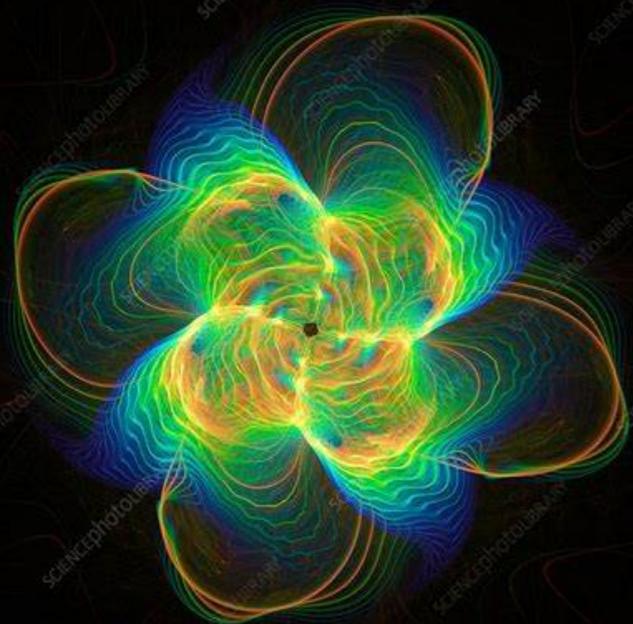


**Direct probe** of Planck scale **impossible** with our current and next future technology (at least if extra dimensions are not fine-tuned to be around  $1-0.0001\text{mm}$ , ADD/RS). Nevertheless tiny residual quantum gravity effects can **survive** at “mesoscopic” scales,  
Lower energy physics.  
This is possible if a “**scale amplifier**”  
Cumulative overall “deviations”





Quantum gravity  
memory lost ...  
And regained...



QG probes in Astrophysics and cosmology,  
multi-messenger physics  
GRBs, AGN, BH-BH mergings,  
NS-NS mergings. MDRs, Horizons,  
Love number etc

*Gamma ray windows, GRBs, AGNs,  
G.Amelino-Camelia, J. Ellis, et al.*



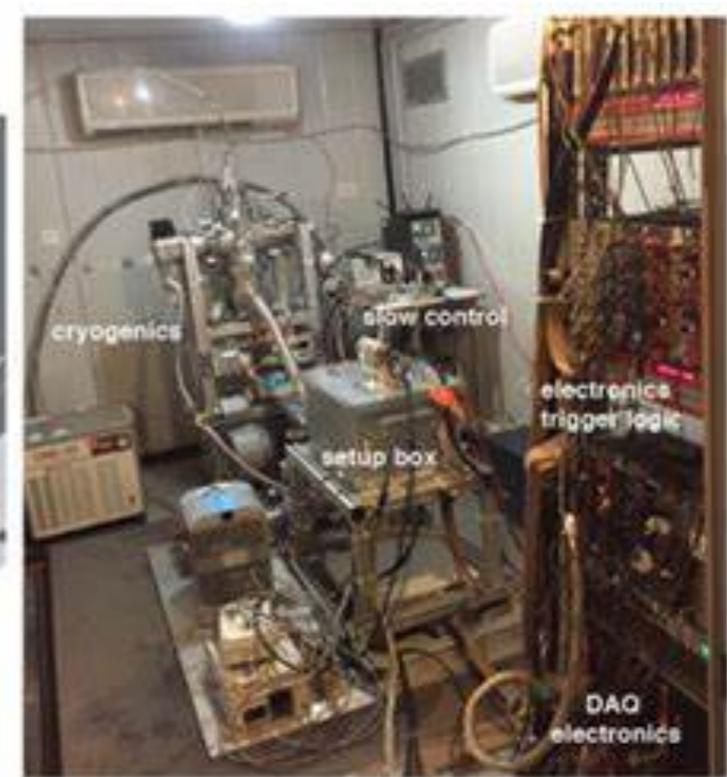
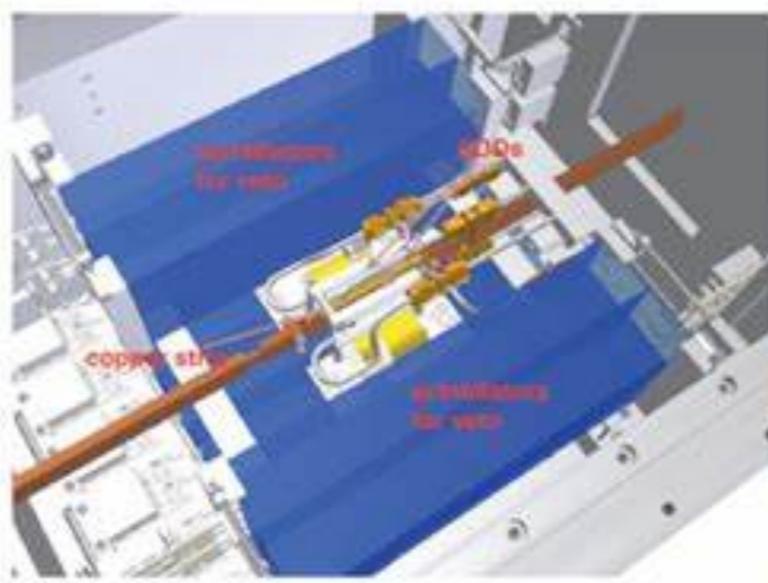
*A. Addazi, N. Yunes,  
A. Marciano PRL highlights 2019*

