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« DARK MATTER CANDIDATES IN STANDARD MODEL EXTENSIONS»

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Introduction

Practically all modern elementary particles physics is currently described by the Standard Model (SM) [1]. It's a theoretical construction that includes all known interactions at the present moment, except for the gravitational one. Though it's a mathematical representation of the physical processes of the microworld, however, it leaves unsolved a large number of questions (such as mass hierarchies problem etc.). There are many indications that SM can be a low-energy limit of some more general theory, just as Galileo's principle of relativity is a special case of Einstein's relativity principle in Newtonian mechanics. That's why the issue of the Standard Model extending to a theory that is capable to describe microworld processes more fully and in detail as well as resolve the problems existing within the SM theory is extremely actual at the moment.

For the searching of "new physics" beyond the SM, there are basically two possible ways. One of them is studying of processes with the probable creation of hypothetical new particles, the other is searching for manifestations of the "new physics" in already known interactions [2]. It should, however, be borne in mind that the experimental confirmation of the theories using the first approach may not be possible at the present time due to the probable presence of the particles of the "new physics" only at higher energies that have not yet been achieved on accelerators.

This abstract is devoted to one of many hypothetical extensions of the Standard Model, the "Small Higgs" theory, in which the Higgs boson is not a fundamental, but a constituent particle, which leads to the elimination of some theoretical problems of the Standard Model.

This abstract is devoted to some hypothetical extensions of the Standard Model, which leads to solutions of some theoretical problems of the Standard Model, and also provides opportunities for solving one of the most important problems of cosmology - the problem of dark matter searching.

1. Problems of the Standard Model

The Standard Model is a theory of strong and electroweak interactions based on the $SU(3) \times SU(2) \times U(1)$ gauge group. The described interactions are gauge so they are carried out by exchange of gauge bosons: photons in the case of electromagnetic interactions, gluons in strong interactions and W and Z in the case of weak interactions.

In contrast to massless photons and gluons, W and Z are massive particles (with a mass of the order of 100 GeV). The presence of a mass of these particles is a consequence of the symmetry breaking with respect to the $SU(2) \times U(1)$ group. It can be a consequence of the existence of some scalar field. The vacuum value of this field leads to the presence of a certain direction in the space of generators of the group $SU(2) \times U(1)$. Then the fact of the presence of the mass of elementary particles (leptons, gauge bosons, etc.) is a consequence of the particles interactions with the given scalar field. The quantum of this field is Higgs boson.

However, the Higgs boson explains only the fact of electroweak symmetry breaking, but not its mechanism. This theory does not explain why the potential of the Higgs field is unstable at zero. Therefore, the electroweak sector is apparently an interesting area for the search for "New Physics" that goes beyond the SM.

2. "Little Higgs" model

2.1 Main idea

An analysis of the experimental data makes possible to make an unambiguous conclusion about the fact of electroweak symmetry breaking but the mechanism of this breaking is still not understood.

If one assumes that there are no new particles with masses smaller than the scale of the electroweak sector then the "new physics" in the electroweak sector is realised by multidimensional operators suppressed by the energy scales of the "new physics" ($\Lambda \sim \text{TeV}$). These operators can be classified according to the symmetries that they violate. For example, it can be violation of CP - symmetry and symmetry of flavours. Thus, these operators impose strict restrictions on the preservation of

symmetries on the investigated scale ~ 1 TeV and SM extensions should not violate this boundary.

For understanding of the Higgs-boson mass stabilising possibility without violating these limitations, it is necessary to consider the reasons of the instability of the Higgs mass.

Let's now consider the main radiative corrections to the mass of the Higgs boson: one-loop diagrams with t-quarks (Fig. 1a), SU(2) gauge bosons (Fig. 1b) and Higgs boson (Fig. 1c) loops.

