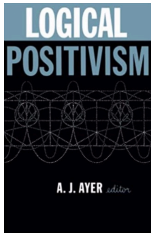
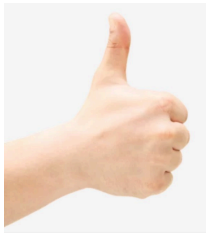


# OBSERVATIONAL EVIDENCE FOR PRIMORDIAL BLACK HOLES: A POSITIVIST PERSPECTIVE \*

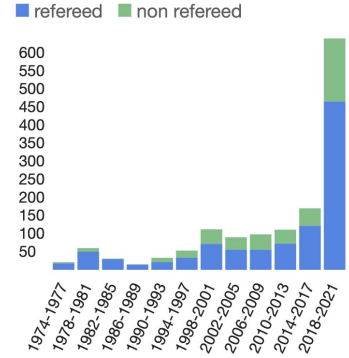



Bernard Carr, Queen Mary University of London  
Leiden/Brussels webinar (3/10/22)

\* with S.Clesse, J.Garcia-Bellido, M.Hawkins, F.Kuhnel

1

# PUBLICATION RATE OF PBH PAPERS



Impossible to keep up with literature!

2

# MY MOST CITED PAPERS!

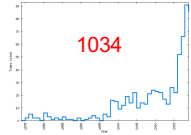
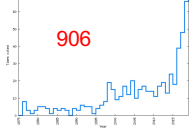
*Mon. Not. R. astr. Soc.* (1974) **108**, 399-415.

**BLACK HOLES IN THE EARLY UNIVERSE**  
B. J. Carr and S. W. Hawking  
(Received 1974 February 25)

**THE PRIMORDIAL BLACK HOLE MASS SPECTRUM\***  
Bernard J. Carr  
Department of Applied Mathematics and Theoretical Physics, Cambridge University, Cambridge, England;  
CERN, Institute of Technology, Pontreux  
(Received 1974 January 17)

**SUMMARY**  
The existence of galaxies today implies that the early Universe must have been inhomogeneous. Some regions might have got so compressed that they underwent gravitational collapse to produce black holes. Once formed, black holes in the early Universe would grow by accreting nearby matter. A first estimate suggests that they might grow at the same rate as the Universe during the radiation era and be of the order of  $10^6$  to  $10^9$  solar masses now. The observational evidence however is against the existence of such giant black holes. This motivates a more detailed study of the rate of accretion which shows that black holes will not in fact substantially increase their original mass by accretion. There could thus be primordial black holes around now with masses from  $10^{-5}$  to  $10^9$  solar masses.

**ABSTRACT**  
We consider what mass spectrum of primordial black holes should result if the early universe contained of small density fluctuations superimposed on a Friedmann background. It is shown that only a certain type of fluctuation leads to the formation of primordial black holes and that, consequently, their spectrum should always have a particular form. Since both the fluctuations which give naturally rise to the fluctuations which are often invoked to explain galaxy formation and of the spectrum of primordial black holes could have had an important effect in the evolution of the universe. In particular, although primordial black holes are unlikely to have a critical density, they could have been sufficiently numerous to act as a condensation nuclei for galaxies. Observational limits on the spectrum of primordial black holes place strong constraints on the magnitude of density fluctuations in the early universe and support the conventional view that the early universe was nearly homogeneous rather than having the irregularities which the early universe has a rich spectrum of mass for a primordial period is shown to be supported, since primordial black holes probably form too profusely in such a situation to be consistent with observations.

Career all downhill from the start.....

3

# .....with a resurgence at the end!

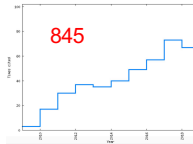

**PHYSICAL REVIEW D** **34**, 1601 (1986)

**New cosmological constraints on primordial black holes**  
B. J. Carr<sup>1</sup>  
<sup>1</sup>Department of Physics and Astronomy, Queen Mary University of London, Mile End Road, London E1 4NS, United Kingdom  
Research Center for the Early Universe (RCEU), Graduate School of Science, The University of Tokyo, Tokyo 113-0033, Japan  
Canadian Institute for Theoretical Astrophysics, University of Toronto, 60 St George Street, Toronto, Ontario M5S 1A5, Canada

**PHYSICAL REVIEW D** **34**, 1601 (1986)

**Primordial black holes as dark matter**  
Bernard Carr,<sup>1,2</sup> Florian Kuhnel,<sup>1,3</sup> and Mark Sandstad<sup>1,2</sup>  
<sup>1</sup>Department of Physics and Astronomy, Queen Mary University of London, Mile End Road, London E1 4NS, United Kingdom  
<sup>2</sup>The Ohio State Center for Cosmological Physics, Department of Physics, The Ohio State University, Columbus, OH 43210, USA  
<sup>3</sup>Max-Planck-Institut für Physik, Werner-Heisenberg-Institut, Munich, Germany