# Deep Underground Experiments!

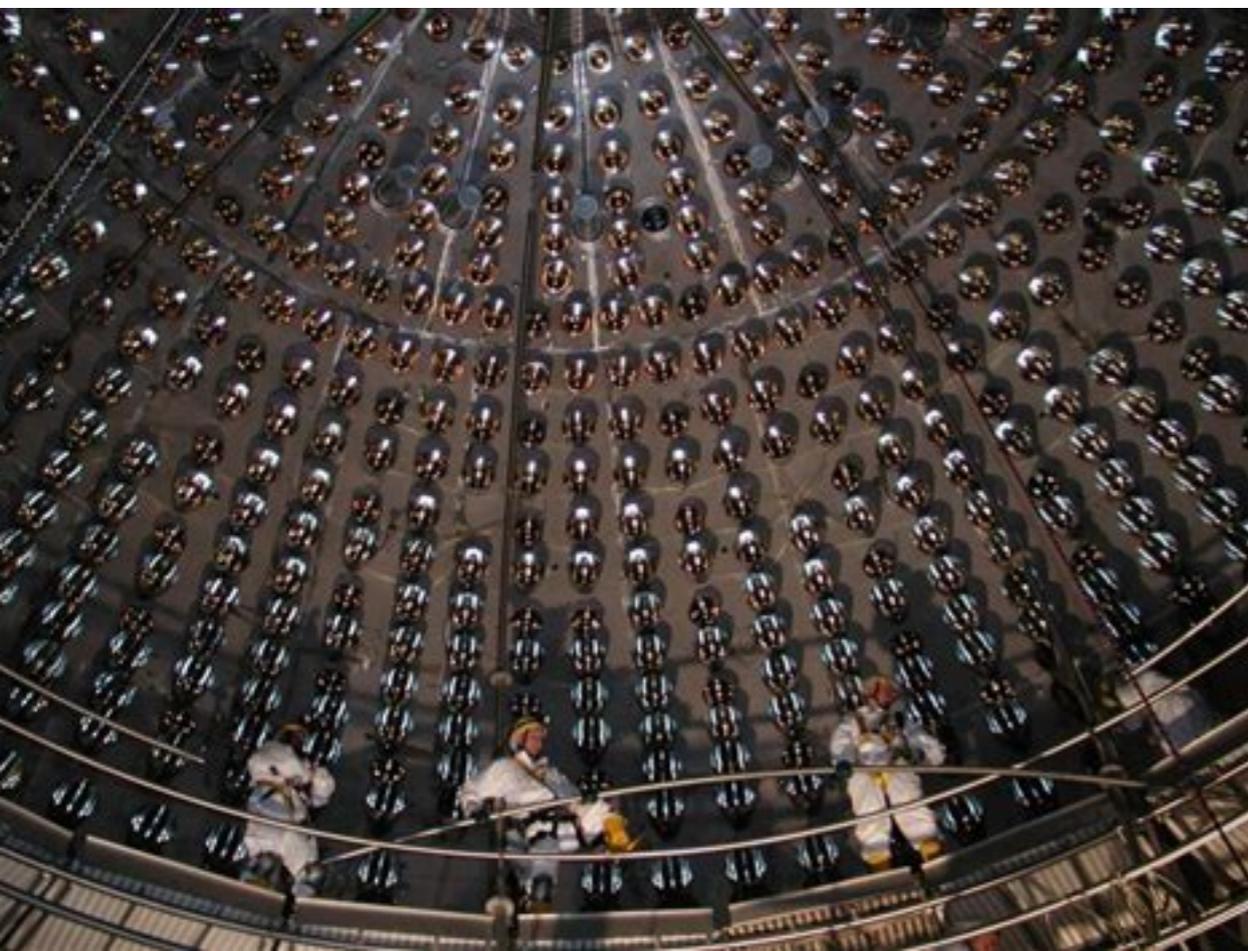
# Gran Sasso National Laboratory INFN



VIP-II



BOREXINO



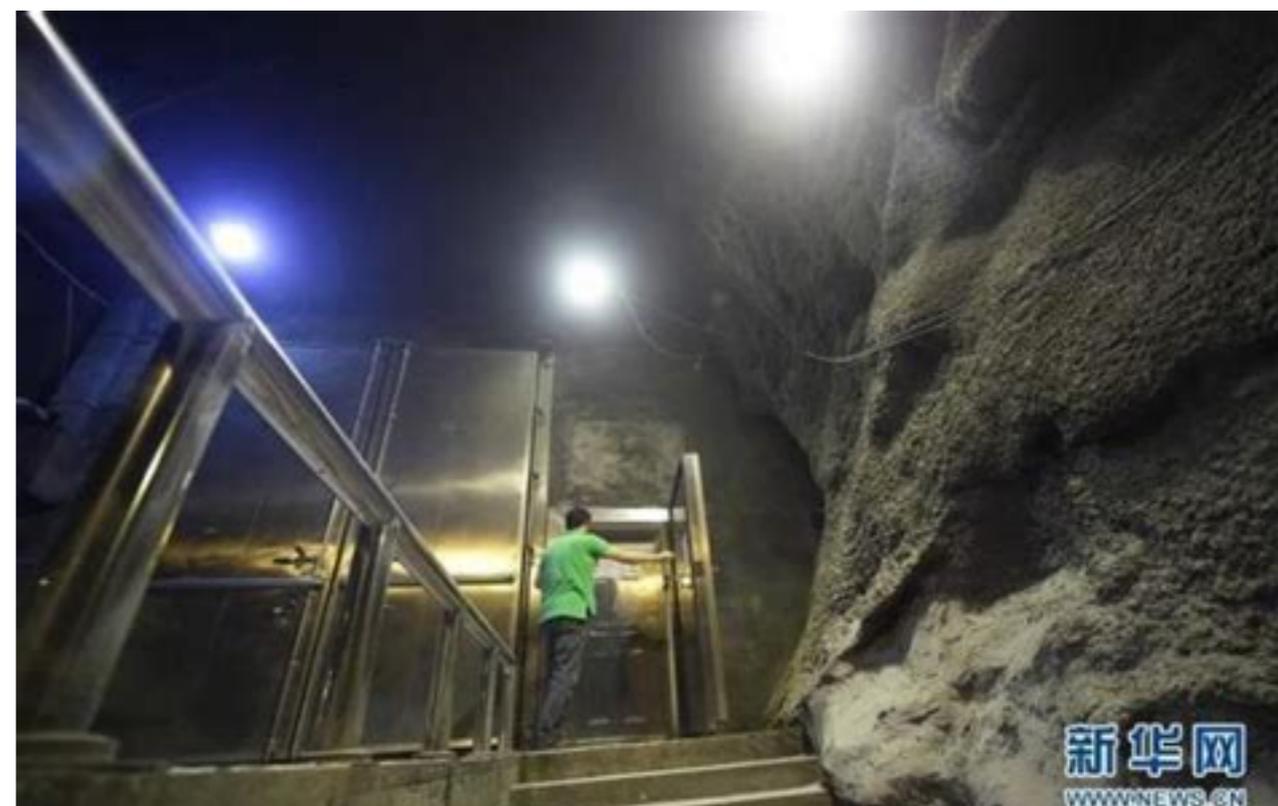
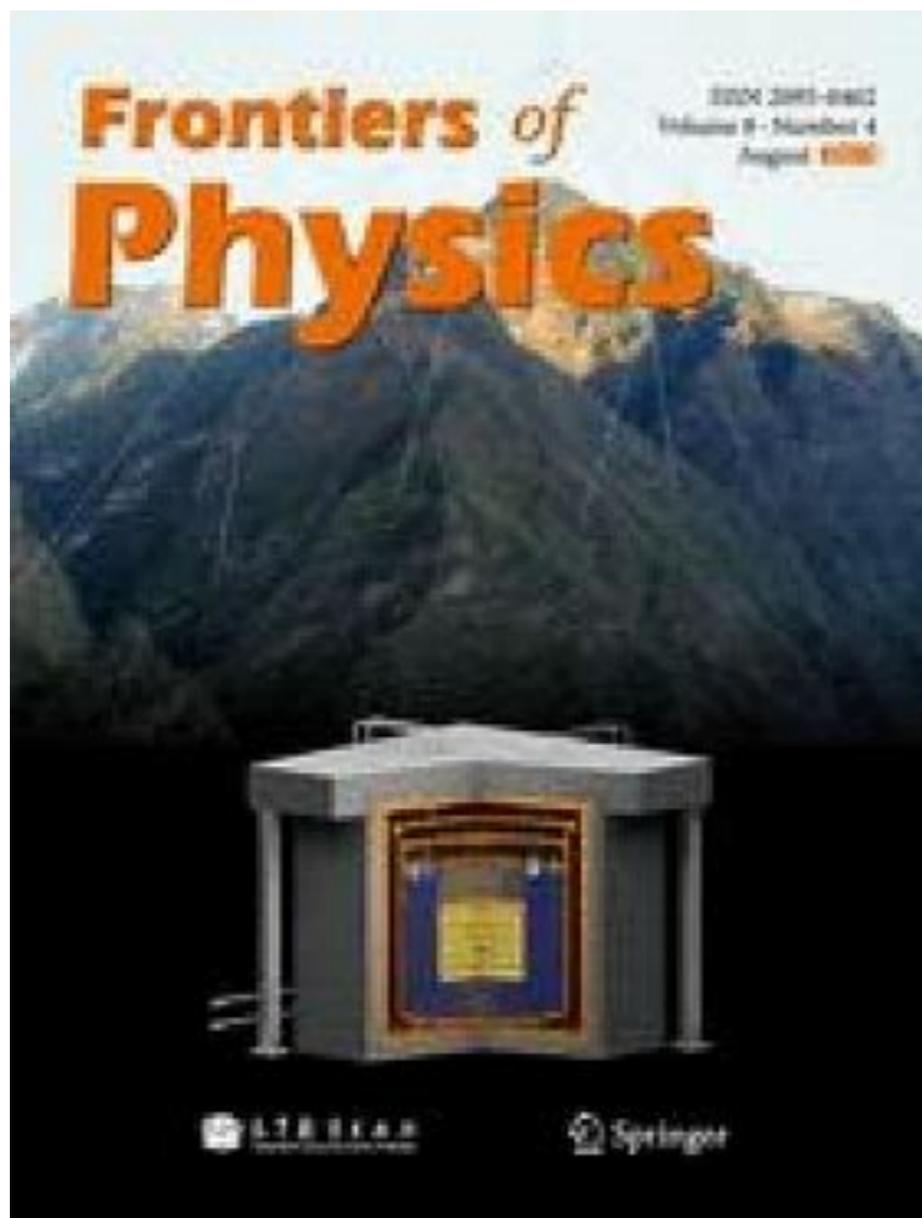
(a)

(b)

DAMA-LIBRA



# CDEX, PANDA-X for Dark Matter searches



# The “power” of underground experiments

Large Statistics and Data taking

Low and Controllable Background

High precision atomic physics

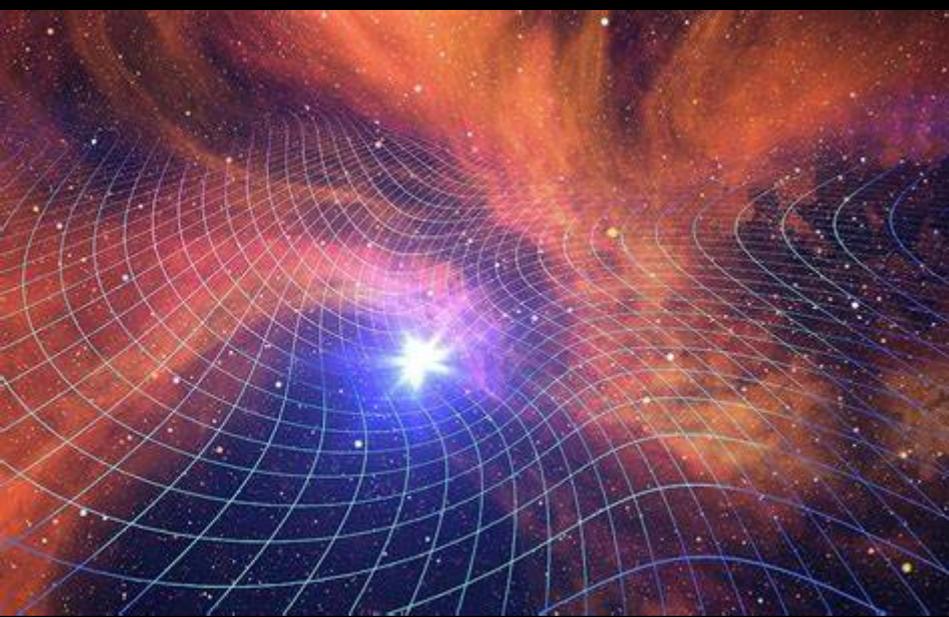
A multitude of techniques:  
Different nuclei and atoms,  
Typical energy scales, temperature,  
Crystals, liquid, double phases etc

