



*Mon. Not. R. astr. Soc.* (1971) **152**, 75-78.

GRAVITATIONALLY COLLAPSED OBJECTS OF VERY LOW MASS

*Stephen Hawking*

(Communicated by M. J. Roes)  
(Received 1970 November 9)

SUMMARY

It is suggested that there may be a large number of gravitationally collapsed objects of mass  $10^{-6}$  g upwards which were formed as a result of fluctuations in the early Universe. They could carry an electric charge of up to  $\pm 30$  electron units. Such objects would produce distinctive tracks in bubble chambers and could form atoms with orbiting electrons or protons. A mass of  $10^{17}$  g of such objects could have accumulated at the centre of a star like the Sun. If such a star later became a neutron star there would be a steady accretion of matter by a central collapsed object which could eventually swallow up the whole star in about ten million years.



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### Black hole explosions? *Nature* 248, 30 - 31 (01 March 1974)

S. W. HAWKING

Quantum Mechanics

Thermodynamics

General Relativity

$T_{BH} [K] = 10^{-7} \frac{M_{\odot}}{M}$

**PBHs are important even if they never formed!**

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### PBH FORMATION ..... AND EVAPORATION

$R_s = 2GM/c^2 = 3(M/M_{\odot}) \text{ km} \Rightarrow \rho_s = 10^{18}(M/M_{\odot})^{-2} \text{ g/cm}^3$

cf. cosmological density  $\rho \sim 1/(Gt^2) \sim 10^6(t/s)^{-2} \text{ g/cm}^3$   
 $\Rightarrow$  **primordial BHs with horizon mass at formation**

$10^{-5} \text{ g at } 10^{-43} \text{ s}$  (minimum?)  
 $M_{PBH} \sim c^3 t / G = 1M_{\odot} \text{ at } 10^{-5} \text{ s}$  (QCD transition)  
 $10^5 M_{\odot} \text{ at } 1 \text{ s}$  (maximum?)

**Black holes radiate thermally with temperature**

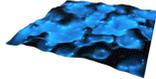
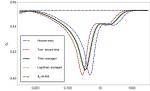
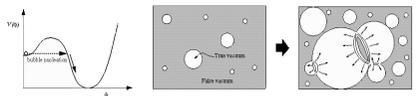
$T = \frac{hc^3}{8\pi GkM} \sim 10^{-7} \left[ \frac{M}{M_{\odot}} \right]^{-1} \text{ K}$

$\Rightarrow$  **evaporate completely in time**  $t_{\text{evap}} \sim 10^{64} \left[ \frac{M}{M_{\odot}} \right]^3 \text{ y}$

$M \sim 10^{15} \text{ g} \Rightarrow$  **final explosion phase today ( $10^{30}$  ergs)**

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### Formation Mechanisms of Primordial Black Holes

- ★ Large density perturbations (inflation) 
- ★ Pressure reduction 
- ★ Cosmic string loops 
- ★ Bubble collisions 

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**PBH FORMATION => LARGE INHOMOGENEITIES**

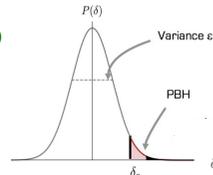
To collapse against pressure, need (Carr 1975)

$$R > \sqrt{\alpha} ct \text{ when } \delta \sim 1 \Rightarrow \delta_H > \alpha \quad (p = \alpha \rho c^2)$$

Gaussian fluctn's with  $\langle \delta_H^2 \rangle^{1/2} = \epsilon(M)$

=> fraction of PBHs

$$\beta(M) \sim \epsilon(M) \exp\left[-\frac{\alpha^2}{2\epsilon(M)^2}\right]$$



p=0 => need spherical symmetry =>  $\beta(M) \sim 0.06 \epsilon(M)^6$

(Khlopov & Polnarev 1982)

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**PBHS AND INFLATION**

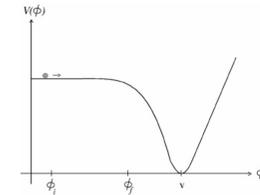
PBHs formed before reheat inflated away =>

$$M > M_{\min} = M_{\text{pl}}(T_{\text{reheat}} / T_{\text{pl}})^{-2} > 1 \text{ gm}$$

CMB quadrupole =>  $T_{\text{reheat}} < 10^{16} \text{ GeV}$

But inflation generates fluctuations

$$\frac{\delta\rho}{\rho} \sim \left[ \frac{V^{3/2}}{M_{\text{pl}}^3 V'} \right]_H$$



Can these generate PBHs?

