

## Do no observations so far of the fourth family quarks speak against the spin-charge-family theory?

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We all are are trying to understand:

- Is **Nature** simple and elegant in law with one constant only, while complications arrive due to many degrees of freedom of fermions and bosons, with symmetries showing up also in these cases?
- Or **Nature** is neither simple nor elegant in laws, and yet she manifests many times - under special conditions - in extremely elegant ways showing up symmetries?  
But where then all the constants come from—

- **Spin-Charge-Family** theory offers explanation for all the assumptions of the Standard model, for Dark matter, Matter-antimatter asymmetry, ... , making predictions.
- The **Spin-Charge-Family** theory predicts among other things several scalar fields, all with properties of the higgs with respect to the weak and the hyper charge, explaining the appearance of the masses of fermions, their mixing matrices and their couplings to higgs scalar, called Yukawa couplings.  
**It predicts the existence of the fourth family to the observed three.**

- There are **no observations** so far of the **fourth family**, predicted by the spin-charge-family theory. Does this mean that the **spin-charge-family** theory is not the right theory, showing the next step beyond the standard model?

More than **40 years ago**, when **our interpretation of the elementary law of nature looked quite complicated**, the **standard model** offered an **elegant new step in understanding the origin of fermions and bosons by postulating**:

- The existence of the **massless family members: coloured quarks and colourless leptons, both left and right handed**, the **left handed members** distinguishing from the **right handed ones** in the **weak and hyper charges** and correspondingly **mass protected**.

$\alpha$ name	hand- edness $-4iS^0 S^{12}$	weak charge $\tau^{13}$	hyper charge $Y$	colour charge	elm charge $Q$
$u_L^i$	-1	$\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$\frac{2}{3}$
$d_L^i$	-1	$-\frac{1}{2}$	$\frac{1}{6}$	colour triplet	$-\frac{1}{3}$
$\nu_L^i$	-1	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
$e_L^i$	-1	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1
$u_R^i$	1	weakless	$\frac{2}{3}$	colour triplet	$\frac{2}{3}$
$d_R^i$	1	weakless	$-\frac{1}{3}$	colour triplet	$-\frac{1}{3}$
$\nu_R^i$	1	weakless	0	colourless	0
$e_R^i$	1	weakless	-1	colourless	-1

Members of each of the  $i = 1, 2, 3$  massless families before the electroweak break. Each family contains the left handed weak charged quarks and the right handed weak chargeless quarks, belonging to the colour triplet

$(1/2, 1/(2\sqrt{3})), (-1/2, 1/(2\sqrt{3})), (0, -1/(\sqrt{3}))$ .

- The existence of **massless families to each of a family member.**

- The existence of the **massless gauge fields** to the observed **charges** of the family **members**.

## Gauge fields before the electroweak break

- Three massless vector fields, the gauge fields of the three charges.

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
hyper photon	0	0	0	colourless	0
weak bosons	0	triplet	0	colourless	triplet
gluons	0	0	0	colour octet	0

They all are vectors in  $d = (3 + 1)$ , in the adjoint representations with respect to the weak, colour and hyper charges.

- The existence of a massive **scalar field** carrying the weak charge  $\pm\frac{1}{2}$  and the hyper charge  $\mp\frac{1}{2}$  with "nonzero vacuum expectation values", breaking the weak and the hyper charge and correspondingly breaking the **mass protection**.
- **The existence** of the **Yukawa couplings** of fermions to the higgs

$$Y^\alpha \frac{v}{\sqrt{2}},$$

which, together (with the **gluons** and) the **scalar Higgs** - after it breaks the weak and the hyper charge - take care of the masses of **fermions** and of the **weak bosons**.



- The Higgs field, the scalar in  $d = (3 + 1)$ , a doublet with respect to the weak charge.  $P_R = (-1)^{2s+3B+L} = 1$ .

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
0 · $Higgs_u$	0	$\frac{1}{2}$	$\frac{1}{2}$	colourless	1
$\langle Higgs_d \rangle$	0	$-\frac{1}{2}$	$\frac{1}{2}$	colourless	0

- 

name	hand- edness	weak charge	hyper charge	colour charge	elm charge
$\langle Higgs_u \rangle$	0	$\frac{1}{2}$	$-\frac{1}{2}$	colourless	0
0 · $Higgs_d$	0	$-\frac{1}{2}$	$-\frac{1}{2}$	colourless	-1

-

**The *standard model* assumptions have been confirmed without offering surprises.**

**The last unobserved field, the **Higgs scalar**, detected in June 2012, was confirmed in March 2013.**

The idea that all the **fermion** and **vector fields** are **massless**, if they are free, was an **elegant** assumption, which is **not the case** with the massive **higgs** and also not with **so many unexplained assumptions**.