# Pauli Spin Statistics Theorem

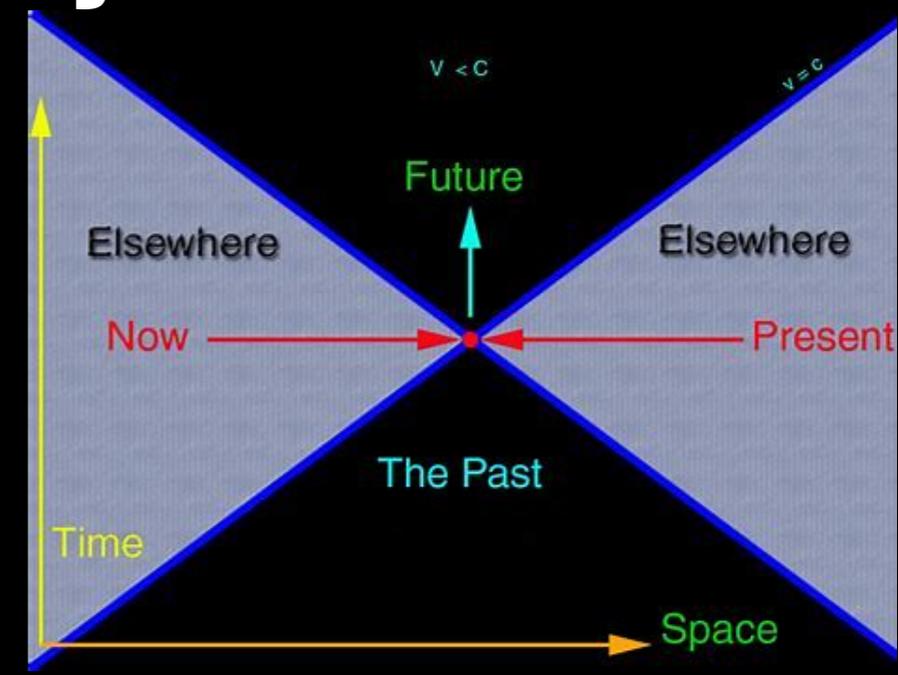
**Fermions:**  
**spin  $1/2$**

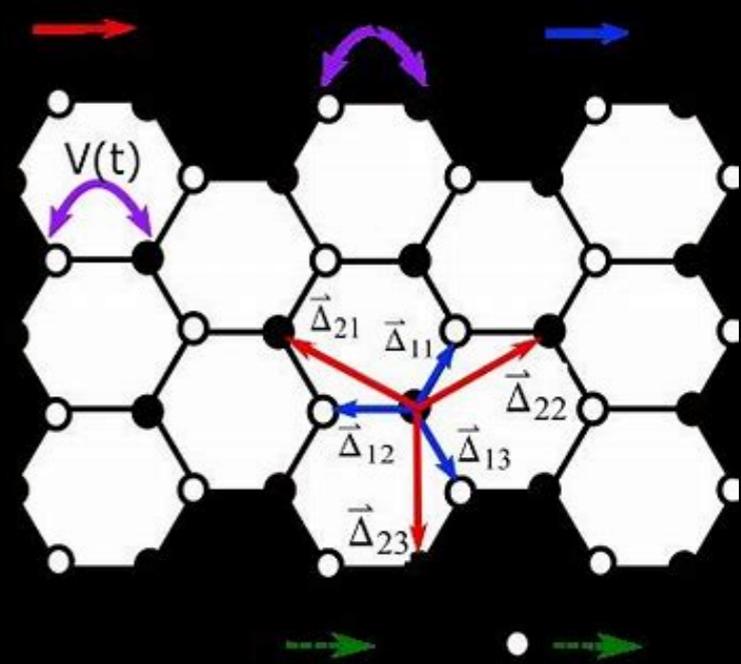
**Bosons:**  
**integer spin  $0, 1$**



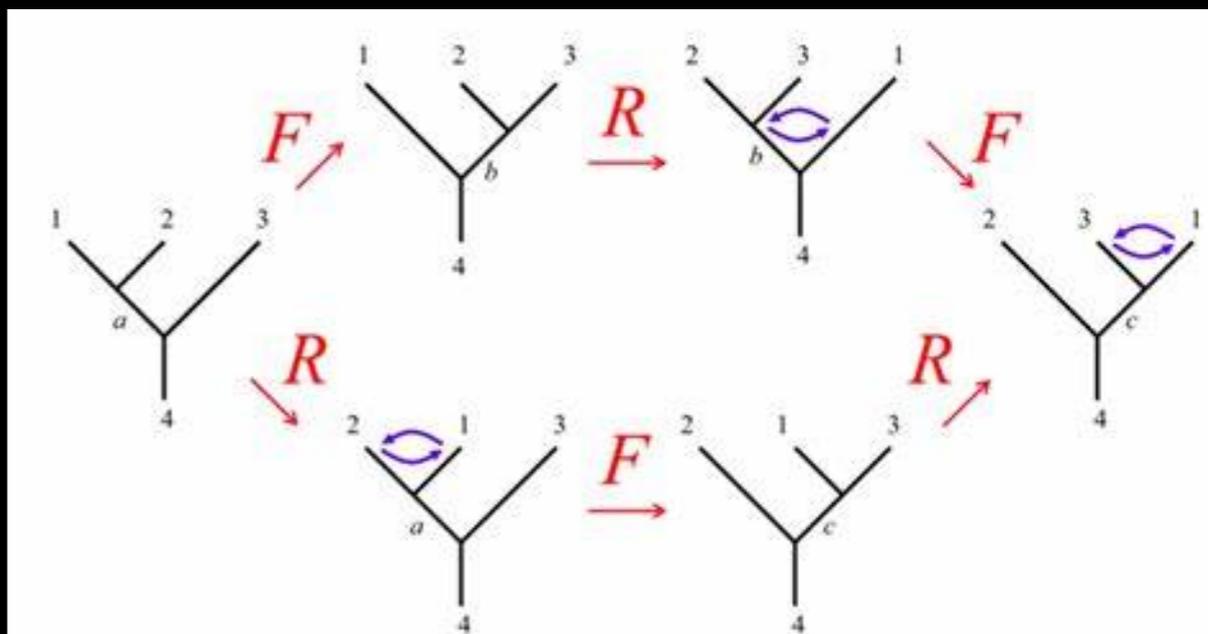


The Theorem is connected to several deep issues:  
**space-time symmetries,**  
**locality, causality**





Examples of “Effective” Violations in  
 Condensed Matter:  
**Topological Materials and Superconductors,  
 Anyons (F. Wilczek),  
 Haldane-Wu statistics**



If I exchange double times two creation/annihilation operators the final quantum state must be unchanged.

Three possibility:

$$|q| = 1$$

$$a_i a_j^\dagger - q a_i^\dagger a_j = \delta_{ij}$$

**Boson**



$$q = 1$$

**Fermions**



$$q = -1$$

Generalized: **Anyons**

$$q = e^{i\delta}$$

**In principle delta can be a function of energy and momentum** (AA et al 2017-2023)

# Anyons (Haldane-Wu statistics)

*Haldane 91', Wu 94'*

*When we exchange two particles in presence of magnetic flux tubes, a relative phase related to the fluxes is obtained  
(from Aharonov-Bohm effect)*

Coordinates start to be effectively  
**non-commutative!**

$$\exp(i\theta_{12}) = \exp[-i(q_1\phi_2 + q_2\phi_1)].$$

$$[R_i^\mu, R_j^\nu] = i l^2 \delta_{ij} q_i \epsilon^{\mu\nu}.$$

But it is not a violation  
for fundamental particles.

**Can we introduce a PEP violating  
algebra in fundamental laws of Nature?**

# q-Algebra

Yu, Ignatiev, Kuzmin, 87'; Greenberg, Mohapatra, 87'

$$aa^\dagger - q_\pm a^\dagger a = 1$$

$$q_\pm = \pm 1 + \frac{1}{2}\delta^2$$


$$\Gamma_i = \delta_i^2 \tilde{\Gamma}_i.$$

Observable:  
transition rates

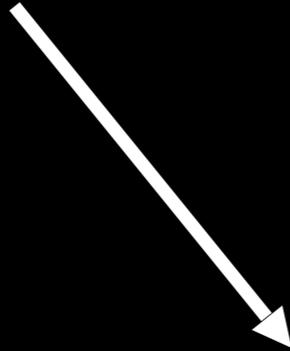
Here: (i)  $\delta_i^2$  is the mixing probability of non-fermion statistics allowing for the transition to the occupied state  $i$ ; (ii)  $\tilde{\Gamma}_i$  is the width of the corresponding PEP-allowed transition whenever the final state ( $i$ ) would be empty.

## Difficulties:

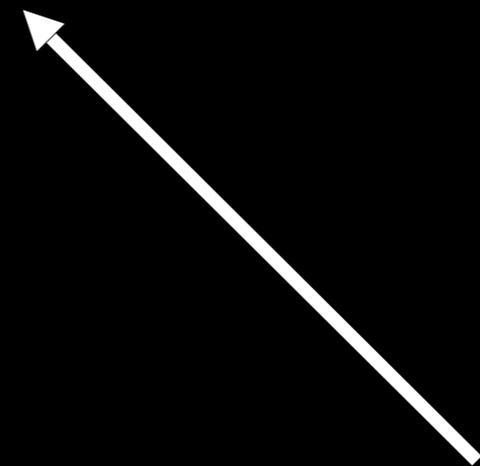
To build a self-consistent quantum field theory with causality, locality, unitarity, Lorentz/Poincaré symmetry appears at the moment impossible.

**Where may Quantum  
Gravity  
and Spin Statistics meet?**

**Quantum Gravity**



**Space-Time  
structure**



**PEP**

**A “class” of Quantum  
gravity models predicts  
tiny violations of PEP**

**PEPV in Non-commutative  
space-time:  
Theta-Poincare, kappa-Poincare...**

Addazi *et al* in a series of works 2017-2023,  
CPC, PRL, PRD, MDPI, IJMPA, IJMPA  
In collaboration with VIP and DAMA

**Non-linear Generalized  
Uncertainty Principle**

Addazi, Bernabei, Belli, Marciano, Shababi  
EPJC 2020

Energy dependence of PEP violations  
Natural in the logic  
of **effective theories**,  
Beyond q-models

$$a_i a_j^\dagger - q(E) a_j^\dagger a_i = \delta_{ij},$$

**Energy of the characteristic  
transition process**

$$q(E) = -1 + \beta^2(E),$$

$$\delta^2(E) = \beta^2(E)/2.$$

$$\delta^2(E) = c_k \frac{E^k}{\Lambda^k} + O(E^{k+1})$$

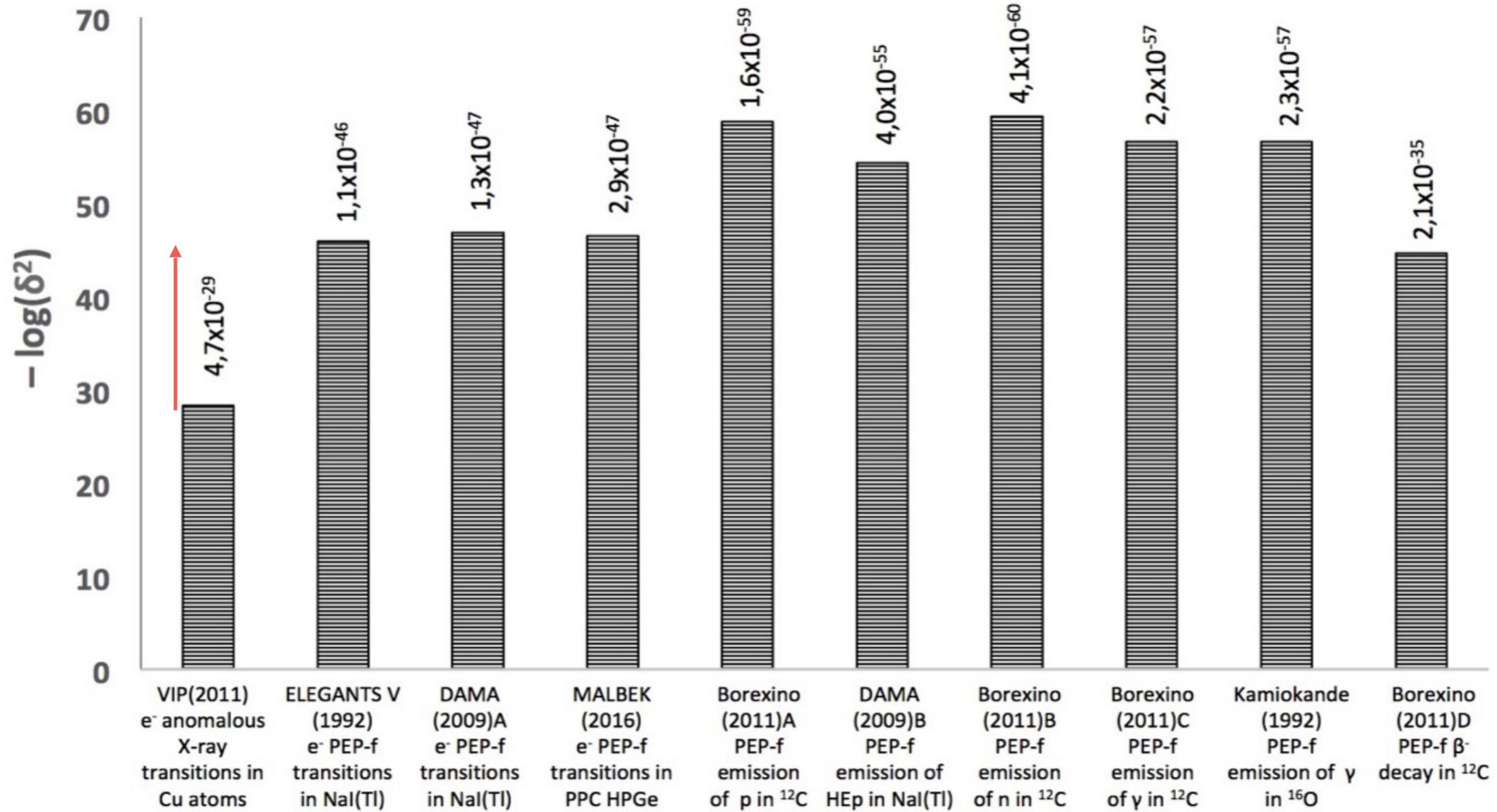
All possible PEPV  
transition rates.