[HUGE NUMBER OF PAPERS ON THIS]

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**Fraction of Universe collapsing**

$\beta(M)$  fraction of density in PBHs of mass M at formation

General limit

$$\frac{\rho_{\text{PBH}}}{\rho_{\text{CMB}}} \approx \frac{\Omega_{\text{PBH}}}{10^{-4}} \left[ \frac{R}{R_0} \right] \Rightarrow \beta \sim 10^{-6} \Omega_{\text{PBH}} \left[ \frac{t}{\text{sec}} \right]^{1/2} \sim 10^{-18} \Omega_{\text{PBH}} \left[ \frac{M}{10^{15} \text{ g}} \right]^{1/2}$$

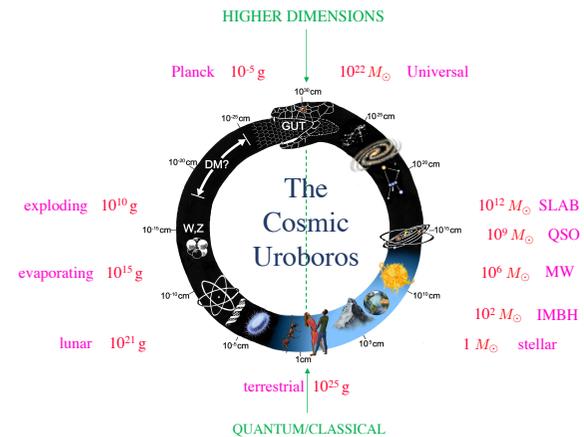
So both require and expect  $\beta(M)$  to be tiny

Fraction of dark matter  $f_{\text{DM}} \sim (\beta / 10^{-9}) (M/M_{\odot})^{-1/2}$

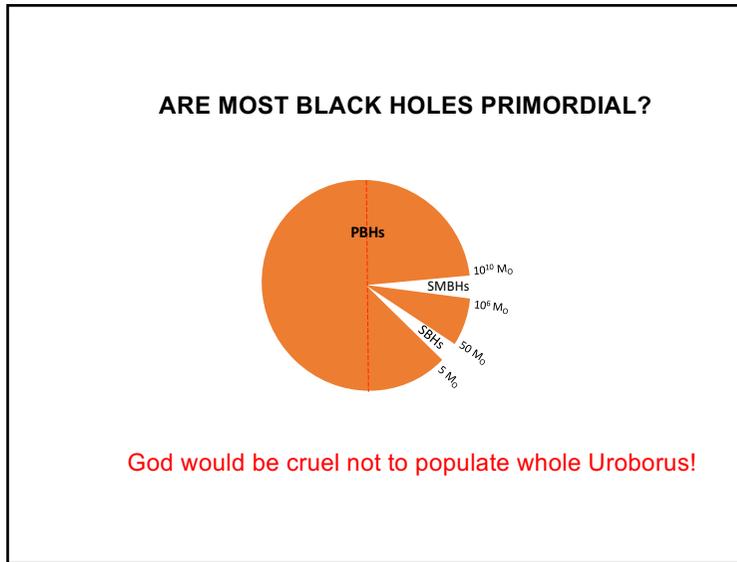
Fine-tuning problem!

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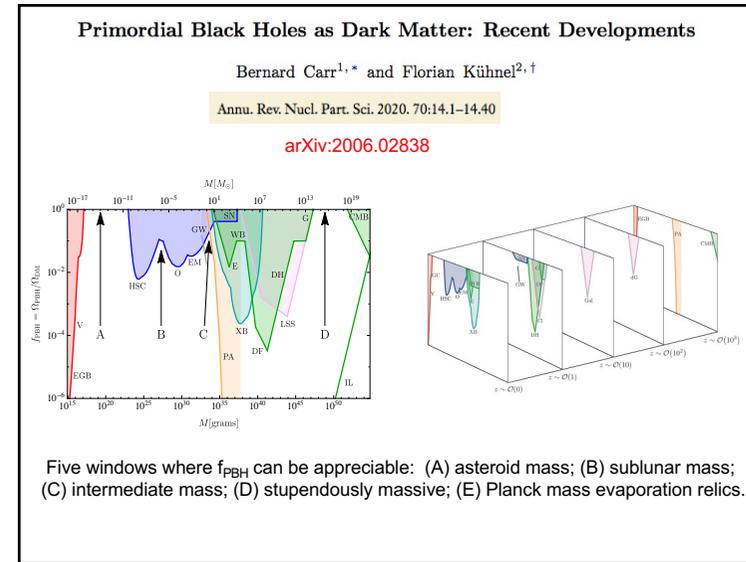
**BLACK HOLES AS LINK BETWEEN MICRO AND MACRO PHYSICS**