**ABSTRACT**  
The possibility that the dark matter comprises primordial black holes (PBHs) is revisited, with particular emphasis on the currently allowed mass windows at  $10^{-16}$  to  $10^{-14}$  M<sub>⊙</sub> and  $10^{-10}$  to  $10^{-8}$  M<sub>⊙</sub>. The PBH mass ratios of models incorporating PBHs are also considered. All relevant constraints (density, dynamical, large-scale structure, and accretion) are reviewed and various effects necessary for a precise calculation of the PBH abundance (gravitational-wave emission, critical collapse, and secondary accretion) are included. It is difficult to put all the dark matter in PBHs if their mass function is monochromatic but this is still possible if the mass function is extended, as expected in many scenarios. A novel procedure for combining observational constraints with an extended PBH mass spectrum is therefore introduced. This applies to arbitrary constraints and a wide range of PBH emission models and allows us to identify which model-independent constraints can be shown from constraints over all mass ranges. We have particularly in PBHs produced by inflation, pointing out which effects in the formation process influence the resulting PBH mass spectrum. We then apply our scheme to the PBH mass function. We then apply our scheme to the PBH mass function. We then apply our scheme to the PBH mass function. We then apply our scheme to the PBH mass function.

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*Mon. Not. R. astr. Soc.* (1971) **152**, 75-78.

GRAVITATIONALLY COLLAPSED OBJECTS OF VERY LOW MASS


Stephen Hawking

(Communicated by M. J. Roes)

(Received 1970 November 9)

SUMMARY

It is suggested that there may be a large number of gravitationally collapsed objects of mass  $10^{-6}$  g upwards which were formed as a result of fluctuations in the early Universe. They could carry an electric charge of up to  $\pm 30$  electron units. Such objects would produce distinctive tracks in bubble chambers and could form atoms with orbiting electrons or protons. A mass of  $10^{17}$  g of such objects could have accumulated at the centre of a star like the Sun. If such a star later became a neutron star there would be a steady accretion of matter by a central collapsed object which could eventually swallow up the whole star in about ten million years.



5

**Black hole explosions?** *Nature* **248**, 30 - 31 (01 March 1974)

S. W. HAWKING

Quantum Mechanics

Thermodynamics

General Relativity

$T_{BH} [K] = 10^{-7} \frac{M_{\odot}}{M}$

PBHs are important even if they never formed!

6

**PBH FORMATION ..... AND EVAPORATION**

$R_S = 2GM/c^2 = 3(M/M_{\odot}) \text{ km} \Rightarrow \rho_S = 10^{18}(M/M_{\odot})^{-2} \text{ g/cm}^3$

cf. cosmological density  $\rho \sim 1/(Gt^2) \sim 10^6(t/s)^{-2} \text{ g/cm}^3$

$\Rightarrow$  **primordial BHs with horizon mass at formation**

$10^{-5} \text{ g at } 10^{-43} \text{ s}$  (minimum?)

$M_{PBH} \sim c^3 t / G = 1 M_{\odot} \text{ at } 10^{-5} \text{ s}$  (QCD transition)

$10^5 M_{\odot} \text{ at } 1 \text{ s}$  (maximum?)

**Black holes radiate thermally with temperature**

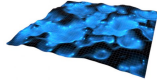
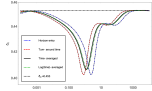
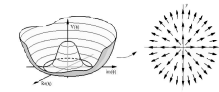
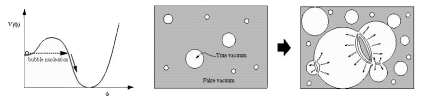
$$T = \frac{hc^3}{8\pi GkM} \sim 10^{-7} \left[ \frac{M}{M_0} \right]^{-1} \text{ K}$$

$\Rightarrow$  **evaporate completely in time**  $t_{\text{evap}} \sim 10^{64} \left[ \frac{M}{M_0} \right]^3 \text{ y}$

$M \sim 10^{15} \text{ g} \Rightarrow$  **final explosion phase today ( $10^{30}$  ergs)**

7

**Formation Mechanisms of Primordial Black Holes**

- ★ Large density perturbations (inflation) 
- ★ Pressure reduction 
- ★ Cosmic string loops 
- ★ Bubble collisions 

8

### PBH FORMATION $\Rightarrow$ LARGE INHOMOGENEITIES

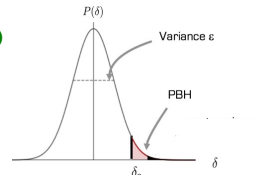
To collapse against pressure, need (Carr 1975)

$$R > \sqrt{\alpha} ct \quad \text{when } \delta \sim 1 \Rightarrow \delta_H > \alpha \quad (p = \alpha \rho c^2)$$

Gaussian fluctn's with  $\langle \delta_H^2 \rangle^{1/2} = \varepsilon(M)$

$\Rightarrow$  fraction of PBHs

$$\beta(M) \sim \varepsilon(M) \exp \left[ -\frac{\alpha^2}{2\varepsilon(M)^2} \right]$$



$p=0 \Rightarrow$  need spherical symmetry  $\Rightarrow \beta(M) \sim 0.06 \varepsilon(M)^6$

(Khlopov & Polnarev 1982)

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### PBHS AND INFLATION

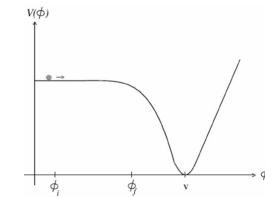
PBHs formed before reheat inflated away  $\Rightarrow$

$$M > M_{\min} = M_{\text{Pl}} (T_{\text{reheat}} / T_{\text{Pl}})^{-2} > 1 \text{ gm}$$

CMB quadrupole  $\Rightarrow T_{\text{reheat}} < 10^{16} \text{ GeV}$

But inflation generates fluctuations

$$\frac{\delta \rho}{\rho} \sim \left[ \frac{V^{3/2}}{M_{\text{Pl}}^3 V'} \right]_H$$



Can these generate PBHs?