Nuclear or atomic transitions.

$$\Gamma_i = \delta_i^2 \tilde{\Gamma}_i.$$

Here: (i)  $\delta_i^2$  is the mixing probability of non-fermion statistics allowing for the transition to the occupied state  $i$ ; (ii)  $\tilde{\Gamma}_i$  is the width of the corresponding PEP-allowed transition whenever the final state ( $i$ ) would be empty.

# COMPILATION



From these limits,  
One can put constraints  
on the new physics scale

**PEPV**

**&**

**Non-commutative space-time**

**Non-commutative space-time is a “old” standing idea. Firstly quoted to *Heisenberg***

$$\theta^{\mu\nu} = -\theta^{\nu\mu} = \text{constant.}$$

$$\hat{x}^\mu(x) = x^\mu$$

$$(\hat{x}^\mu \star \hat{x}^\nu - \hat{x}^\nu \star \hat{x}^\mu) = [\hat{x}^\mu, \hat{x}^\nu]_\star = i\theta^{\mu\nu}.$$



Here we insert the effective non-commutative length

In other words we imagine that the non-commutativity of space-time coordinates emerges out at a critical length scale having in mind the quantum gravity Planck scale...In the macroscopic limit the NC vanishes as consequence of the *correspondence principle*

Such a new quantum uncertainty  
can **delocalize** the General  
Relativity singularities beyond the  
Classical Penrose theorem

The we can think to formulate  
a Quantum field theory in the  
NC background

But there is a problem:  
NC is not compatible with local Lorentz  
invariance...

If we want a controllable new QFT  
we need new symmetries enlarging the  
Poincaré symmetry and compatible with NC

# Theta-Poincarè :in the Groenwald-Moyal arena

$$f \star g = f e^{\frac{i}{2} \overleftarrow{\partial}_\mu \theta^{\mu\nu} \overrightarrow{\partial}_\nu} g,$$

$$\theta^{\mu\nu} = -\theta^{\nu\mu} = \text{constant.}$$

$$\hat{x}^\mu(x) = x^\mu$$

$$(\hat{x}^\mu \star \hat{x}^\nu - \hat{x}^\nu \star \hat{x}^\mu) = [\hat{x}^\mu, \hat{x}^\nu]_\star = i\theta^{\mu\nu}.$$

$$\Delta_\theta(g) = e^{\frac{i}{2} P_\mu \otimes \theta^{\mu\nu} P_\nu} (g \otimes g) e^{-\frac{i}{2} P_\mu \otimes \theta^{\mu\nu} P_\nu} = \hat{F}_\theta^{-1} (g \otimes g) \hat{F}_\theta ,$$

## Groenwald-Moyal product deformation

**GM** :  $so(3, 1) \rightarrow$  noncommutative dual “deformed”  $so(3, 1)$

**GM** : (creation/annihilation ops.)  $\rightarrow$  (GM – phase)(creation/annihilation ops.) ,

**GM** : (fields)  $\rightarrow$  (GM – phase)(fields) ,

**GM** : N – field interactions  $\rightarrow$  (GM – phase)<sup>N</sup>(creation/annihilation ops.)<sup>N</sup> .

# Quantum fields as Groenwald-Moyal representations

$$\varphi = \int d\mu(p) \tilde{\varphi}(p) \mathbf{e}_p \qquad \varphi = \int \frac{d^d p}{2p_0} (a(p) \mathbf{e}_p + a^\dagger(p) \mathbf{e}_{-p}) \ ,$$

$$\varphi \otimes \chi = \int d\mu(p) d\mu(q) \tilde{\varphi}(p) \tilde{\chi}(q) \mathbf{e}_p \otimes \mathbf{e}_q$$

$$\rho(\Lambda) \varphi = \int d\mu(p) \tilde{\varphi}(p) \mathbf{e}_{\Lambda p} = \int d\mu(p) \tilde{\varphi}(\Lambda^{-1} p) \mathbf{e}_p \ ,$$

$$\rho(e^{iP \cdot a}) \varphi = \int d\mu(p) e^{ip \cdot a} \tilde{\varphi}(p) \mathbf{e}_p \ .$$

$$\Delta_\theta(\Lambda) (\tilde{\varphi} \otimes \tilde{\chi})(p, q) = \tilde{F}_\theta^{-1}(\Lambda^{-1} p, \Lambda^{-1} q) \tilde{F}_\theta(p, q) \tilde{\varphi}(\Lambda^{-1} p) \tilde{\chi}(\Lambda^{-1} q) \ .$$

$$F_\theta = e^{-\frac{i}{2}(-i\partial_\mu)\theta^{\mu\nu} \otimes (-i\partial_\nu)}$$

$$a(p)a^\dagger(q) = \tilde{\eta}'(p, q) \tilde{F}_\theta^{-2}(-q, p) a^\dagger(q)a(p) + 2p_0 \delta^d(p - q) \ .$$

## Overlap probability different from zero: PEPV

$$\begin{aligned} |\alpha, \alpha\rangle &= \langle a^\dagger, \alpha \rangle \langle a^\dagger, \alpha \rangle |0\rangle \\ &= \int \frac{d^d p_1}{2p_{10}} \frac{d^d p_2}{2p_{20}} e^{-\frac{i}{2} p_{1\mu} \theta^{\mu\nu} p_{2\nu}} \alpha(p_1) \alpha(p_2) c^\dagger(p_1) c^\dagger(p_2) |0\rangle . \end{aligned}$$

$$|\beta, \gamma\rangle = \langle a^\dagger, \beta \rangle \langle a^\dagger, \gamma \rangle |0\rangle, \quad \beta \neq \gamma.$$

We have

$$\langle \beta, \gamma | \alpha, \alpha \rangle = \int \frac{d^d p_1}{2p_{10}} \frac{d^d p_2}{2p_{20}} (\bar{\beta}(p_1) \alpha(p_1)) (\bar{\gamma}(p_2) \alpha(p_2)) [1 - e^{-ip_{1\mu} \theta^{\mu\nu} p_{2\nu}}] \frac{1}{N(\alpha, \alpha)} .$$

# CPT

$$\Delta_\theta(\mathcal{C}) = \Delta_0(\mathcal{C}) = \mathcal{C} \otimes \mathcal{C},$$

$$\Delta_0(\mathcal{P}) = \mathcal{P} \otimes \mathcal{P},$$

$$\Delta_0(\mathcal{T}) = \mathcal{T} \otimes \mathcal{T}.$$

$$CPT : \phi_\theta = (CPT \phi_0 (CPT)^{-1}) e^{\frac{1}{2} \overleftarrow{\partial} \wedge P},$$

$$\Delta_\theta(CPT) = \mathcal{F}_\theta^{-1} \Delta_0(CPT) \mathcal{F}_\theta.$$

# CPT and S-matrix

$$S_\theta = T_\star \exp_\star \left[ -i \int d^4x \mathcal{H}_{I,\theta}(x) \right],$$

$$\mathcal{H}^n \equiv \mathcal{H}_{1,\theta} \star \mathcal{H}_{2,\theta} \star \dots \star \mathcal{H}_{n,\theta} = \mathcal{H}_{1,0} \mathcal{H}_{2,0} \dots \mathcal{H}_{n,0} e^{i \overleftarrow{\partial} \wedge P} \equiv \mathcal{H}^{n\dagger},$$

Hermitian at tree-level  
(possible attacks from UV/IR mixings)

$$(CPT) \mathcal{H}^n (CPT)^{-1} = (\text{MOYAL}) \mathcal{H}^n.$$

Non-trivial transformation under CPT

# Microcausality: Bogoliubov-Shirkov condition

$$[\mathcal{H}_*(x), \mathcal{H}_*(y)] \neq 0, \quad (x - y)^2 < 0.$$

$$\begin{aligned} S[g] &= 1 + \int dx_1 g(x_1) \star S_1(x_1) + \int dx_1 dx_2 g(x_1) \star g(x_2) \star S_2(x_1, x_2) + \dots \\ &= 1 + \sum_{n \geq 1} \frac{1}{n!} \int S_n(x_1, \dots, x_n) \star g(x_1) \star \dots \star g(x_n) dx_1 \dots dx_n. \end{aligned}$$

Then, the BS causality condition reads

$$\frac{\delta}{\delta g(x)} \left( \frac{\delta S(g)}{\delta g(y)} \star S^\dagger(g) \right) = 0, \quad x < y,$$

**You can show that BS is violated! proof in**  
*Addazi, Marciano IJMPA*

# UV/IR mixings

$$\Lambda_{\text{eff}} = \Lambda_0 + C/(\theta^2 p^2)$$

Appearing in one-loop radiative  
computation *Alvarez-Gaume et al*

Not fully understood and  
In principle it may be cancelled by possible  
Cerenkov emission  
Comment in Addazi-Marciano IJMPA review

# Mention: the case of kappa-Poincare

Ambiguity in quantization procedure,  
M. Arzano, A. Marciano;  
K, Glikman et al.  
Ambiguity Vs PEPV

# **Generalized Uncertainty Principle (GUP)**

First appearance in the first works of *Amati, Ciafaloni and Veneziano 87'* on gravitational scatterings in the “Arena” of string theory. From Perturbative corrections the Heisenberg uncertainty principle gets an effective correction as follow:

$$\Delta x \Delta p \geq \frac{\hbar}{2} (1 + \beta \Delta p^2)$$

Reconsider as basic new principle by *Kempf-Mangano-Mann 95'*

Further non-perturbative quantum gravity effects motivate possible analysis of non-linear extensions!

# Example: Non-linear GUPs with a UV pole

$$[X_i, P_j] = \frac{i\hbar\delta_{ij}}{(1 - (\beta P^2)^{m'})^k}, \quad [P_i, P_j] = 0,$$

$$[X_i, X_j] = \frac{2i\hbar\beta}{(1 - (\beta P^2)^{m'})^{2k}} (P_i X_j - P_j X_i),$$

$$[L_i, L_j] = \frac{i\hbar}{(1 - (\beta P^2)^{m'})^k} (X_i P_j - X_j P_i)$$

$$= \frac{i\hbar}{(1 - (\beta P^2)^{m'})^k} \epsilon_{ijk} L_k,$$

$$L_i = \frac{1}{(1 - (\beta P^2)^{m'})^k} \epsilon_{ijk} r_j P_k.$$

$$[X_i, X_j] = \frac{-2i\hbar\beta}{(1 - (\beta P^2)^{m'})^k} L_{ij}.$$

# Around the UV pole super-uncertainty

$$\lim_{P \rightarrow \Lambda} \Delta X \Delta P \rightarrow \infty$$

$$\lim_{P \rightarrow \Lambda} \Delta X_i \Delta X_j \rightarrow \infty$$

$$\Delta L_i \Delta L_j \rightarrow \infty$$

A 100% localization of an electron on a precise level is impossible.