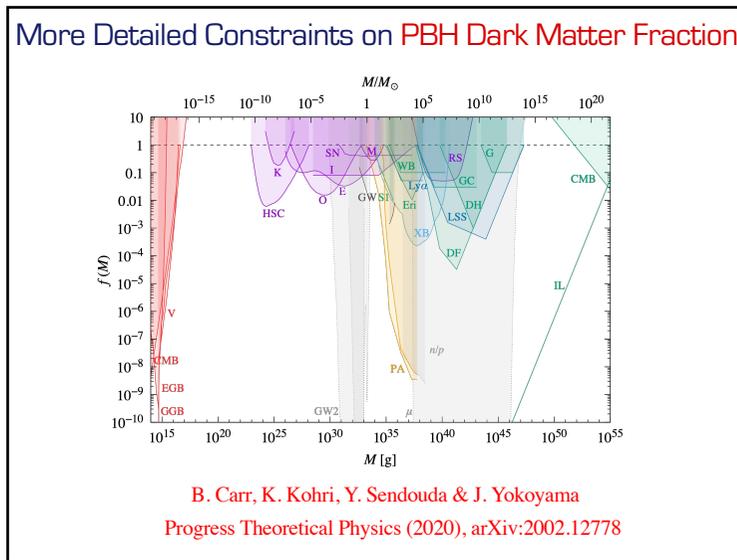
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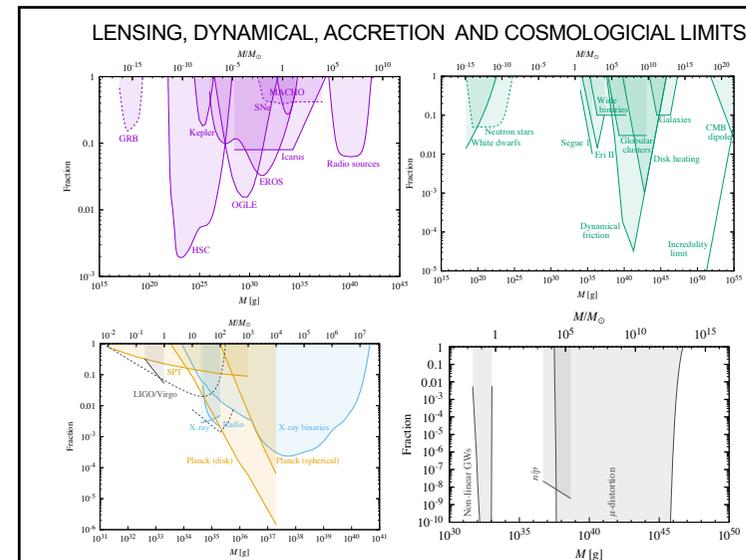
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### EXTENDED MASS FUNCTION

Most constraints assume monochromatic PBH mass function

Can we evade standard limits with extended mass spectrum?

**But this is two-edged sword!**

PBHs may be dark matter even if fraction is low at each scale

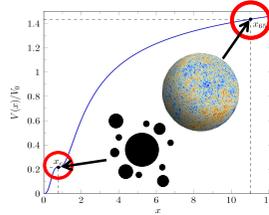
PBHs giving dark matter at one scale may violate limits at others

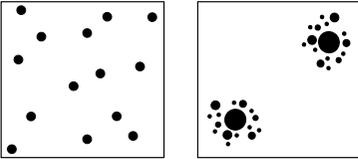
**PBH CONSTRAINTS FOR EXTENDED MASS FUNCTIONS**  
Carr, Raidal, Tenkanen, Vaskonen & Veermäe (arXiv:1705.05567)

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### Clustering

- ★ Many inflationary scenarios yield a lognormal PBH mass distribution.
- This leads to clusters of 100 – 1000 PBHs with extend ~ 1 Mpc.





Trashorras et al. arXiv:2006.15018

- ★ Always expect Poisson clustering (many recent papers)

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### PBH Constraints — Comments

- ★ These constraints are not just nails in a coffin!



- ★ All constraints have caveats and may change.
- ★ PBHs are interesting even for  $f_{PBH} \ll 1$ .
- ★ Each constraint is a potential signature.
- ★ PBHs generically have an extended mass function.

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### PRIMORDIAL BLACK HOLES AS DARK MATTER

**PRO**

- \* Black holes exist
- \* No new physics needed
- \* LIGO results

**CON**

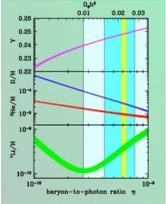
- \* Requires fine-tuning



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**BLACK HOLES COULD BE DARK MATTER ONLY IF PRIMORDIAL**

BBNS  $\Rightarrow \Omega_{\text{baryon}} = 0.05$



$\Omega_{\text{vis}} = 0.01, \Omega_{\text{dm}} = 0.25 \Rightarrow$  need baryonic and non-baryonic DM

↑ MACHOs      ↑ WIMPs

PBHs are non-baryonic with features of both WIMPs and MACHOs

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Cosmological effects of primordial black holes

GEORGE F. CHAPLINE

Nature 253, 251–252 (24 January 1975)  
doi:10.1038/253251a0  
Download Citation

Received: 29 July 1974  
Revised: 03 October 1974  
Published online: 24 January 1975

**Abstract**

ALTHOUGH only black holes with masses  $\geq 1.5M_{\odot}$  are expected to result from stellar evolution<sup>1</sup> black holes with much smaller masses may be present throughout the Universe<sup>2</sup>. These small black holes are the result of density fluctuations in the very early Universe. Density fluctuations on very large mass scales were certainly present in the early universe as is evident from the irregular distribution of galaxies in the sky<sup>3</sup>. Evidence of density fluctuations on scales smaller than the size of galaxies is generally thought to have been destroyed during the era of radiation recombination<sup>4</sup>. But fluctuations in the metric of order unity may be fossilised in the form of black holes. Observation of black holes, particularly those with masses  $M < M_{\odot}$ , could thus provide information concerning conditions in the very early Universe.