[HUGE NUMBER OF PAPERS ON THIS]

10

### Fraction of Universe collapsing

$\beta(M)$  fraction of density in PBHs of mass  $M$  at formation

General limit

$$\frac{\rho_{\text{PBH}}}{\rho_{\text{CMB}}} \approx \frac{\Omega_{\text{PBH}}}{10^{-4}} \left[ \frac{R}{R_0} \right] \Rightarrow \beta \sim 10^{-6} \Omega_{\text{PBH}} \left[ \frac{t}{\text{sec}} \right]^{1/2} \sim 10^{-18} \Omega_{\text{PBH}} \left[ \frac{M}{10^{15} \text{ g}} \right]^{1/2}$$

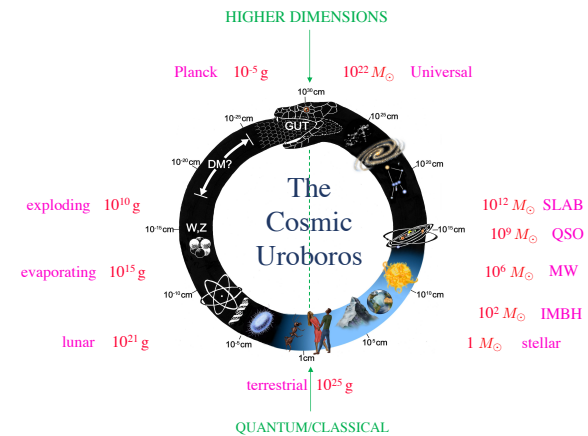
So both require and expect  $\beta(M)$  to be tiny

Fraction of dark matter  $f_{\text{DM}} \sim (\beta / 10^{-9}) (M/M_\odot)^{-1/2}$

Fine-tuning problem!

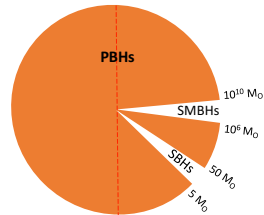
11

### BLACK HOLES AS LINK BETWEEN MICRO AND MACRO PHYSICS



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## ARE MOST BLACK HOLES PRIMORDIAL?



God would be cruel not to populate whole Uroborus!

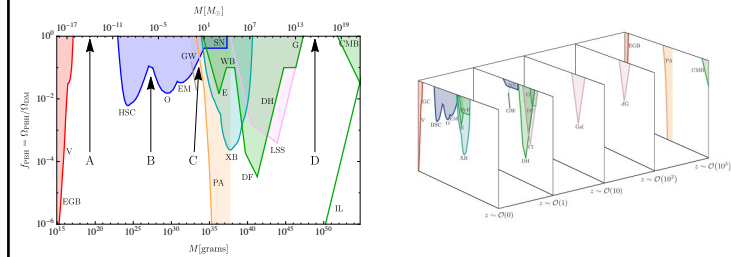
13

## Primordial Black Holes as Dark Matter: Recent Developments

Bernard Carr<sup>1,\*</sup> and Florian Kühnel<sup>2,†</sup>

Annu. Rev. Nucl. Part. Sci. 2020. 70:14.1–14.40

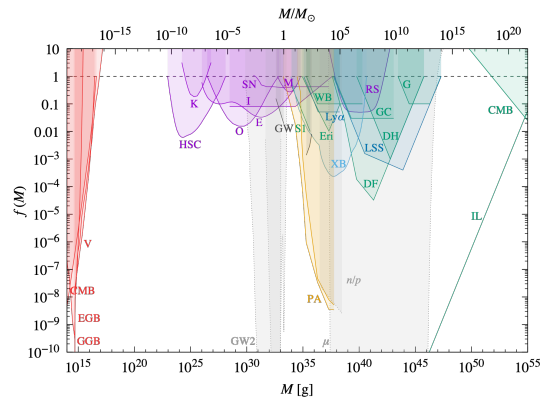
arXiv:2006.02838



Five windows where  $f_{\text{PBH}}$  can be appreciable: (A) asteroid mass; (B) sublunar mass; (C) intermediate mass; (D) stupendously massive; (E) Planck mass evaporation relics.