**What questions** should one ask to see the next step beyond the standard model, which would extend the **elegance** of the **standard model** and offer the explanation for its **assumptions?**

I suggest the **most urgent** questions:

- **Where do families originate? Why there exist families at all? How many families are there?**

- **Why there are left and right handed family members, distinguishing so much in charges?**

Why family members – quarks and leptons – manifest so different properties if they all start as massless?

- **How is the origin of the scalar field (the Higgs) and the Yukawa couplings connected with the origin of families?**

- **How many scalar fields determine properties of the so far (and others possibly be) observed fermions and masses of weak bosons?**

- Why is **the Higgs's scalar**, or are all the scalar fields, if there are several, **doublets** with respect to the weak and the hyper charge?
- Where do the scalar fields **masses** originate?
- Are there **scalar fields with the colour charge** in the fundamental representation and where, if they are, **do they manifest?**
- Where does the **dark matter** originate?
- Where does the **dark energy** originate and why is it so **small?**
- Where does the "ordinary" **matter-antimatter asymmetry** originate?
- Where do the **charges** and correspondingly the so far (and others possibly be) **observed gauge** originate?



- What is the dimension of space?  $(3 + 1)?$ ,  $((d - 1) + 1)?$ , infinite?
- **What** is the role of the **symmetries**– discrete, continuous, global and gauge –in Nature?
- **Why** there exist **fermions** and **bosons**?
- **And many others.**

## My statement:

- **An elegant trustworthy step beyond the standard model must offer answers to several open questions, explaining:**
  - The **origin of the charges.**
  - The **origin and properties of the families.**
  - The **origin and properties of the scalar fields.**
  - The **origin and properties of the vector gauge fields.**
  - The **origin of the dark matter.**
  - The **origin of the "ordinary" matter-antimatter asymmetry.**

- There exist not yet **observed families, gauge fields, scalar fields.**
- **Dimension of space is larger than 4** (very probably infinite).
- Inventing a next step which covers only one of the open questions, **can hardly be the right step.**

In the literature **NO explanation for the existence of the families can be found**, which would not just assume the family groups. Several extensions of the **standard model** are, however, proposed, like:

- **A tiny extension**: The inclusion of the right handed neutrinos into the family.
- The  $SU(3)$  group is assumed to describe – not explain – the existence of three families.

Like the **Higgs's** scalar charges are in the **fundamental** representations of the groups, also the **Yukawas** are assumed to emerge from the scalar fields, in the **fundamental** representation of the  $SU(3)$  group.

- **SU(5) and SU(10) grand unified theories are proposed, unifying all the charges.** But the **spin** (the handedness) is obviously **connected with** the (weak and the hyper) **charges** and the **appearance of families is not explained.**
- **Supersymmetric theories, assuming the existence of bosons with the charges of quarks and leptons and fermions with the charges of the gauge vector fields, although having several nice properties but not explaining the occurrence of families (except again by assuming larger groups), are not, to my understanding, the right next step beyond the *standard model*.**

The **Spin-Charge-Family** theory does offer **the explanation for all the assumptions of the standard model** and answers several above cited open questions!

**Starting with a simple action for fermions and gravity only it is an elegant next step beyond the standard model .**



- A brief introduction into the **spin-charge-family theory**.

- **Spinors** carry in  $d \geq (13 + 1)$  two kinds of **spin**, no charges.
  - The **Dirac spin** ( $\gamma^a$ ) in  $d = (13 + 1)$  describes in  $d = (3 + 1)$  the **spin and ALL the charges of quarks and leptons, left and right handed**.
  - The **second kind of the spin** ( $\tilde{\gamma}^a$ ) describes **FAMILIES**.
  - There is **NO third kind of spin**.
- **C,P,T symmetries** in  $d = (3 + 1)$  follow from the **C,P,T symmetry** in  $d \geq (13 + 1)$ . (*JHEP* **04** (2014) 165)