First paper on PBHs as dark matter

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Astron. & Astrophys. 38, 5–13 (1975)

**Primeval Black Holes and Galaxy Formation**

P. Mészáros  
Institute of Astronomy, University of Cambridge  
Received September 4, revised October 14, 1974

**Summary.** We present a scheme of galaxy formation, based on the hypothesis that a certain fraction of the mass of the early universe is in the form of black holes. It is argued that the black hole mass should be  $\sim 1 M_{\odot}$  and it is shown that random statistical fluctuations in their number cause density fluctuations which grow in time. The advantage over the usual baryon fluctuations are twofold:  $\delta N/N$  is much larger for black holes than for baryons, and the black holes are not electromagnetically coupled to the radiation field, as the baryons are. One is thus able to achieve galaxy and cluster formation at the right redshifts, and at the same time

the black holes would account for the recently proposed massive halos of galaxies, and for the hidden mass in clusters required by virial theorem arguments. The number of free parameters in this theory is less than, or at most equal to, that in the current "primeval fluctuations" theory, while the physical picture that is achieved seems more satisfactory, from a self-consistency point of view.

**Key words:** galaxy formation — primeval black holes — hidden mass — cosmology

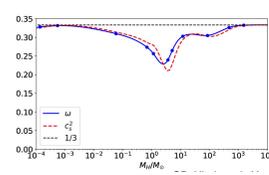
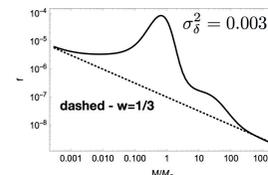
PBHs relevant to galaxy formation if dark matter

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**Primordial black holes with an accurate QCD equation of state**

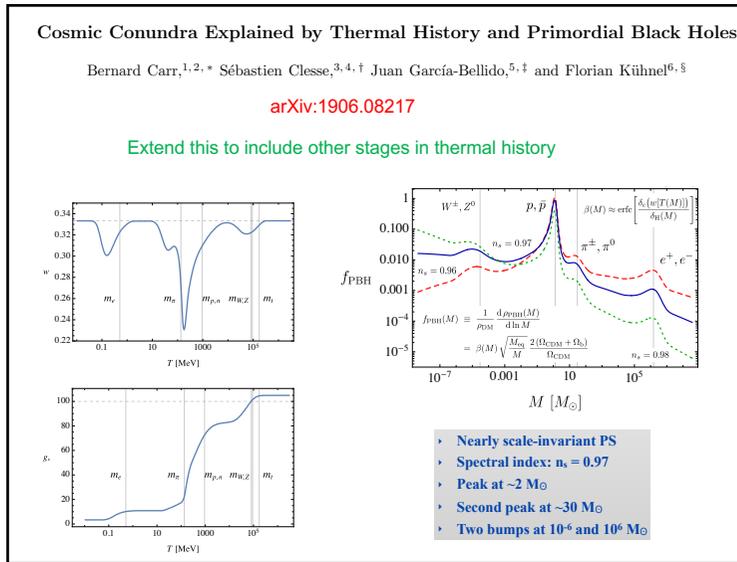
Christian T. Byrnes,<sup>1,\*</sup> Mark Hindmarsh,<sup>1,2,†</sup> Sam Young,<sup>1,‡</sup> and Michael R. S. Hawkins<sup>3,§</sup>

arXiv:1801.06138

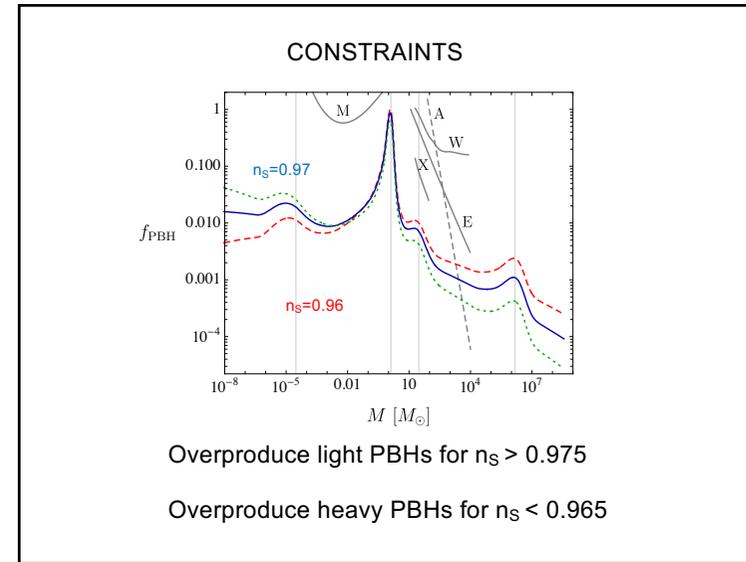



Jedamzik (1996)