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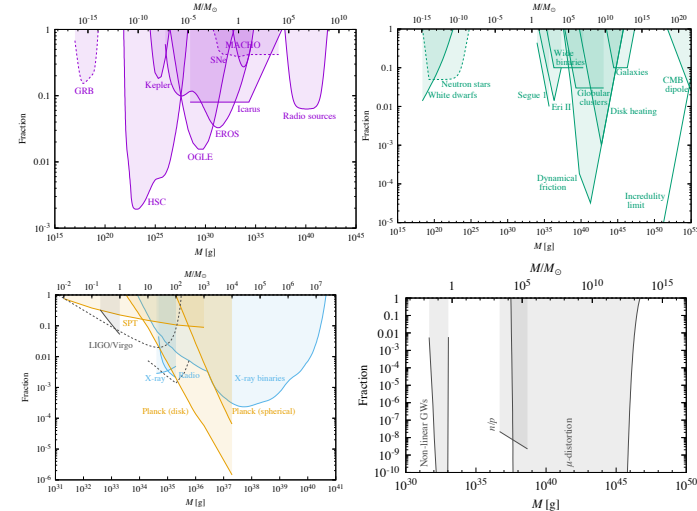
## More Detailed Constraints on PBH Dark Matter Fraction



B. Carr, K. Kohri, Y. Sendouda & J. Yokoyama  
Progress Theoretical Physics (2020), arXiv:2002.12778

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## LENSING, DYNAMICAL, ACCRETION AND COSMOLOGICAL LIMITS



16



## EXTENDED MASS FUNCTION

Most constraints assume monochromatic PBH mass function

Can we evade standard limits with extended mass spectrum?

But this is two-edged sword!

PBHs may be dark matter even if fraction is low at each scale

PBHs giving dark matter at one scale may violate limits at others

### PBH CONSTRAINTS FOR EXTENDED MASS FUNCTIONS

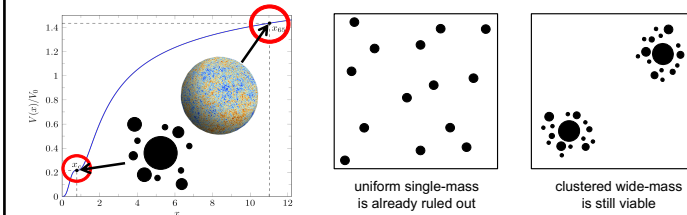
Carr, Raidal, Tenkanen, Vaskonen & Veermäe (arXiv:1705.05567)

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## Clustering

★ Many inflationary scenarios yield a lognormal PBH mass distribution.

→ This leads to clusters of 100 – 1000 PBHs with extend  $\sim 1$  Mpc.



Trashorras et al. arXiv:2006.15018

★ Always expect Poisson clustering (many recent papers)

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## PBH Constraints — Comments

★ These constraints are not just nails in a coffin!



★ All constraints have caveats and may change.

★ PBHs are interesting even for  $f_{\text{PBH}} \ll 1$ .

★ Each constraint is a potential signature.

★ PBHs generically have an extended mass function.

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## PRIMORDIAL BLACK HOLES AS DARK MATTER

### PRO

- \* Black holes exist
- \* No new physics needed
- \* LIGO results

### CON

- \* Requires fine-tuning

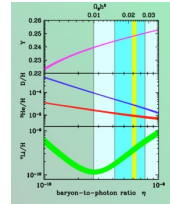
### PBH can do it!



20

# BLACK HOLES COULD BE DARK MATTER ONLY IF PRIMORDIAL

$$\text{BBNS} \Rightarrow \Omega_{\text{baryon}} = 0.05$$



$$\Omega_{\text{vis}} = 0.01, \Omega_{\text{dm}} = 0.25 \Rightarrow \text{need baryonic and non-baryonic DM}$$

↑ MACHOs      ↑ WIMPs

PBHs are non-baryonic with features of both WIMPs and MACHOs

21

## Cosmological effects of primordial black holes

GEORGE F. CHAPLINE

Nature **253**, 251–252 (24 January 1975)  
doi:10.1038/253251a0  
Download Citation

Received: 29 July 1974  
Revised: 03 October 1974  
Published online: 24 January 1975

### Abstract

ALTHOUGH only black holes with masses  $\geq 1.5M_{\odot}$  are expected to result from stellar evolution<sup>1</sup> black holes with much smaller masses may be present throughout the Universe<sup>2</sup>. These small black holes are the result of density fluctuations in the very early Universe. Density fluctuations on very large mass scales were certainly present in the early universe as is evident from the irregular distribution of galaxies in the sky<sup>3</sup>. Evidence of density fluctuations on scales smaller than the size of galaxies is generally thought to have been destroyed during the era of radiation recombination<sup>4</sup>. But fluctuations in the metric of order unity may be fossilised in the form of black holes. Observation of black holes, particularly those with masses  $M < M_{\odot}$ , could thus provide information concerning conditions in the very early Universe.