Example of a two level system

Quantum State of an almost first level electron:

$$|J', M'\rangle \simeq (1 - k(\beta P^2)^{m'}) |j_1, m_1\rangle + k(\beta P^2)^{m'} |j_2, m_2\rangle,$$

Quantum State of an almost second level electron:

$$|J, M\rangle \simeq [k(\beta \tilde{P}^2)^{m'} |j_1, m_1\rangle + (1 - k(\beta \tilde{P}^2)^{m'}) |j_2, m_2\rangle].$$

Non-zero overlap: PEP violating jumps

$$\langle J, M | J', M' \rangle |_{J, M \neq J', M'}$$

$$= [k(\beta \tilde{P}^2)^{m'} (1 - k(\beta P^2)^{m'}) + k(\beta P^2)^{m'} (1 - n(\beta \tilde{P}^2)^{m'})].$$

$$\langle J, M | J', M' \rangle \simeq 2k(\beta P)^m$$

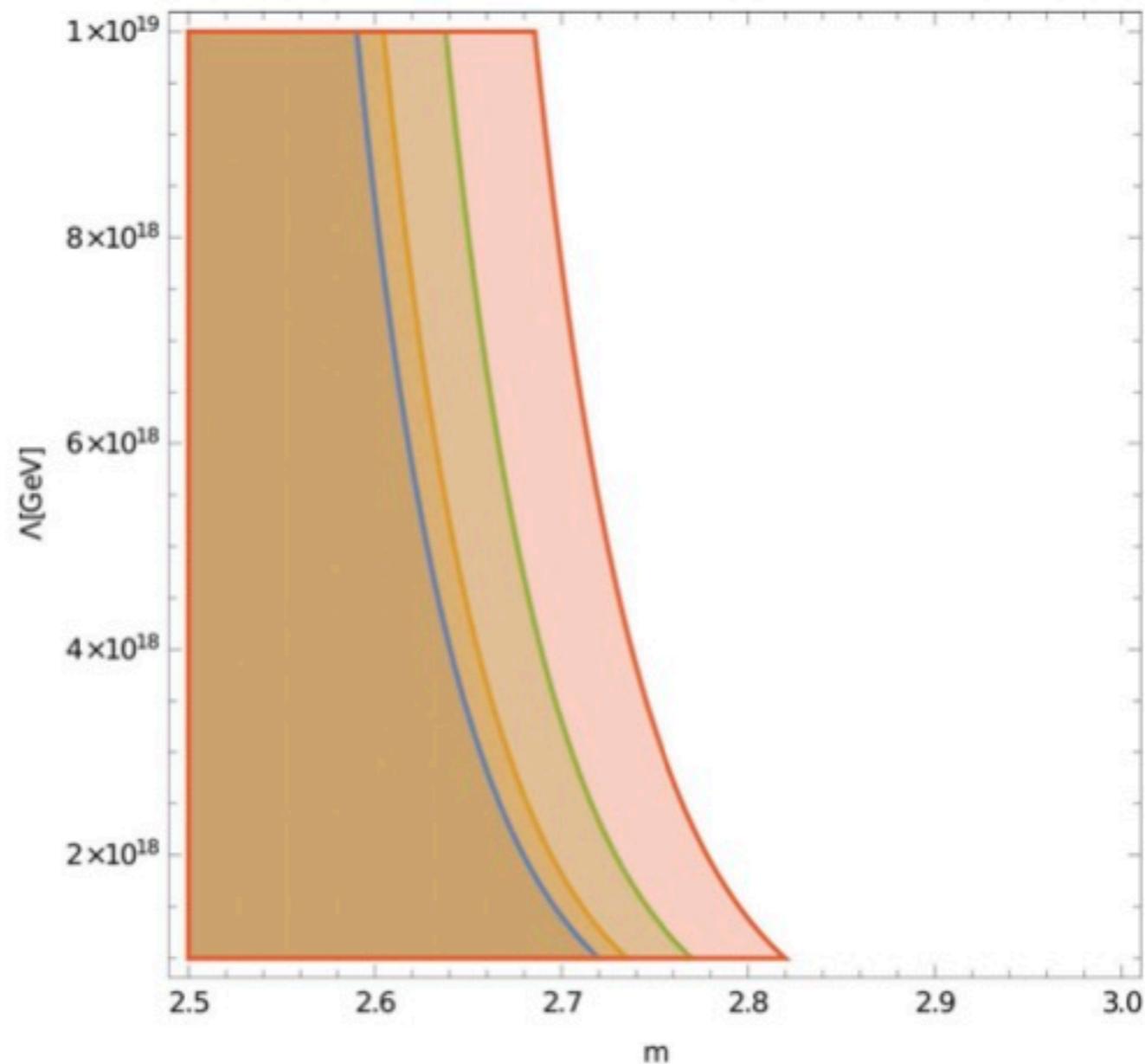
# Results from DAMA/LIBRA

From exclusions of Na a I PEPV transitions

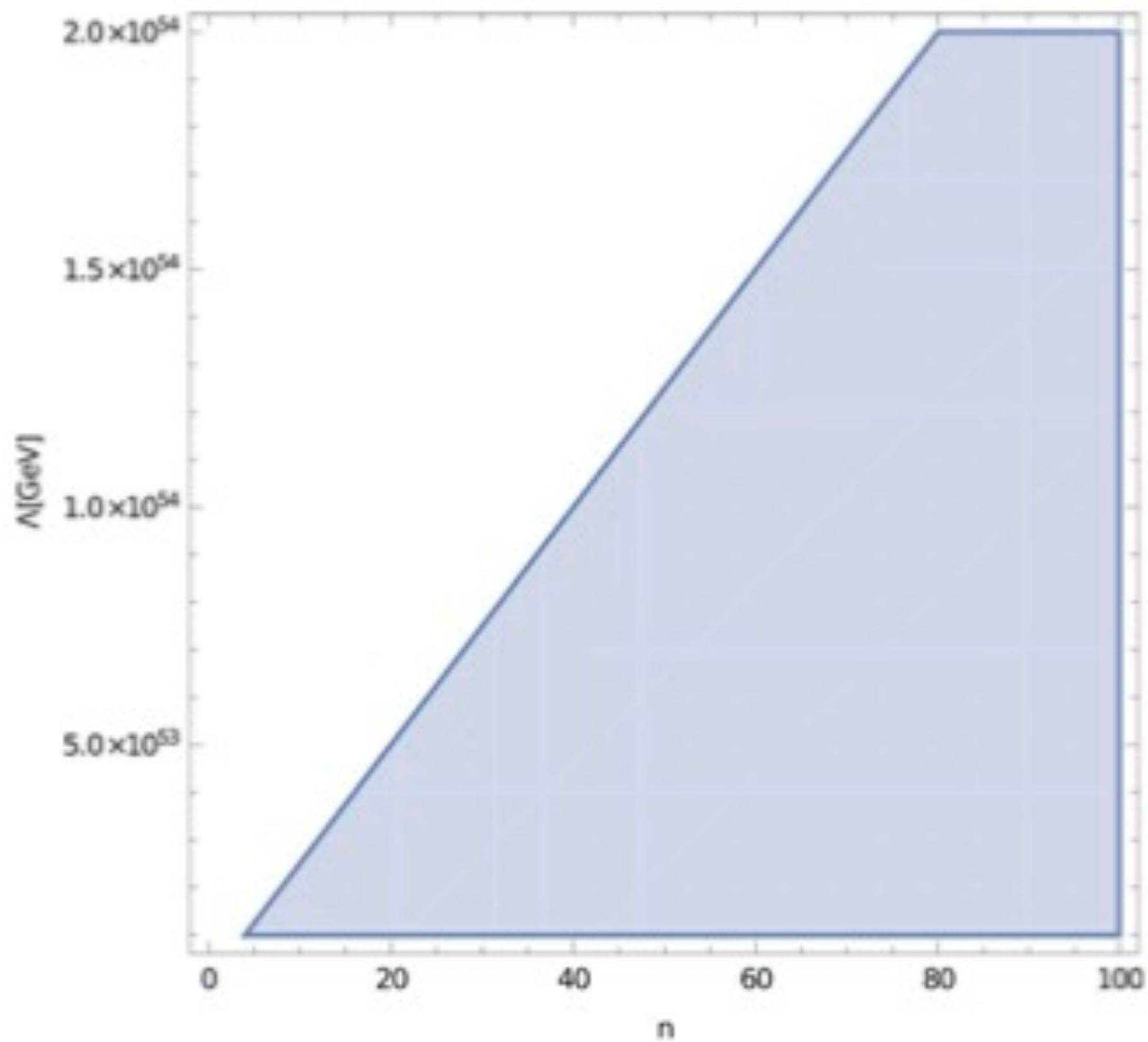
$$\Gamma_{PEPV} = n(\Lambda^{-1} P)^m \Gamma_{SM},$$

where  $n = 4k^2$ ,  $m = 4m'$ .