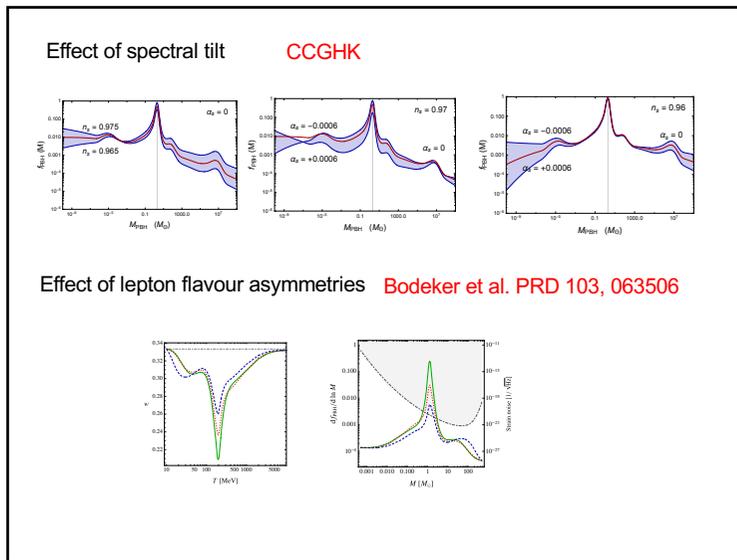
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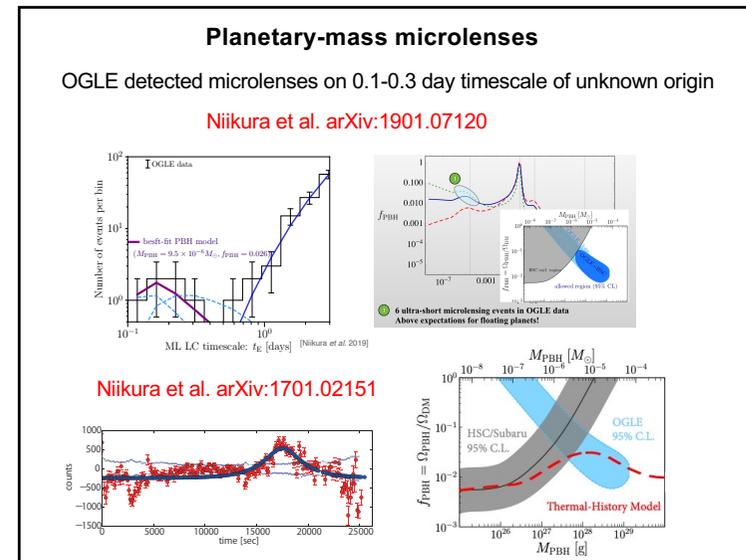
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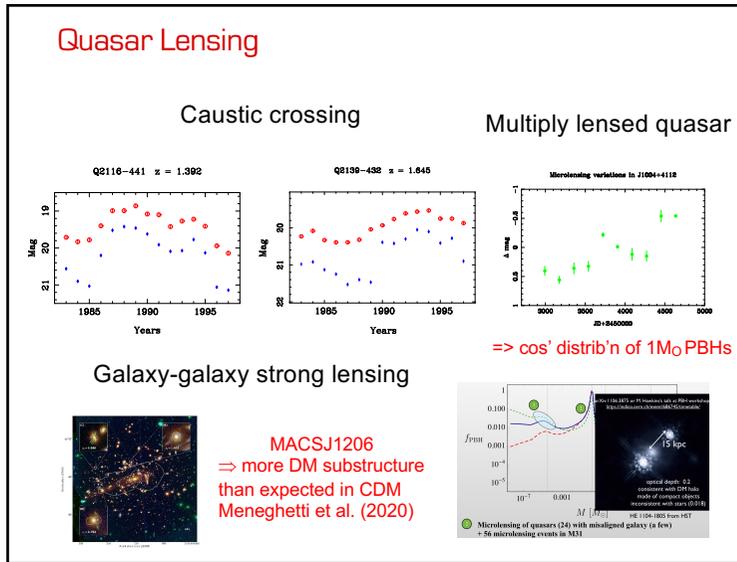
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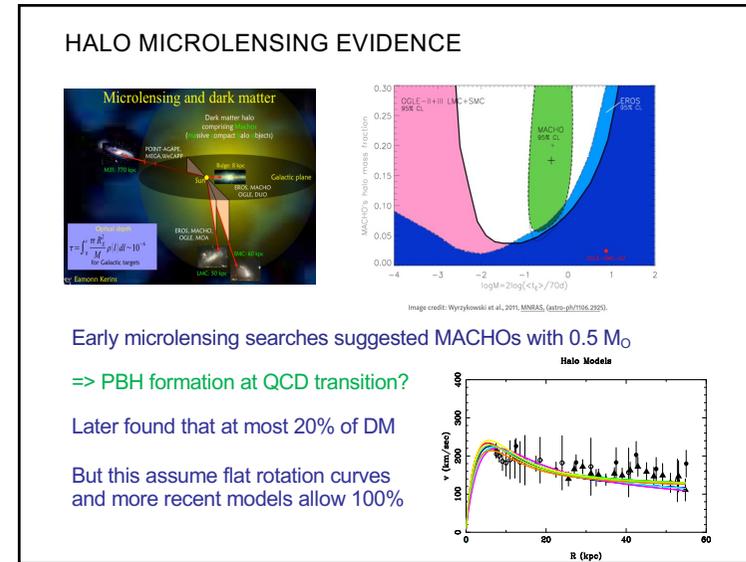