First paper on PBHs as dark matter

22

Astron. & Astrophys. **38**, 5–13 (1975)

## Primeval Black Holes and Galaxy Formation

P. Mészáros  
Institute of Astronomy, University of Cambridge  
Received September 4, revised October 14, 1974

**Summary.** We present a scheme of galaxy formation, based on the hypothesis that a certain fraction of the mass of the early universe is in the form of black holes. It is argued that the black hole mass should be  $\sim 1 M_{\odot}$ , and it is shown that random statistical fluctuations in their number cause density fluctuations which grow in time. The advantage over the usual baryon fluctuations are twofold:  $\delta N/N$  is much larger for black holes than for baryons, and the black holes are not electromagnetically coupled to the radiation field, as the baryons are. One is thus able to achieve galaxy and cluster formation at the right redshifts, and at the same time

the black holes would account for the recently proposed massive halos of galaxies, and for the hidden mass in clusters required by virial theorem arguments. The number of free parameters in this theory is less than, or at most equal to, that in the current "primeval fluctuations" theory, while the physical picture that is achieved seems more satisfactory, from a self-consistency point of view.

**Key words:** galaxy formation — primeval black holes — hidden mass — cosmology

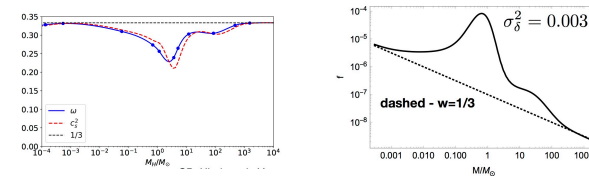
PBHs relevant to galaxy formation if dark matter

23

## Primordial black holes with an accurate QCD equation of state

Christian T. Byrnes,<sup>1,\*</sup> Mark Hindmarsh,<sup>1,2,†</sup> Sam Young,<sup>1,‡</sup> and Michael R. S. Hawkins<sup>3,§</sup>

arXiv:1801.06138



Jedamzik (1996)

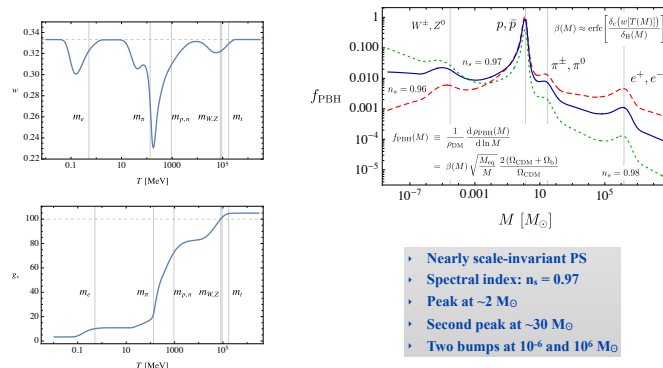
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## Cosmic Conundra Explained by Thermal History and Primordial Black Holes

Bernard Carr,<sup>1,2,\*</sup> Sébastien Clesse,<sup>3,4,†</sup> Juan García-Bellido,<sup>5,‡</sup> and Florian Kühnel<sup>6,§</sup>

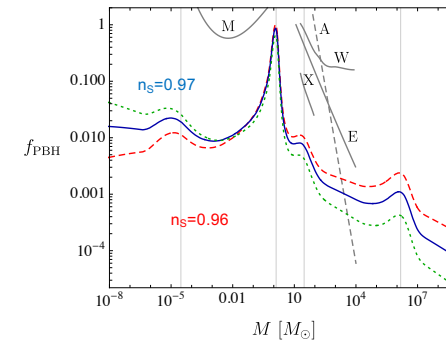
arXiv:1906.08217

Extend this to include other stages in thermal history



25

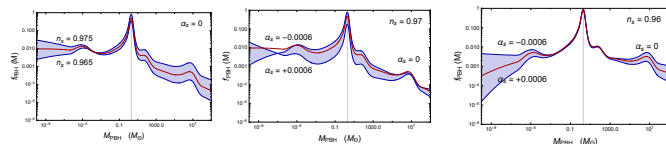
## CONSTRAINTS

Overproduce light PBHs for  $n_s > 0.975$ Overproduce heavy PBHs for  $n_s < 0.965$ 

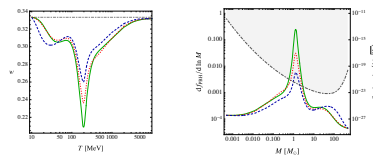
26

## Effect of spectral tilt

CCGHK



## Effect of lepton flavour asymmetries Bodeker et al. PRD 103, 063506

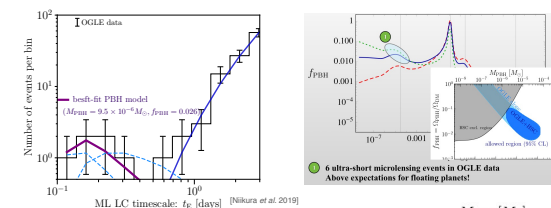


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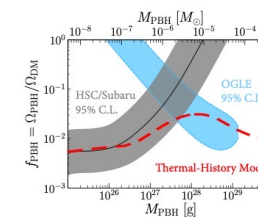
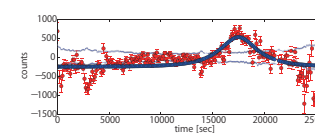
## Planetary-mass microlenses