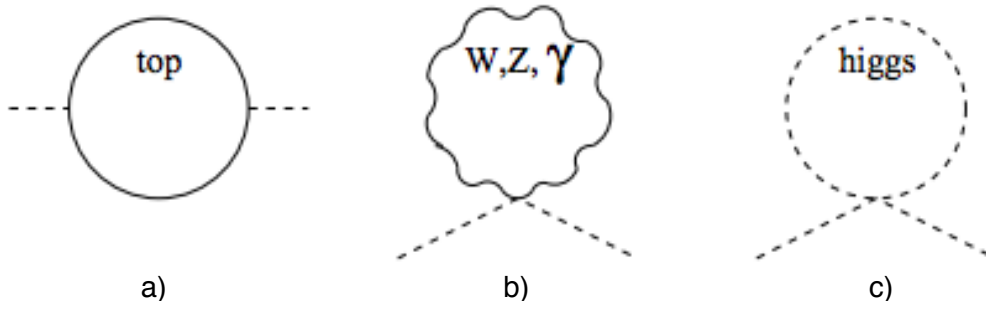


Fig. 1. Basic radiative corrections to the mass of the Higgs boson: a) single-loop diagrams with t-quarks b) single-loop diagrams with virtual Z and W bosons c) single-loop diagrams with Higgs bosons.

The contribution of the one-loop diagram is proportional to the square of the coupling constant [3], and this in turn is proportional to the mass of the virtual particle being formed. Since the mass of the t-quark significantly exceeds the masses of the other quarks (170 GeV is significantly higher than the next b-quark mass of the order of 4 GeV), all other contributions can be neglected. The remaining possible diagrams will give significantly lower contributions due to the smallness of their coupling constants in comparison with those considered.

If we assume that the SM remains true at energy scales of $\Lambda \sim 10$ TeV then the considered diagrams give a definite contribution to the mass of the Higgs boson (Table 1).

Diagram	Operator	contribution to $(m_H)^2$
t-quark loop	$-\frac{3}{8\pi^2}\lambda_t^2\Lambda^2$	$\sim(2 \text{ T}\mathfrak{B})^2$
SU(2) - bosons loop	$\frac{9}{64\pi^2}g^2\Lambda^2$	$\sim(700 \text{ T}\mathfrak{B})^2$
Higgs-bosons loop	$\frac{1}{16\pi^2}\lambda_t^2\Lambda^2$	$\sim(500 \text{ T}\mathfrak{B})^2$

Table. 1. The contribution of the diagrams to the squared mass of the Higgs boson.

For the Higgs boson's mass remaining at the electroweak scale, the energy scale of cutting should be:

- 1) for a loop diagram with a top quark: $\Lambda \leq 2 \text{ TeV}$;
- 2) for the loop diagram with gauge bosons: $\Lambda \leq 5 \text{ TeV}$;
- 3) for the loop diagram with the Higgs-loop: $\Lambda \leq 10 \text{ TeV}$.

Consequently, at the scale of energies of the order of 2 TeV one can expect the manifestation of a "new physics" associated with truncation of the divergent t-quark loop. It means that there have to exist new particles generating new loop diagrams that reduce the contribution from loops with the t-quark with the mass is equal to $\sim 2 \text{ TeV}$ and related by some symmetry to the t-quark.

Similarly at a scale of energies of the order of 5 TeV there must be new particles which are connecting with a similar type of symmetry with gauge bosons of the Standard Model, and at energies of the order of 10 TeV there must be new particles that cut the divergent loop with the Higgs boson.

One of the SM extensions solving this problem is the Little Higgs model, where the Higgs boson is a pseudo-Nambu-Goldstone boson. In this case global symmetries lead to a shift of the Higgs fields and as a result the Higgs mass does not contain single-loop divergences.

2.2 Nambu-Goldstone bosons

Nambu-Goldstone bosons are particles that arise due to spontaneous global symmetry breaking [4]. The simplest example is the case of an the U(1) group.

Suppose that we have a scalar field ϕ with a potential $V(\phi^*\phi)$. The $U(1)$ group involves the invariance of the potential with respect to the transformations:

$$\phi \rightarrow \phi \cdot e^{i\alpha}. \quad (1)$$

Because of the minimum of the potential is not equal to zero but at some point $f > 0$ (Figure 2), $U(1)$ symmetry spontaneously breaks.

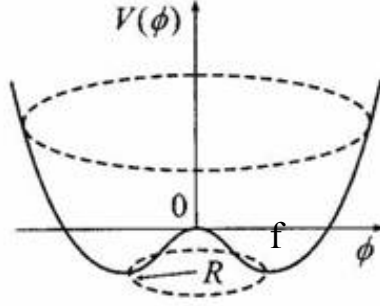


Fig. 2. Potential of spontaneous symmetry breaking of the $U(1)$ group.