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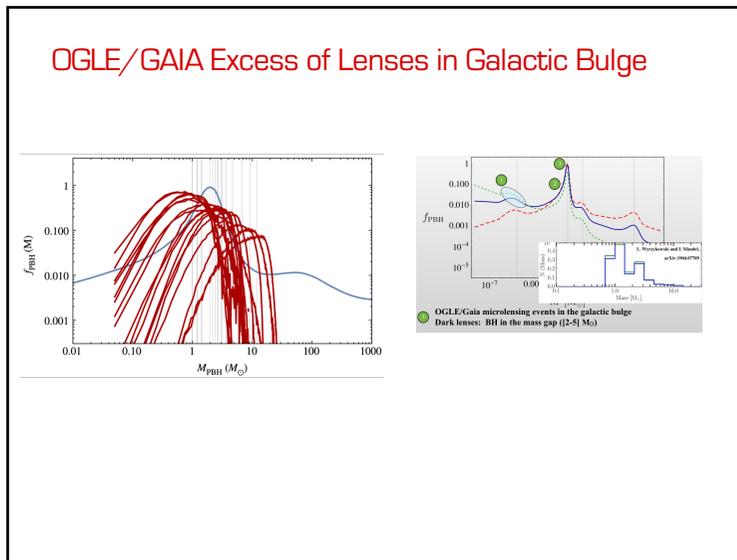
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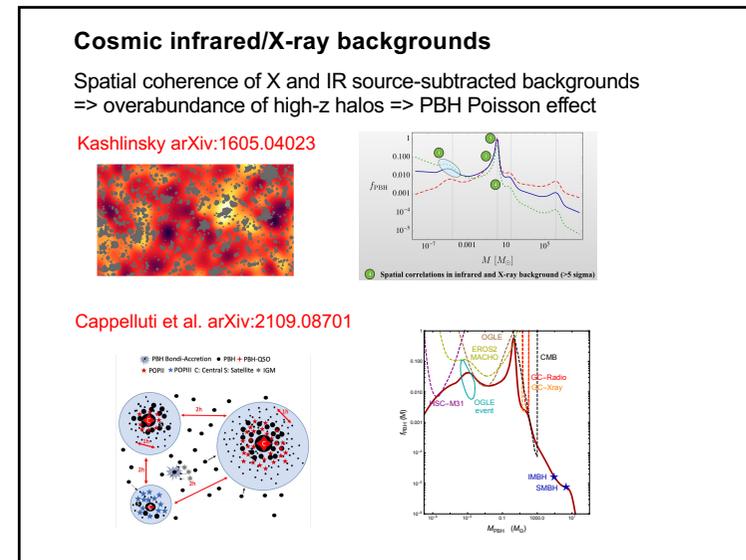
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### Ultra-Faint Dwarf Galaxies