OGLE detected microlenses on 0.1-0.3 day timescale of unknown origin

Niikura et al. arXiv:1901.07120



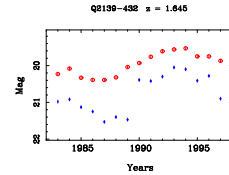
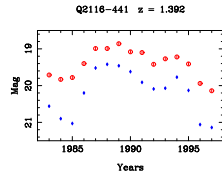
Niikura et al. arXiv:1701.02151



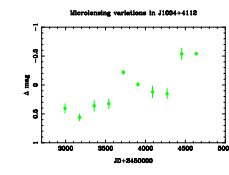
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## Quasar Lensing

### Caustic crossing

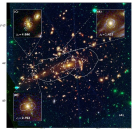


### Multiply lensed quasar

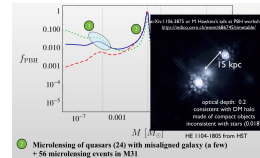


=> cos' distrib'n of  $1M_{\odot}$  PBHs

### Galaxy-galaxy strong lensing



MACSJ1206  
=> more DM substructure  
than expected in CDM  
Meneghetti et al. (2020)



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## HALO MICROLENSING EVIDENCE

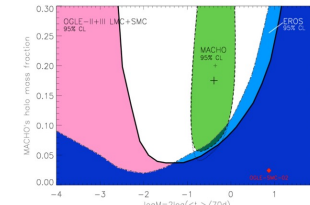
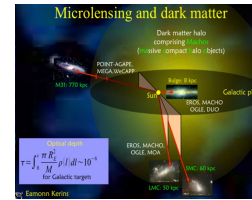


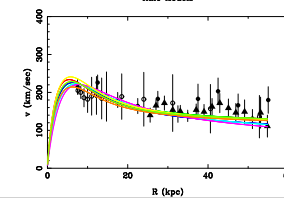
Image credit: Wyrzykowski et al., 2011, MNRAS, (astro-ph/1005.2925).

Early microlensing searches suggested MACHOs with  $0.5 M_{\odot}$

=> PBH formation at QCD transition?

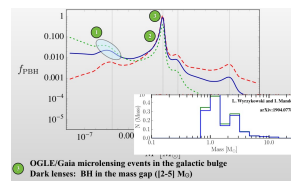
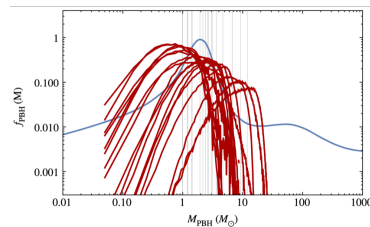
Later found that at most 20% of DM

But this assume flat rotation curves  
and more recent models allow 100%



30

## OGLE/GAIA Excess of Lenses in Galactic Bulge



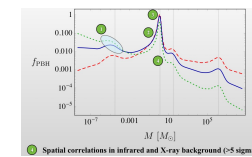
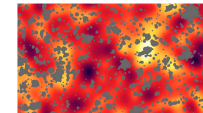
OGLE/Gaia microlensing events in the galactic bulge  
Dark lenses: BH in the mass gap (2-5  $M_{\odot}$ )

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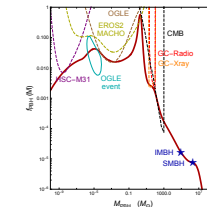
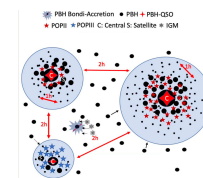
## Cosmic infrared/X-ray backgrounds

Spatial coherence of X and IR source-subtracted backgrounds  
=> overabundance of high-z halos => PBH Poisson effect

Kashlinsky arXiv:1605.04023



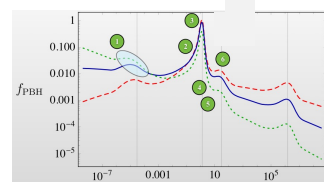
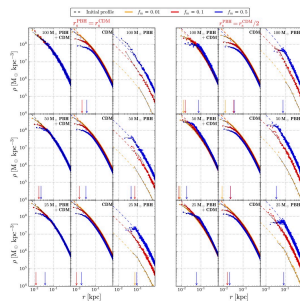
Cappelluti et al. arXiv:2109.08701



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### Ultra-Faint Dwarf Galaxies

PBH dark matter => UFDGs unstable below some radius  
Non-detection of galaxies smaller than 10-20pc => PBHs?



Improved constraints from ultra-faint dwarf galaxies on PBHs as DM  
Stegmann et al [arXiv:1910.04793](https://arxiv.org/abs/1910.04793)

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### CUSP/CORE PROBLEM

CDM => cuspy DM halos => stellar feedback or WIMP self-interaction

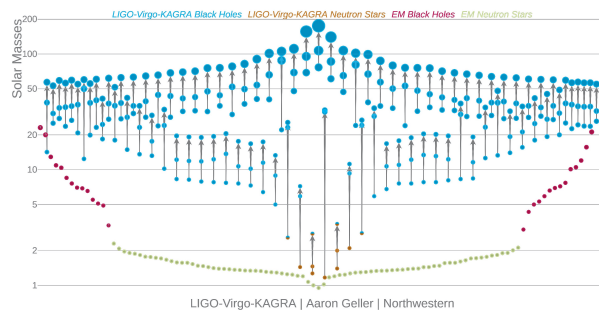
$10^7 M_\odot$  dwarf galaxies + 1% DM in 25-100  $M_\odot$  PBHs resolves problem

PBHs => cusp-to-core transition in low-mass dwarf galaxies  
[Boldrini et al. arXiv:1909.07395](https://arxiv.org/abs/1909.07395)

Break in distribution of halo wide binaries =>  $M > 10 M_\odot$  (Tien)

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### PBHs AND LIGO/Virgo/KAGRA



Do we need PBHs?