Let's assume that the deviations of the field from the minimum are small. In this case, the field near the vacuum value can be expanded in a series:

$$\phi(x) = \frac{1}{\sqrt{2}}(f + r(x)) \cdot \exp\left[\frac{i\theta(x)}{f}\right], \quad (2)$$

where $r(x)$ is a massive radial mode, and $\theta(x)$ is a Nambu-Goldstone boson (NGB).

Because of the radial field $r(x)$ must be invariant with respect to $U(1)$ transformations, it can be shown that θ undergoes a shift to satisfy this condition: (3)

$$\theta \rightarrow \theta + \alpha, \quad \alpha \ll \theta.$$

It is important to note that the resulting effective Lagrangian must not contain the mass term of the field $\theta(x)$. The general form of the NGB Lagrangian is:

$$L = \text{const} + f^2 \left| \partial_\mu \phi \right|^2 + O(\partial^4). \quad (4)$$

2.3. Nambu-Goldstone bosons in non-abelian case

In the case of a spontaneous breaking of a non-abelian symmetry group each violated generator leads to the formation of one Nambu-Goldstone boson.

For example one can consider the case of violation of $SU(N) \rightarrow SU(N-1)$ due to the expectation value of the vacuum field ϕ . The number of generators of the group decreases from $(N)^2-1$ to $(N-1)^2-1$ so the number of violated generators is:

$$(N)^2-1-((N-1)^2-1) = 2N-1.$$

It is convenient to use the following form:

(5)

$$\phi = \exp \left[\frac{i}{f} \left(\begin{array}{ccc|c} \ddots & & \ddots & \pi_1 \\ & 0 & & \vdots \\ \ddots & & \ddots & \pi_{N-1} \\ \hline \pi_1^+ & \dots & \pi_{N-1}^+ & \pi_0 / \sqrt{2} \end{array} \right) \right] \left(\begin{array}{c} 0 \\ \vdots \\ f \end{array} \right) = e^{\frac{i\pi}{f}} \phi_0, \quad (6)$$

The π_0 field is real and the remaining ones are complex.

2.4. Little Higgs formation

Let's consider the $SU(3) \rightarrow SU(2)$ symmetry breaking. h is the doublet with respect to the undisturbed symmetry of the $SU(2)$ group, as required by the Standard Model mechanism. However, since he undergoes a shift relative to the breaking of the $SU(3)$ symmetry, h is a Nambu-Goldunian boson.

In this case:

$$\pi = \left(\begin{array}{c|c} -\eta/2 & |h \\ \hline h^+ & |\eta \end{array} \right) \quad (7)$$

moreover, the field η is a singlet with respect to $SU(2)$.

Then:

$$\phi = \exp \left[\frac{i}{f} \left(\begin{array}{cc} 0 & h \\ h^+ & 0 \end{array} \right) \right] \left(\begin{array}{c} 0 \\ f \end{array} \right) = \left(\begin{array}{c} 0 \\ f \end{array} \right) + i \left(\begin{array}{c} 0 \\ h \end{array} \right) - \frac{1}{2f} \left(\begin{array}{cc} 0 & \\ h^+ & h \end{array} \right) \quad (8)$$

and:

$$f^2 |\partial_\mu \phi|^2 = |\partial_\mu h|^2 + \frac{|\partial_\mu h|^2 h^+ h}{f^2}, \quad (9)$$

which describes the interaction suppressed by the symmetry breaking scale f . To determine the scale of the cutoff Λ , the contribution of the divergent one-loop diagram is taken into account in the second summand of the kinetic term. In case of cutting the divergence on the scale Λ , we find that the kinetic term is proportional to $\frac{1}{f^2} \frac{\Lambda^2}{16\pi^2}$. Based on the requirements on the coupling constant ≥ 1 , we obtain the condition $\Lambda < 4\pi f$.