PBH dark matter => UFDGs unstable below some radius  
 Non-detection of galaxies smaller than 10-20pc => PBHs?

Improved constraints from ultra-faint dwarf galaxies on PBHs as DM  
 Stegmann et al [arXiv:1910.04793](https://arxiv.org/abs/1910.04793)

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### CUSP/CORE PROBLEM

CDM => cuspy DM halos => stellar feedback or WIMP self-interaction

10<sup>7</sup>M<sub>⊙</sub> dwarf galaxies + 1% DM in 25-100 M<sub>⊙</sub> PBHs resolves problem

PBHs => cusp-to-core transition in low-mass dwarf galaxies  
[Boldrini et al. arXiv:1909.07395](https://arxiv.org/abs/1909.07395)

Break in distribution of halo wide binaries => M > 10M<sub>⊙</sub> (Tien)

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### PBHS AND LIGO/Virgo/KAGRA

LIGO-Virgo-KAGRA | Aaron Geller | Northwestern

Do we need PBHs?

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Merger at early or late times?  
[Bird et al. arXiv:1603.00464](https://arxiv.org/abs/1603.00464) [Sasaki et al. arXiv:1603.08338](https://arxiv.org/abs/1603.08338)

Poisson clustering boosts merging rate at late times

PBHs of 30 M<sub>⊙</sub> can only provide 0.1-1% of DM

PBHs of 1 M<sub>⊙</sub> can only provide 100% of DM  
 => late ~ early ~ neutron star => could be PBHs

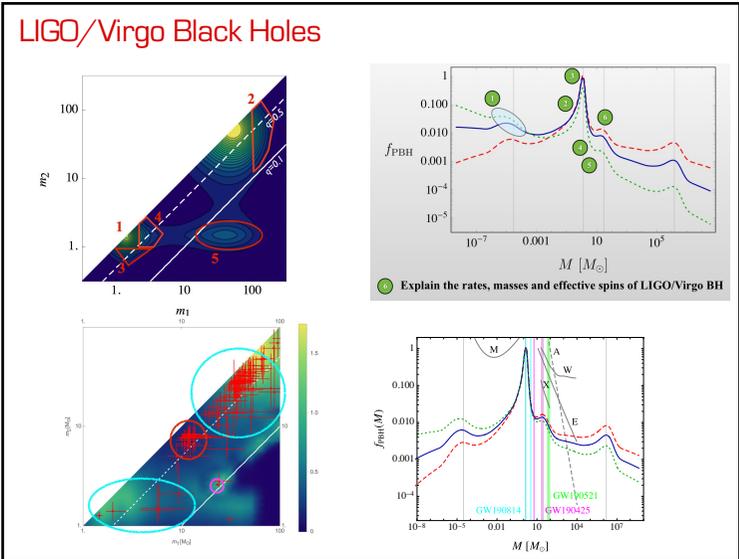
BHs in pair-instability and low mass gaps

Extended mass function => asymmetric masses  
 challenging astrophysical models

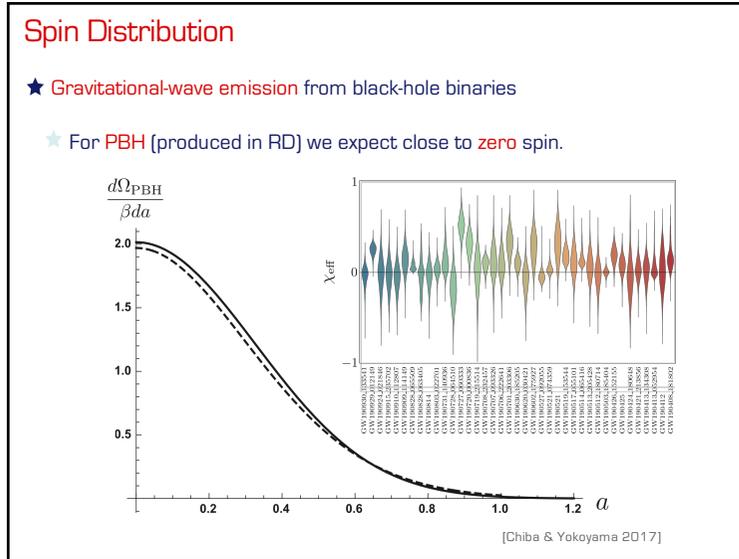
Subsolar candidates?

Mass, spin and redshift distribution will determine

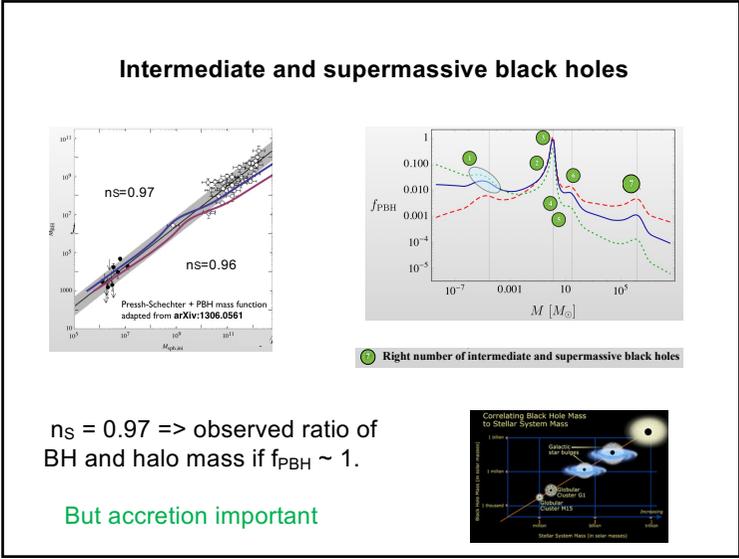
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### OTHER COSMIC PROBLEMS