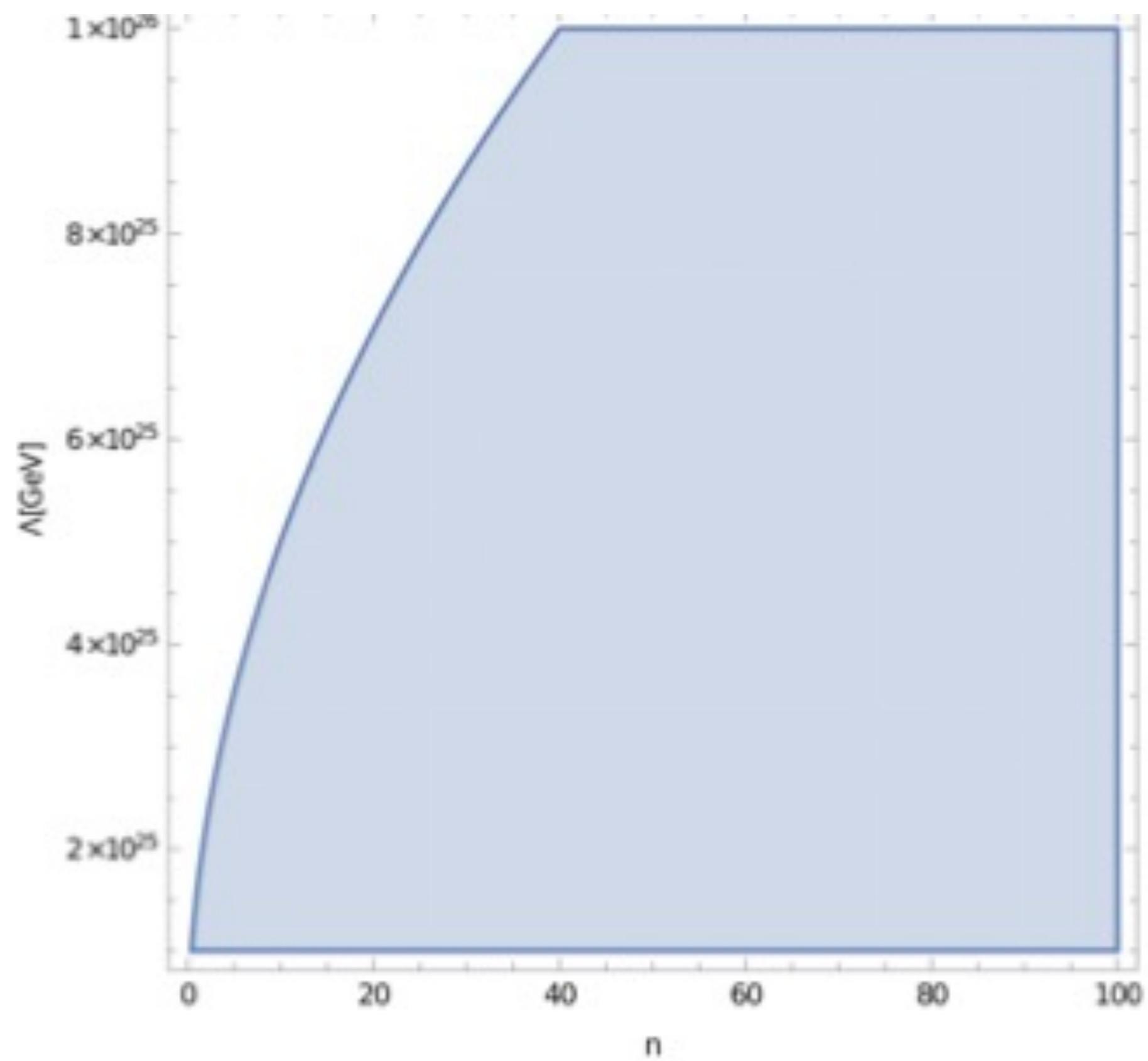
$$n(\Lambda^{-2} P)^m < 4 \times 10^{-33} \text{ (90\% C.L.)}.$$



**Fig. 1** Excluded parameter space ( $\Lambda$ ,  $m$ ) from DAMA experiment: the four contour limits correspond to fix  $n = 1, 2, 10, 100$  respectively



**Fig. 2** Excluded parameter space ( $\Lambda$ ,  $n$ ) from DAMA experiment, fixing  $m = 1$



Let's return to the model  
independent analysis  
well motivated by NC

$$a_i a_j^\dagger - q(E) a_j^\dagger a_i = \delta_{ij},$$

**Energy of the characteristic  
transition process**

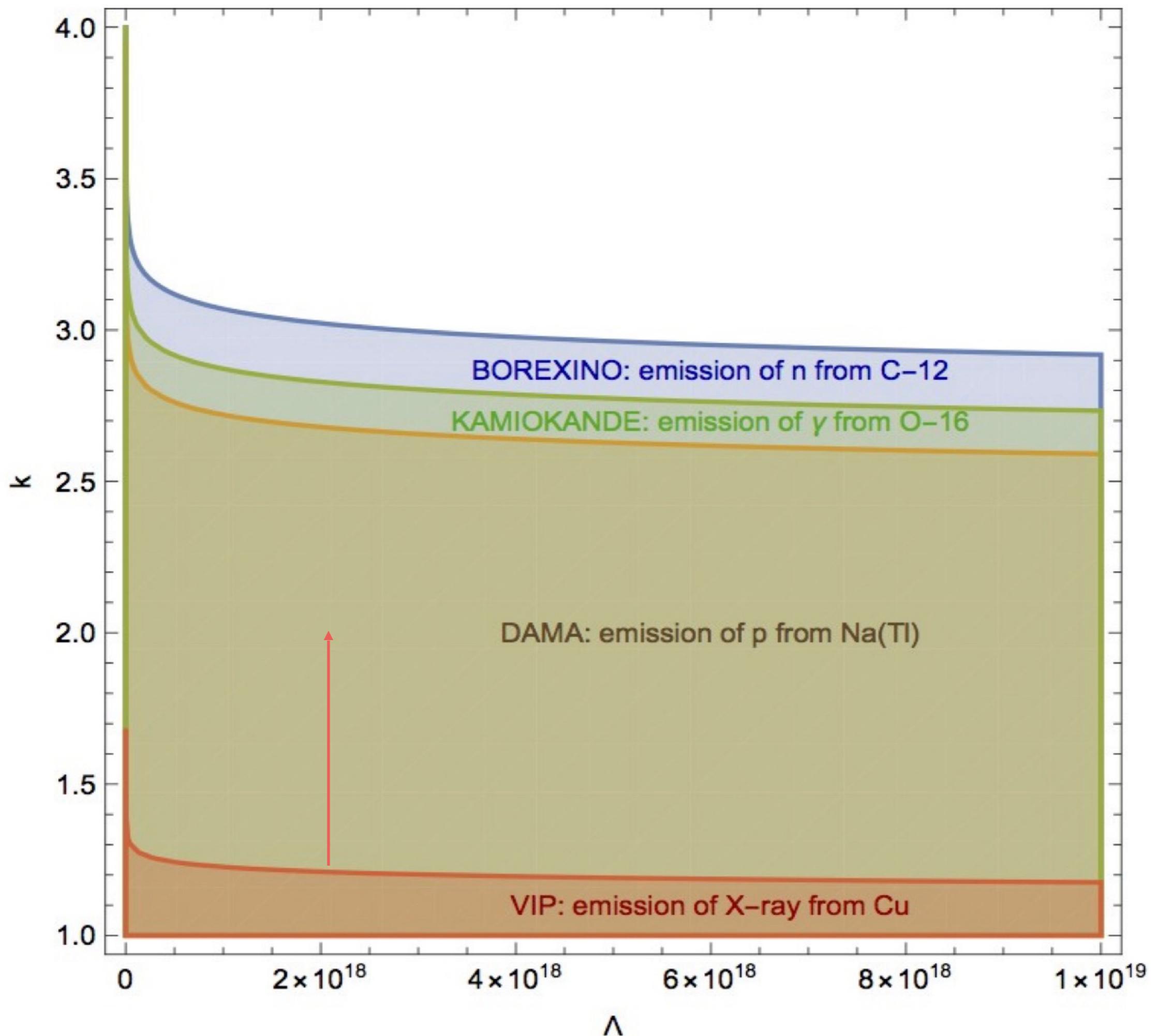
$$q(E) = -1 + \beta^2(E),$$

$$\delta^2(E) = \beta^2(E)/2.$$

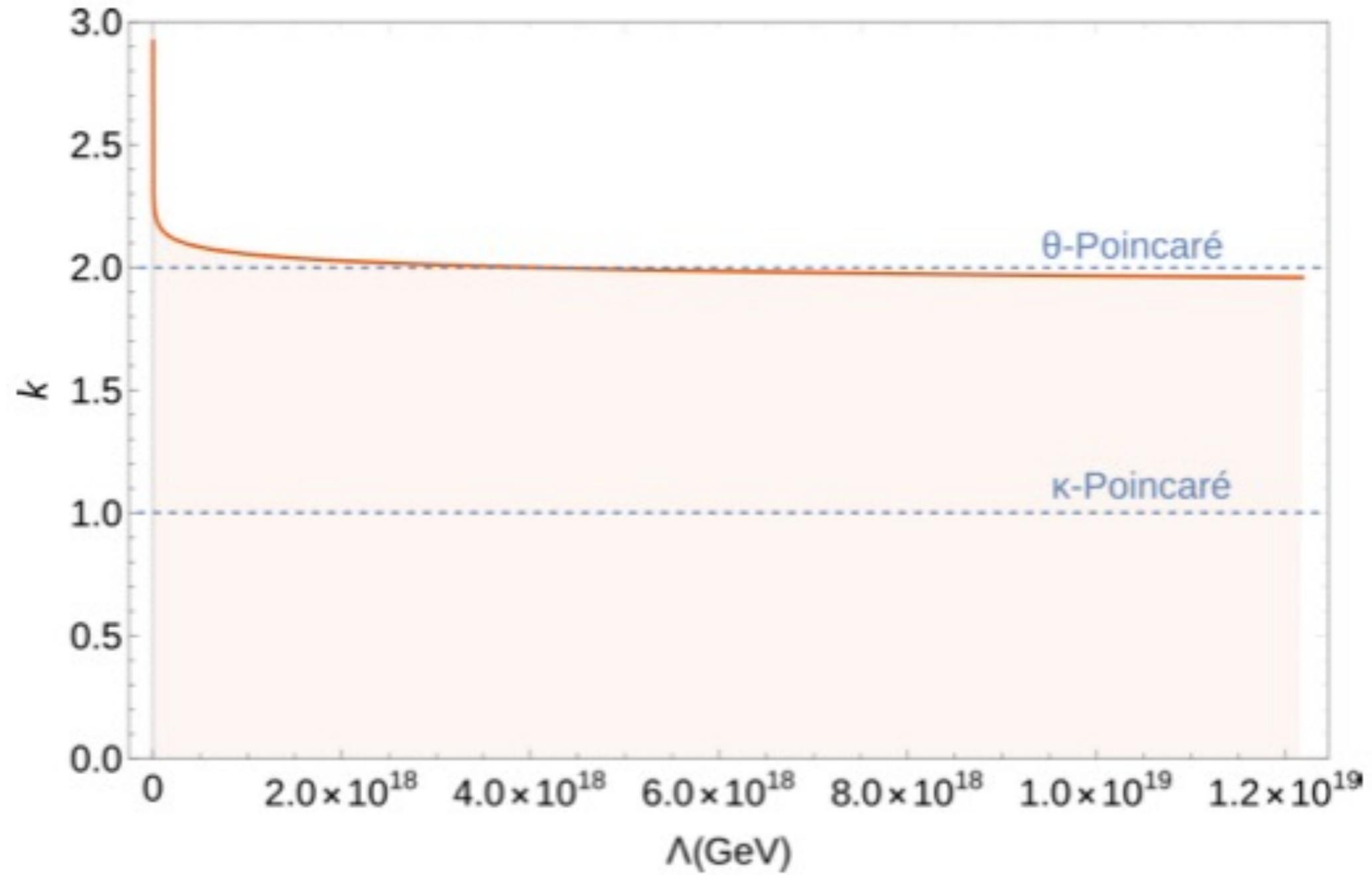
$$\delta^2(E) = c_k \frac{E^k}{\Lambda^k} + O(E^{k+1})$$