The next step is the construction of gauge interactions. It is important, however, to remember that the mechanism of gauge interactions should not contain quadratic divergences. For this, two Nambu-Goldstone bosons ϕ_1 and ϕ_2 are considered. Parametrize them:

$$\phi_1 = \exp\left(\frac{i\pi_1}{f}\right) \begin{pmatrix} \\ f \end{pmatrix}, \phi_2 = \exp\left(\frac{i\pi_2}{f}\right) \begin{pmatrix} \\ f \end{pmatrix}, \quad (10)$$

taking into account that the vacuum mean fields are the same: $f_1 = f_2 = f$.

Then the Lagrangian of such a system can be written as follows:

$$L = |D_\mu \phi_1|^2 + |D_\mu \phi_2|^2. \quad (11)$$

It includes the following diagrams:

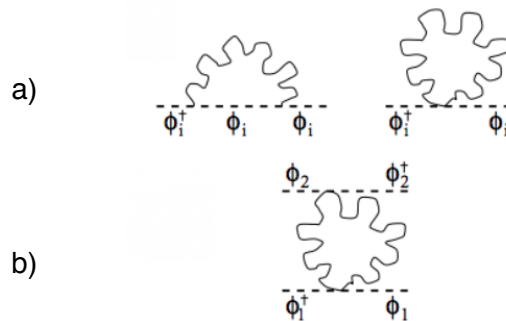


Fig. 3. Corrections to the interaction potential of one (a) and two (b) fields.

Contribution from diagrams containing only one field ϕ_1 or ϕ_2 (Figure 3a):

$$\frac{g^2}{16\pi^2} \Lambda^2 (\phi_1^+ \phi_1 + \phi_2^+ \phi_2) = \frac{g^2}{16\pi^2} \Lambda^2 (f^2 + f^2). \quad (12)$$

And from a diagram containing simultaneously the fields ϕ_1 or ϕ_2 (Fig. 3b):

$$\frac{g^2}{16\pi^2} \log\left(\frac{\Lambda^2}{\mu^2}\right) |\phi_1^+ \phi_2|^2. \quad (13)$$

Forasmuch:

$$|\phi_1^+ \phi_2| = f^2 - 2h^+ h + \dots, \quad (14)$$

Equation (13) can be rewritten in the form:

$$\frac{g^2}{16\pi^2} \log\left(\frac{\Lambda^2}{\mu^2}\right) f^2. \quad (15)$$

If the constant g is the coupling constant of SU(2) group, then $f \sim 1$ TeV, and the contribution to the squared mass of the Higgs boson is $\sim v^2$, which agrees with the Standard Model. In this case one-loop quadratic divergences in the mass of the Higgs boson are absent.

3. Experimental evidence of the “little Higgs”

All of the “little Higgs” models regardless of their implementation [5] include a vector-like quark that shortens the divergence of the single-loop t-quark diagrams, as well as a set of gauge bosons cuts bosonic loops.

The creation of these bosons occurs as a result of hadronic collisions, that is, one can expect the presence of these particles at the LHC experiment.

4. “Little Higgs” cosmological manifestation

Since the “little Higgs” model is a theory that considers the violation of electroweak symmetry, the natural step is to search for the cosmological manifestation of this model in the cosmology of the early Universe [6]. Specifically, of particular interest is the era of electroweak interactions, that is, the period between 10^{-32} and 10^{-12} seconds after the Big Bang, when the temperature of the Universe is

high enough, and due to high energies such particles as W-boson, Z-boson and boson Higgs are formed [7].

It was shown above that the "дшееду Higgs" model includes new particles on an energy scale of the order of 1 TeV. Since these particles are stable and weakly interacting, they can be candidates for the role of particles of dark matter, thus representing a solution to one of the main problems of modern cosmology [8].

Согласно современным астрофизическим представлением, на долю обычной барионной материи (межгалактический газ, звезды и т.д.) приходится менее 5%, на темную энергию ~ 68.5%, на нейтрино около 0.5%, а на темную материю, оставшиеся 26.5% [9]. Таким образом, почти 95% массы Вселенной состоит из неизвестной нам на данный момент массы, изучение которой имеет фундаментальное значение для космологии [10].

According to the modern astrophysical representation, ordinary baryonic matter (intergalactic gas, stars, etc.) accounts for less than 5%, including ~ 68.5% of dark energy, ~ 0.5% of neutrinos, and the remaining 26.5% of dark matter [9]. Thus, almost 95% of the mass of the universe consists of a mass unknown to us at the moment, the study of which is of fundamental importance for cosmology [10].