- \* Fast radio bursts
- \* Missing pulsar problem
- \* Hubble tension
- \* Non-flat rotation curves at high redshift
- \* High velocity stars
- \* Low mass X-ray binaries

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**ADDRESSING FINE-TUNING PROBLEM AT QCD EPOCH**

Carr, Clesse & Garcia-Bellido, arXiv:1904.02129

PBHs forming at time  $t$  have mass and collapse fraction  
 $M \sim 10^5(t/s) M_\odot$ ,  $\beta(M) \sim 10^{-9} f(M) (M/M_\odot)^{1/2}$

So  $\beta$  appears fine-tuned and we must also explain why  
 $\chi = \rho_{\text{PBH}}/\rho_B = f \rho_{\text{DM}}/\rho_B = 6 f$  is  $O(1)$ .

$\chi \gg 1 \Rightarrow t_{\text{eq}} \ll t_{\text{dec}} \Rightarrow$  not enough baryons to make galaxies  
 $\chi \ll 1 \Rightarrow t_{\text{dec}} \gg t_{\text{eq}} \Rightarrow$  fluctuations too small to make galaxies

QCD epoch  $\Rightarrow M \sim M_C$ ,  $\beta(M) \sim \eta = n_B/n_\gamma \sim 10^{-9}$  anthropic selection?  
 $\Rightarrow$  dark matter and visible baryons have similar mass  
 $\Rightarrow$  PBHs may generate baryon asymmetry

$M_C \sim \alpha_G^{-3/2} m_p \sim 1 M_\odot$  and all stars have mass in range (0.1–10)  $M_C$

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**Primordial Black Holes**  
as a common origin of baryons and dark matter

Garcia-Bellido, Carr, Clesse  
arXiv:1904.114827

- C and CP violation of the standard model (CKM matrix)
- Baryon number violation: sphaleron transitions from  $> \text{TeV}$  collisions
- Out of thermal equilibrium (PBH collapse)

$\chi \approx \gamma/(1 - \gamma) \approx 5$  if  $\gamma \approx 0.8$

$\eta_{\text{loc}} \sim 1 \Rightarrow \eta \sim \beta$  and  $\chi \sim 1$  after diffusion of baryon asymmetry

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**PBH + Particle DM**

- ★ Always when  $f_{\text{PBH}} < 1$  there **must** be another DM component!
- ★ Study a **combined** scenario: **DM = PBHs + Particles**
  - ★ The latter will be **accreted** by the former; **formation of halos**.
  - ★ Study **WIMP annihilations** in PBH halos:
    - ★ The annihilation rate  $\Gamma \propto n^2$ .
    - ★ Halo profile  $\Rightarrow$  **enhancement** of  $\Gamma$  in density spikes.
      - 1) Derive the **density profile** of the captured WIMPs;
      - 2) calculate the **annihilation rate**;
      - 3) and **compare to extragalactic gamma-ray background**.

[Eroshenko 2016, Boucenna et al. 2017, Adamek et al. 2019, BC, FK, Visinelli 2020 & 2021]

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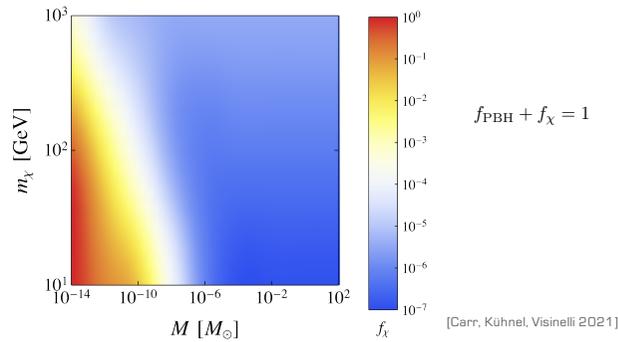
**PBHs & WIMPs - Constraints**

If the LIGO/Virgo black holes are primordial, this would rule out any standard WIMP scenario!

[BC, FK, Visinelli 2021]

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PBHs & WIMPs - Constraints



- ★ Even for small values of  $f_{\text{PBH}}$ ,  $f_{\chi}$  is heavily constrained.
  - ★ For  $M_{\text{PBH}} \gtrsim 10^{-11} M_{\odot}$  and  $m_{\chi} \lesssim 100 \text{ GeV}$ , both the WIMP and PBH fractions are  $\mathcal{O}(10\%)$ .
- Motivates a third dark-matter candidate?

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CONCLUSIONS

PBH studies have already led to profound insights into cosmology and fundamental physics, even if they never formed.

Until recently most work focused on PBH constraints but now they have been invoked for numerous cosmological purposes:



These are distinct roles but PBHs with extended mass function could play all of them with fine-tuning of collapse fraction.

PBHs naturally form at QCD epoch and could explain both dark matter and baryon asymmetry with anthropic fine-tuning.

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