# Results

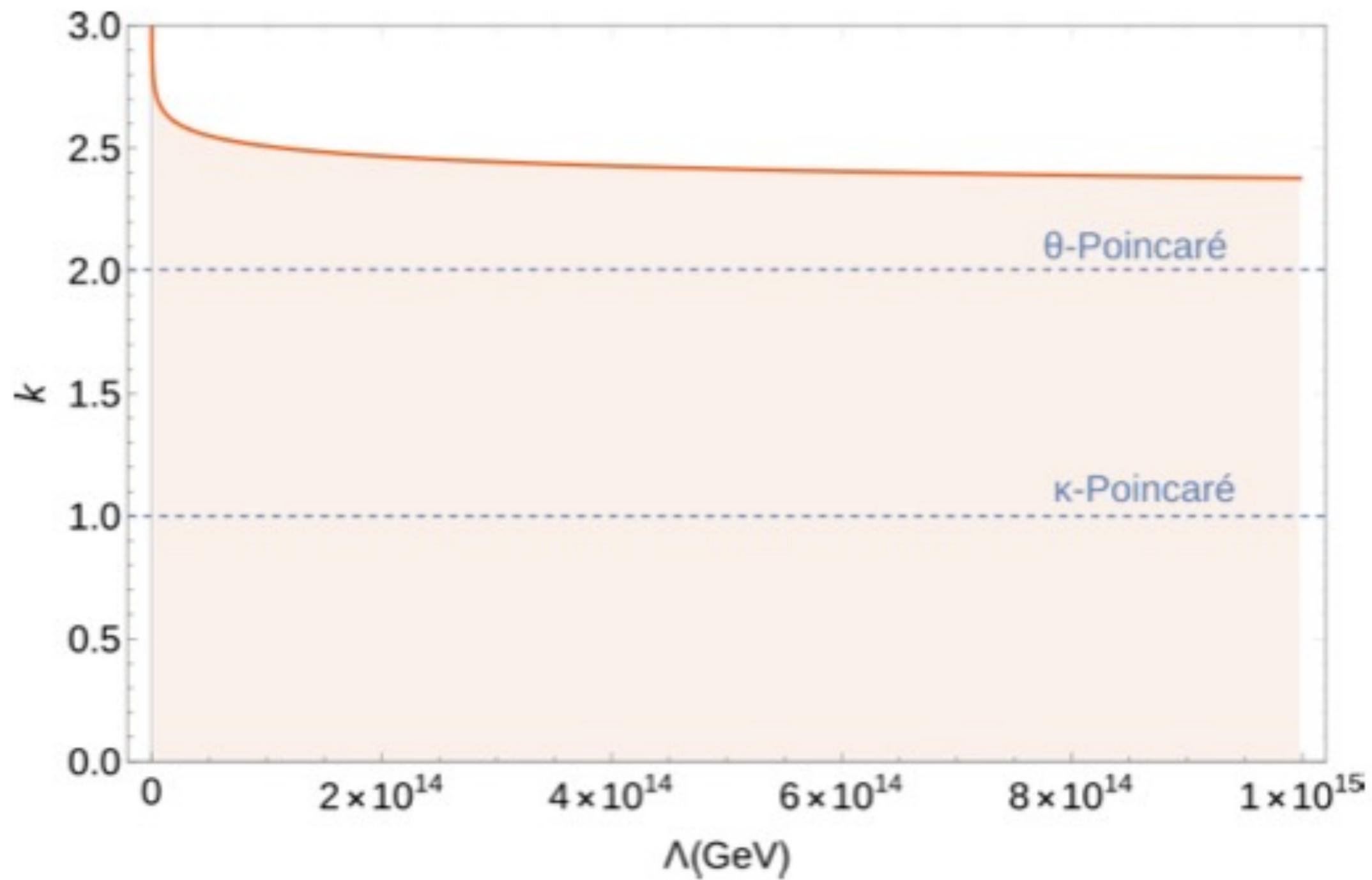
A. Addazi, P. Belli, R. Bernabei, A. Marciano  
2017-2019



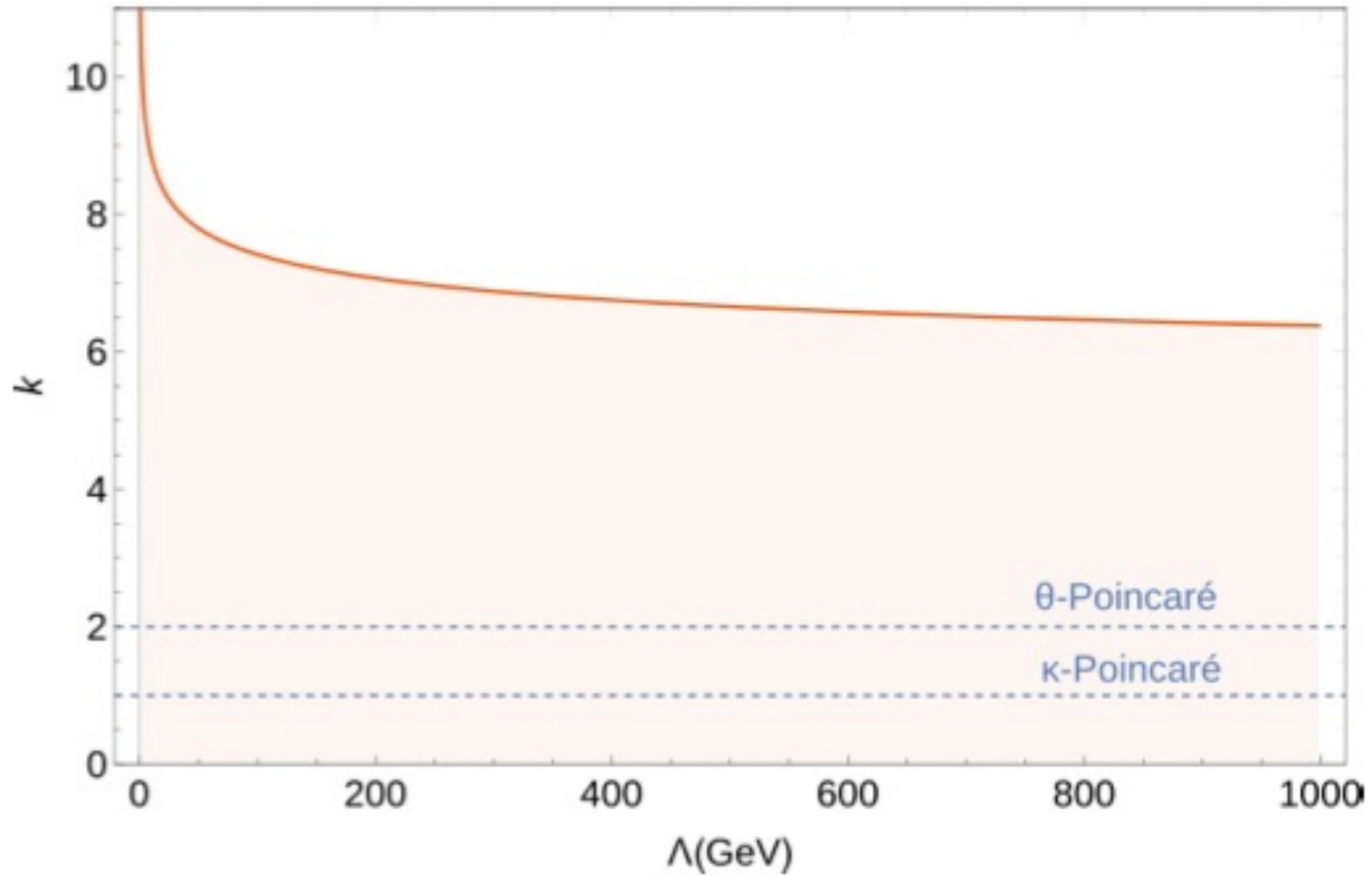
# VIP-II



# VIP-II



# VIP-II



Thus, surprise, many  
quantum gravity models  
appear to be excluded yet!

Importance of multi-channels:  
nuclear and atomic physics:

**Vexata quaestio:  
Democratic or non-democratic  
PEP violations???**

- **Weak and Strong  
Equivalence Principle???**
- **B-form couplings with strings???**

**IT DESERVES A TEST IN ALL  
POSSIBLE CHANNELS!**

$\langle B \rangle X X$

Seidberg, Witten

“In principle its condensation may be highly non-trivial as a consequence of NS-NS or R-R string fluxes or exotic string instantons.  $B(x)$  with  $x$  space coordinate”

Addazi to Bernabei, private conversation 2017 Chengdu

**In this prospective we follow  
with great interests new  
experiments based on atomic  
transitions**

# **VIP-2 improvements**

$$\phi_{\text{PEPV}} = \delta^2 \simeq \frac{D}{2} \frac{E_N}{\Lambda} \frac{\Delta E}{\Lambda}, \quad D = p_1^0 \bar{\theta}_{0j} p_2^j + p_2^0 \bar{\theta}_{0j} p_1^j,$$

$$E_N \simeq m_N \simeq$$

$$\phi_{\text{PEPV}} = \delta^2 \simeq \frac{C}{2} \frac{E_1}{\Lambda} \frac{E_2}{\Lambda},$$

$$\Delta E = E_2 - E_1$$

where  $E_{1,2}$  are the energy levels occupied by the initial and the final electrons and  $C = p_1^i \bar{\theta}_{ij} p_2^j$ . The former

# Theta-Poincare from VIP

- $\Lambda > 6.9 \cdot 10^{-2}$  Planck scales for  $\theta_{0i} = 0$
- $\Lambda > 2.6 \cdot 10^2$  Planck scales for  $\theta_{0i} \neq 0$

Physical Review Letters result 2022

# New Plots and analysis VIP

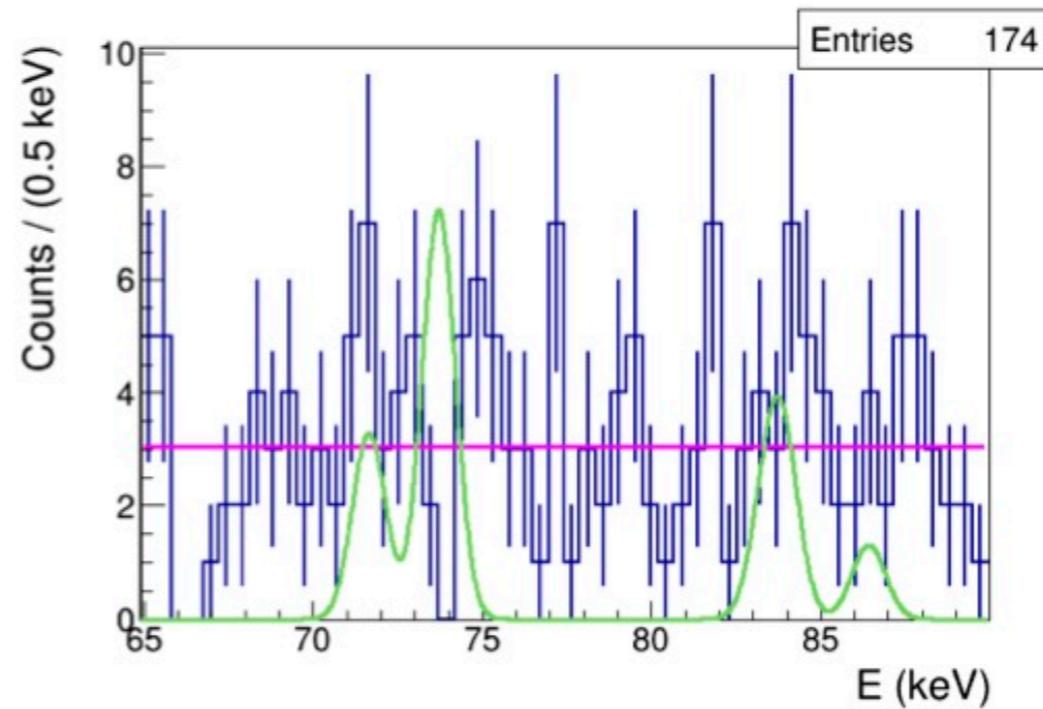


FIG. 1. The measured X-ray spectrum, in the region of the  $K_\alpha$  and  $K_\beta$  standard and PEP-violating transitions in Pb, is shown in blue; the magenta line represents the fit of the background distribution. The green line corresponds to the shape of the expected signal distribution (with arbitrary normalization) for  $\theta_{0i} \neq 0$ .