4.1. "Dark matter" problem

Let's consider the main evidence of the presence of dark matter [11]:

- 1) presence of rotation curves;
- 2) gravitational lensing;

4.1.1. Rotation curves

Galactic rotation curves are one of the most obvious proofs. According to Kepler's law, for the spiral galaxy the following relationship must be hold:

$$v^2(r) = \frac{G \cdot M(r)}{r},$$

where G is the gravitational constant and $M(r)$ is the mass concentrated inside the cluster of radius r . It can be expressed as:

$$M(r) = \int \rho(r) r^2 dr,$$

where $\rho(r)$ is the density distribution of matter inside the cluster.

In the outer region of the galaxy, the mass $M(r)$ is practically constant and the velocity dependence on the distance corresponds to the case with a point mass in the center of the galaxy:

$$v(r) \sim \frac{1}{\sqrt{r}}.$$

The rotation speed $v(r)$ is determined, for example, by measuring the Doppler shift in the emission spectrum of the He-II regions around the O-stars. However, the experimental data indicate that, with the distance from the center of the galaxy, the rotational velocity remains practically unchanged: $v(r) \approx \text{const.}$

The constancy of $v(r)$ for large values of the radius means that the mass M_r also increases with increasing radius: $M_r \sim r$. This indicates the presence of invisible matter. The stars move faster than one would expect on the basis of the apparent amount of matter. As an example of such a measurement, we can give results for the spiral galaxy M33 (Fig. 4) [12].

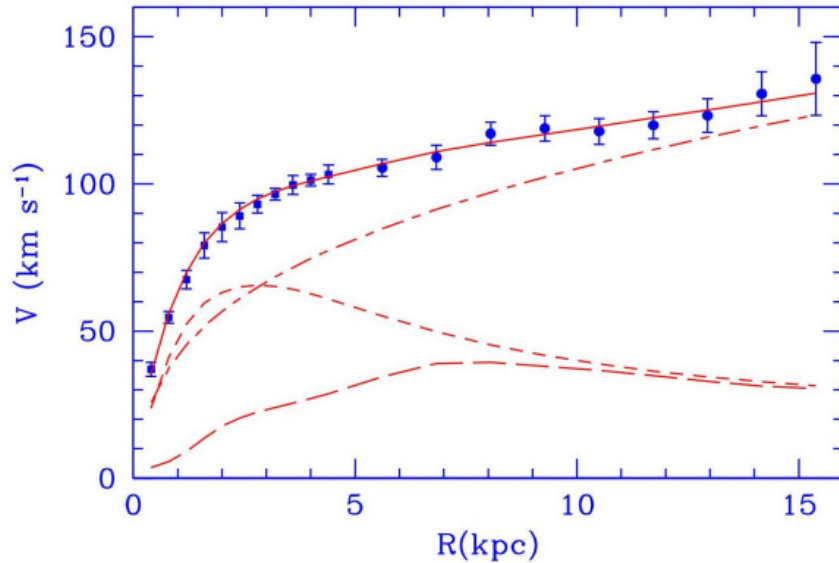


Fig. 4. Experimental rotational curve for the M33 spiral galaxy. The dot-dashed line takes into account the contribution of the halo to the theoretical model, and the short and long dotted line represents the stellar disk and the gas contribution, respectively.

4.1.2. Gravitational lensing

Явление гравитационного линзирования заключается в отклонении электромагнитного излучения вблизи массивных тел. Как правило для заметного искажения изображения нужны массы порядка размера галактик или их скоплений. Такими гравитационными линзами могут являться скопления скрытой массы, что подтверждается данными, полученными с использованием эксперимента Hubble. Гравитационное линзирование позволяет, в частности, численно рассчитать предполагаемый количественный вклад тёмной материи.