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Merger at early or late times?

[Bird et al. arXiv:1603.00464](https://arxiv.org/abs/1603.00464) [Sasaki et al. arXiv:1603.08338](https://arxiv.org/abs/1603.08338)

Poisson clustering boosts merging rate at late times

PBHs of 30  $M_\odot$  can only provide 0.1-1% of DM

PBHs of 1  $M_\odot$  can only provide 100% of DM  
=> late ~ early ~ neutron star => could be PBHs

BHs in pair-instability and low mass gaps

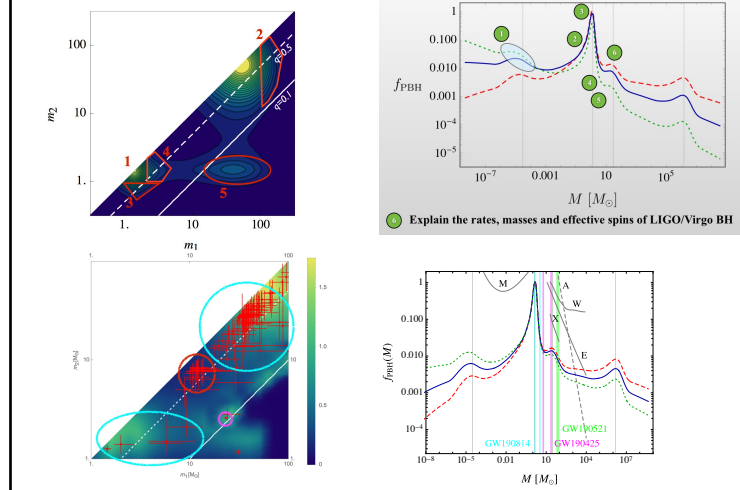
Extended mass function => asymmetric masses  
challenging astrophysical models

Subsolar candidates?

Mass, spin and redshift distribution will determine

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## LIGO/Virgo Black Holes

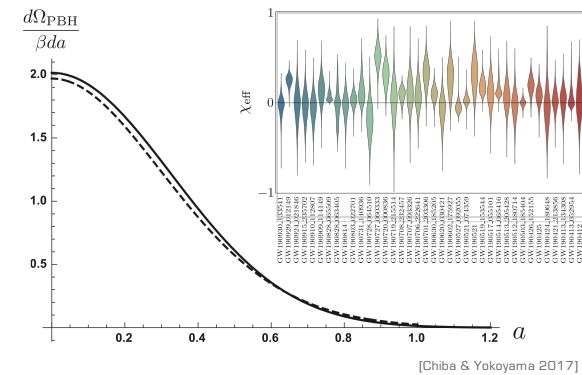


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## Spin Distribution

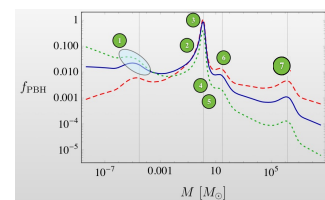
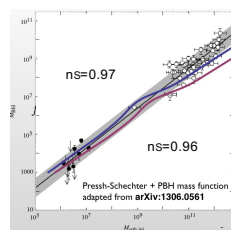
★ Gravitational-wave emission from black-hole binaries

★ For PBH (produced in RD) we expect close to zero spin.



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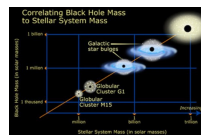
## Intermediate and supermassive black holes



Right number of intermediate and supermassive black holes

$n_s = 0.97 \Rightarrow$  observed ratio of  
BH and halo mass if  $f_{PBH} \sim 1$ .

But accretion important



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## OTHER COSMIC PROBLEMS

- \* Fast radio bursts
- \* Missing pulsar problem
- \* Hubble tension
- \* Non-flat rotation curves at high redshift
- \* High velocity stars
- \* Low mass X-ray binaries

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## ADDRESSING FINE-TUNING PROBLEM AT QCD EPOCH

Carr, Clesse &amp; Garcia-Bellido, arXiv:1904.02129

PBHs forming at time  $t$  have mass and collapse fraction  
 $M \sim 10^5 (t/s) M_\odot$ ,  $\beta(M) \sim 10^{-9} f(M) (M/M_\odot)^{1/2}$

So  $\beta$  appears fine-tuned and we must also explain why  
 $\chi = \rho_{\text{PBH}}/\rho_B = f \rho_{\text{DM}}/\rho_B = 6 f$  is  $O(1)$ .