TABLE I. Calculated PEP-violating  $K_\alpha$  and  $K_\beta$  atomic transition energies in Pb (column labeled forb.). As a reference, the allowed transition energies are also quoted (allow.). Energies are in keV.

Transitions in Pb	allow. (keV)	forb. (keV)
1s - 2p <sub>3/2</sub> $K_{\alpha 1}$	74.961	73.713
1s - 2p <sub>1/2</sub> $K_{\alpha 2}$	72.798	71.652
1s - 3p <sub>3/2</sub> $K_{\beta 1}$	84.939	83.856
1s - 4p <sub>1/2(3/2)}</sub> $K_{\beta 2}$	87.320	86.418
1s - 3p <sub>1/2</sub> $K_{\beta 3}$	84.450	83.385

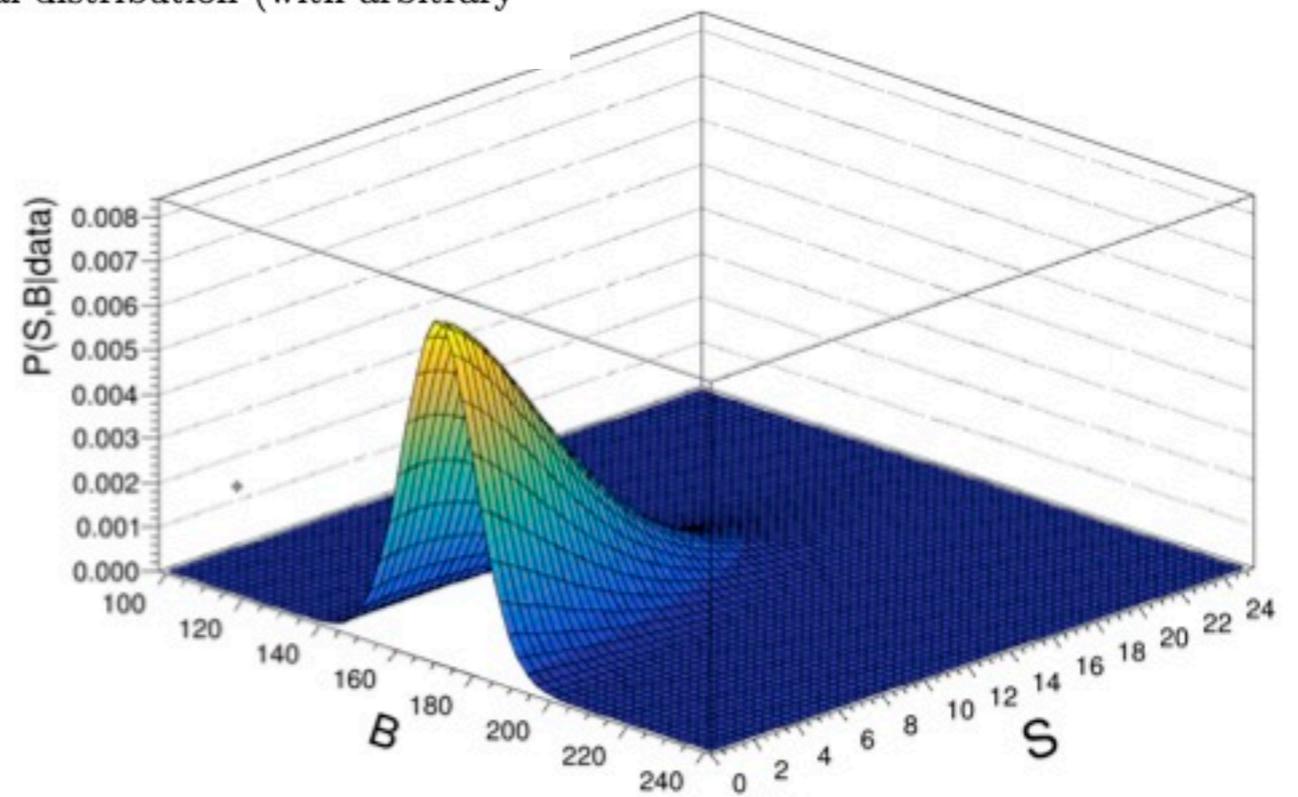


FIG. 2. Joint *pdf*  $P(S, B|data)$  of the expected number of total signal and background counts corresponding to  $\theta_{0i} \neq 0$ .

Several open  
Questions and Perspectives  
Never explored before!

Is it gravity emergent?

If the graviton is a spin 2 composite state or  
a pseudo-particle emerging  
From a fundamental renormalizable  
quantum gauge field theory  
like  $SU(N)$ ,  $SO(N)$ ...

Obstacle: spin 2 massless particle  
cannot be such a bound state if  
Lorentz invariance is preserve.  
Weinberg's theorem

However, Lorentz invariance can be spontaneously or dynamically broken,  
**Bjorken 63'**

No any no go theorem on the fact that tensor condensates

Cannot dynamically emerge from confinement in a generic gauge theory  
We can test confinement in QCD which is theoretically still purely understood.

Philips '66, Ohanian '69: Kostelecky, Berezhiani and Kanchelli: Carol, Tam, Wehus;  
Chkareuli, Jejelava, Tatishvili, Tomboulis

In this case,

The confinement scale  
Is assumed at or below the Planck  
scale, as UV completion

In general a tiny mass term for  
the graviton is generated out

The Equivalence Principle is  
violated from

Non-universality of couplings

Philips '66, Ohanian '69: Kostelecky, Berezhiani and Kanchelli: Carol, Tam, Wehus;  
Chkareuli, Jejelava, Tatishvili, Tomboulis

Spin Statistics?

It is preserved in UV

But It can be touched after the  
spontaneous Lorentz symmetry breaking

$$\langle T_{\mu\nu}(x) \rangle = \int \mathcal{D}\Phi \mathcal{T}_{\mu\nu} e^{iS\{\Phi\}}.$$

$$\Phi = \phi, \psi, A_\mu$$

$$\mathcal{T}_{\mu\nu} = \text{Tr}[K_1 \mathcal{O}_{\mu\nu}^{(1)} + K_2 \mathcal{O}_{\mu\nu}^{(2)} + K_3 \mathcal{O}_{\mu\nu}^{(3)}],$$

$$\mathcal{O}_{\mu\nu}^{(1)} = \phi^\dagger \partial_\mu \partial_\nu \phi, \quad \mathcal{O}_{\mu\nu}^{(2)} = \bar{\psi}(\partial_\mu \gamma_\nu + \partial_\nu \gamma_\mu \psi), \quad \mathcal{O}_{\mu\nu}^{(3)} = B_{\mu\rho} B_{\nu\sigma} \eta^{\rho\sigma}$$

$$\langle T_{\mu\nu} \rangle = G_{\mu\nu}.$$

$$\langle T_{\mu\nu} \rangle = G_{\mu\nu} .$$

$$\phi \partial_\mu \partial_\nu G^{\mu\nu} \phi, \quad \phi \partial_\mu \phi \partial_\nu \phi G^{\mu\nu}, \quad \phi \partial_\mu \partial_\nu \phi G^{\mu\lambda} \eta_\lambda^\nu .$$

$$\Delta^{-1} = k^2 - m^2 + k_\mu k_\nu \Delta_{\mu\nu} + X_{\mu\nu\rho\sigma} k^\mu k^\nu k^\rho k^\sigma / \Lambda^2 + O(k^n) ,$$

$$\Delta_{\mu\nu} = a_1 G_{\mu\nu} + a_2 G_\mu^\lambda G_{\lambda\nu} + \dots ,$$

$$a_{\mathbf{p}} a_{\mathbf{q}}^\dagger - f(p, q) a_{\mathbf{q}}^\dagger a_{\mathbf{p}} = (2\pi)^2 \delta^{(3)}(\mathbf{p} - \mathbf{q})$$

$$f(p, q) = 1 + \frac{1}{Q^2} \left( \Delta_{\mu\nu} Q^\mu Q^\nu - \frac{1}{\Lambda^2} X_{\mu\nu\rho\sigma} Q^\mu Q^\nu Q^\rho Q^\sigma \right) \Big|_{q^0=p^0},$$

$$Q_\mu(p, q) = p_\mu + q_\mu$$

**In non-relativistic limit and preserving Rotational invariance subrgoup SO(3):**

$$\langle T_{00} \rangle = \eta_{00}, \quad \langle T_{ij} \rangle = \langle T_{0i} \rangle = 0.$$

$$f(p, q) = 1 + \Delta_{00} - 4 \frac{1}{\Lambda^2} X_{0000} E_p^2,$$

# QED, PEPV

$$\frac{1}{\Lambda} G_{\mu\nu} \gamma^\mu p^\nu,$$

$$\langle \alpha\alpha | \beta\gamma \rangle \simeq N \int d\Sigma \bar{\alpha} \bar{\alpha} \beta \alpha G_{00}^2 \Delta E_{\alpha\beta} \Delta E_{\alpha\gamma} / \Lambda^2,$$

$$\Delta E_{\alpha\beta} = E_\alpha - E_\beta$$

# Conclusions:

Probes of Pauli Exclusion Principle Violations can provide a strong indirect test of quantum gravity models with physics observables much below the Planck physics domain

Both **Non-commutative and Non-linear GUP** models can be constrained up to the **Planck Scale regime.**

Not all of them but a large sub-group.

In particular the notorious Theta-Poincaré models seems already excluded in a “democratic scenario”

Consequences of energy dependent  
PEPV discovery for quantum gravity: a  
revolution of our picture of space-time,  
causality, locality, vacuum structure, ...