4.1.3 Non-baryonic nature of dark matter

Of particular interest is the consideration of the nature of the matter of dark matter. The evolution of the universe is described by the Friedman equations [13]:

$$\begin{cases} \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3}\epsilon - \frac{K}{a^2} \\ \frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\epsilon + 3p) \end{cases}$$

where G is the gravitational constant, ϵ is the energy density, p is the matter pressure. K is the curvature parameter. The case $K = 0$ corresponds to a flat world, $K = 1$ to a open world, and $K = -1$ to a closed world. The Hubble parameter in the case of a flat world:

$$H = \frac{\dot{a}}{a}$$

is expressed by the first Friedmann equation:

$$(H)^2 = \frac{8\pi G}{3}\epsilon_{crit},$$

where the corresponding energy density is called critical:

$$\epsilon_{crit} = \frac{3H^2}{8\pi G}.$$

The density of the component of matter is measured in units of critical density:

$$\Omega = \frac{\epsilon}{\epsilon_{crit}},$$

Where ε is the density of this component.

To measure the energy density, one can obtain from Friedmann's equations that:

$$\begin{cases} \dot{\varepsilon} = -3H(\varepsilon + p) \\ \Omega = 1 + \frac{K}{a^2} \end{cases}$$

The total energy density, estimated from the experimental data [14]:

$$\Omega \approx 1 \pm 0.1.$$

On the other hand, an estimate of the baritonic density of matter, performed on the luminosity of galaxies:

$$\Omega_{bar} < 0.04.$$

This discrepancy, firstly, is another confirmation of the fact of the presence of dark matter, and secondly - it makes possible to make a conclusion about the non-baryonic nature of the matter of dark matter.

4.2. “Dark matter” problem’s solution with “little Higgs” theory

4.2.1. Estimation of the density of dark matter

According to modern cosmological concepts, the density of matter of dark matter is in the range [15]:

$$0.094 < \Omega_{DM} h^2 < 0.126,$$

where h is Planck's constant and Ω_{DM} is the matter density of dark matter, measured in units of critical density.

On the other hand, it is possible to estimate the matter density of dark matter from the theoretical point of view [16]. In the early universe, dark matter particles were in thermal equilibrium with the rest of the cosmic plasma. In the process of cooling the universe, density decreases due to annihilation, which leads to the fact that for each particle annihilation becomes less likely due to a decrease in the concentration of the partner particles, therefore, over time the density will tend to a constant value, which corresponds to the stage of "freezing" . Thus, the density of dark matter particles is completely determined at the time of freezing, which can be

expressed by the condition of thermodynamic averaging of the cross section during the freezing time [17]:

$$\Omega_\chi h^2 \approx \frac{1.07 \cdot 10^{-9} \text{ GeV}^{-1}}{M_{Pl}} \cdot \frac{x_F}{\sqrt{g_*}} \cdot \frac{1}{\langle \sigma v \rangle},$$

where M_{Pl} is the Planck mass, σv is the annihilation cross section of particles and antiparticles, and g_* is the number of relativistic degrees of freedom. The x_F value parametrizes the freezing temperature and can be estimated from the solution of the equation:

$$x_F = \ln \left[c(c+2) \sqrt{\frac{45}{8}} \frac{g}{2\pi^3} \frac{m M_{Pl} \langle \sigma v \rangle}{\sqrt{g_*} \sqrt{x_F}} \right],$$

where c is a constant determined from the comparison of solutions for the early and late Universe.

As a result of solving this equation in the allowed range of matter density of dark matter:

$$0.094 < \Omega_{DM} h^2 < 0.126,$$

the following relation is obtained between the cut-off parameter f and the mass of dark matter:

$$f = 3.2 M_\chi + 600,$$

where the mass and f are given in GeV.

4.2.1. Dark matter cross section of annihilation

On the other hand, we can consider the cross section for annihilation of particles and antiparticles [18]. The quenching condition [19], in which the amount of particles of the hidden mass becomes constant:

$$H = n \langle \sigma v \rangle,$$

where H is the Hubble parameter, σv is the annihilation cross section of particles and antiparticles, and n is the concentration of these particles. In order for the number of particles to correspond to the observed values, the annihilation cross section should be:

$$\langle\sigma v\rangle=3\cdot10^{-26} sm^3/sec,$$

which in order of magnitude corresponds to weak interactions scale.

Since the little Higgs theory considers the electroweak sector of the Standard Model, the cross section for the annihilation of the produced particles is determined by the weak interaction, which ultimately leads to the conclusion that this theory does not contradict cosmological constraints and can be one of the possible candidates for dark matter particles.

5. Conclusion

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