$\chi \gg 1 \Rightarrow t_{\text{eq}} \ll t_{\text{dec}} \Rightarrow$  not enough baryons to make galaxies  
 $\chi \ll 1 \Rightarrow t_{\text{dec}} \gg t_{\text{dec}} \Rightarrow$  fluctuations too small to make galaxies

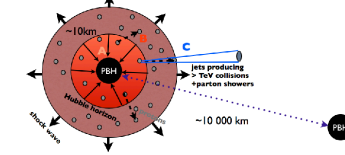
QCD epoch  $\Rightarrow M \sim M_C$ ,  $\beta(M) \sim \eta = n_B/n_\gamma \sim 10^{-9}$  **anthropic selection?**  
 dark matter and visible baryons have similar mass  
 $\Rightarrow$  PBHs may *generate* baryon asymmetry

$M_C \sim \alpha_G^{-3/2} m_P \sim 1 M_\odot$  and all stars have mass in range  $(0.1-10) M_\odot$

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## Primordial Black Holes

as a common origin of baryons and dark matter

Garcia-Bellido, Carr, Clesse  
arXiv:1904.114827

- C and CP violation of the standard model (CKM matrix)
- Baryon number violation: sphaleron transitions from  $> \text{TeV}$  collisions
- Out of thermal equilibrium (PBH collapse)

$$\chi \approx \gamma/(1 - \gamma) \approx 5 \text{ if } \gamma \approx 0.8$$

$\eta_{\text{loc}} \sim 1 \Rightarrow \eta \sim \beta$  and  $\chi \sim 1$  after diffusion of baryon asymmetry

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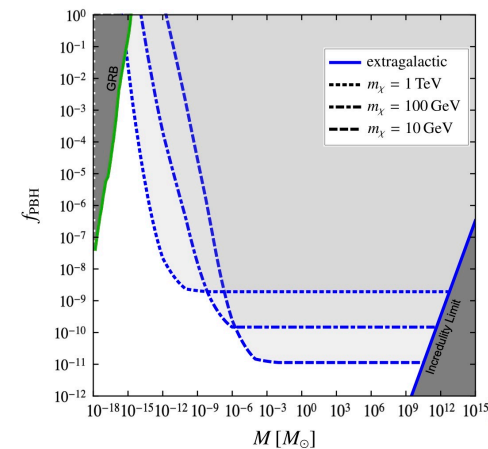
## PBH + Particle DM

- ★ Always when  $f_{\text{PBH}} < 1$  there **must** be another DM component!
- ★ Study a **combined** scenario: DM = PBHs + Particles
  - ★ The latter will be **accreted** by the former; **formation of halos**.
  - ★ Study **WIMP annihilations** in PBH halos:
    - ★ The annihilation rate  $\Gamma \propto n^2$ .
    - ★ Halo profile  $\Rightarrow$  **enhancement** of  $\Gamma$  in density spikes.
      - 1) Derive the **density profile** of the captured WIMPs;
      - 2) calculate the **annihilation rate**;
      - 3) and **compare to extragalactic gamma-ray background**.

[Eroshenko 2016, Boucenna *et al.* 2017, Adamek *et al.* 2019, BC, FK, Visinelli 2020 & 2021]

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## PBHs &amp; WIMPs - Constraints

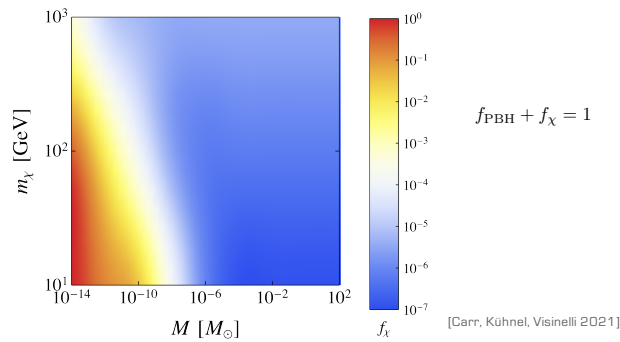


[BC, FK, Visinelli 2021]

If the LIGO/Virgo black holes are primordial, this would **rule out** any standard WIMP scenario!

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## PBHs &amp; WIMPs - Constraints



- ★ Even for small values of  $f_{\text{PBH}}$ ,  $f_{\chi}$  is heavily constrained.
- ★ For  $M_{\text{PBH}} \gtrsim 10^{-11} M_{\odot}$  and  $m_{\chi} \lesssim 100 \text{ GeV}$ , both the WIMP and PBH fractions are  $\mathcal{O}(10\%)$ .

→ Motivates a third dark-matter candidate?

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## CONCLUSIONS

PBH studies have already led to profound insights into cosmology and fundamental physics, even if they never formed.

Until recently most work focused on PBH constraints but now they have been invoked for numerous cosmological purposes:

Dark matter

LIGO/Virgo

SMBH seeds

These are distinct roles but PBHs with extended mass function could play all of them with fine-tuning of collapse fraction.

PBHs naturally form at QCD epoch and could explain both dark matter and baryon asymmetry with anthropic fine-tuning.

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