- **Spinors** interact correspondingly with the **vielbeins** and the two kinds of the **spin connection fields**.
- In  $d = (3 + 1)$  the **spin-connection fields**, together with the **vielbeins**, manifest either as
  - the **vector** gauge fields with all the **charges** in the **adjoint representations** (contribution to the Bled proceedings 2015) or as
  - the **scalar** gauge fields with the **charges** with respect to the **space index** in the **fundamental** representations and all the other **charges** in the **adjoint** representations or as
  - the **tensor** gravitational field.
- If there are **no spinor sources present**, then either vector  $(\vec{A}_m^A, m = 0, 1, 2, 3)$  or scalar  $(\vec{A}_s^A, s = 5, 6, \dots, d)$  gauge fields are determined by **vielbeins**.



There are two kinds of **scalar fields** with respect to the space index  $s$ :

- Those with zero "spinor charge" and  $s = 5, 6, 7, 8$  are **doublets** with respect to the **weak charge** and the **second  $SU(2)_H$  charge**. They are in the **adjoint** representations with respect to the family and the family members **charges**.
- These **scalars** explain the **Higgs scalar** and Yukawa couplings.

- **Those** with twice the "spinor charge" of a quark and  $s = 9, 10, ..d$  are **colour triplets**. **Also they are in the adjoint representations** with respect to the family and the family members **charges**.
  - These **scalars** transform antileptons into quarks, and antiquarks into quarks and back and correspondingly **contribute to matter-antimatter asymmetry** of our universe and to **proton decay**.
- **There are no additional scalar fields in the spin-charge-family theory.**



- The (assumed) scalar **condensate** of two right handed neutrinos with the **family** quantum numbers of the upper four families (there are two four family groups in the theory), appearing  $\approx 10^{16}$  GeV,
  - **breaks the CP** symmetry, causing the **matter-antimatter asymmetry** and the proton decay,
  - couples to all the **scalar fields**, making them massive,
  - couples to all the phenomenologically **unobserved vector gauge fields**, making them massive.



- The **vector fields**, which do not couple to the condensate and remain massless, are:
  - the **hyper charge vector field**.
  - the **weak vector fields**,
  - the **colour vector fields**,
  - the **gravity fields**.

The  $SU(2)_H$  symmetry breaks due to the condensate.

- When the scalar fields with the **space index** (7, 8) gain **nonzero vacuum expectation values**,
  - they cause the **electroweak break**,
  - breaking the weak and the hyper charge.
  - They change their own masses,
  - bring masses to the **weak bosons**,
  - bring masses to the **families of quarks and leptons**.
- The only gauge fields which do not couple to these scalars and remain massless are the **electromagnetic** and **colour** vector gauge fields, and the **gravity**.
- There are two times four decoupled massive **families** of **quarks and leptons** after the electroweak break .



- **It is extremely encouraging** for the spin-charge-family theory, that a simple starting action manifests in the low energy regime all the directly or indirectly **observed phenomena** and that only the

○ **condensate** and

○ **nonzero vacuum expectation values of all the scalar fields with  $s = (7, 8)$**

**explain all the assumptions of the standard model, explaining also the dark matter, the matter/antimatter asymmetry and...**

## A brief overview of the **spin-charge-family** theory.

## There are two kinds of the Clifford algebra objects (only two):

- The **Dirac**  $\gamma^a$  operators (used by Dirac 90 years ago).
- The **second one**:  $\tilde{\gamma}^a$ , which I recognized in the Grassmann space.

$$\{\gamma^a, \gamma^b\}_+ = 2\eta^{ab} = \{\tilde{\gamma}^a, \tilde{\gamma}^b\}_+,$$

$$\{\gamma^a, \tilde{\gamma}^b\}_+ = 0,$$

$$(\tilde{\gamma}^a \mathbf{B} : = \mathbf{i}(-)^{n_B} \mathbf{B} \gamma^a) |\psi_0 \rangle,$$

$$(\mathbf{B} = a_0 + a_a \gamma^a + a_{ab} \gamma^a \gamma^b + \dots + a_{a_1 \dots a_d} \gamma^{a_1} \dots \gamma^{a_d}) |\psi_0 \rangle$$

$(-)^{n_B} = +1, -1$ , when the object  $B$  has a Clifford even or odd character, respectively.

$|\psi_0 \rangle$  is a vacuum state on which the operators  $\gamma^a$  apply.

$$\mathbf{S}^{ab} := (\mathbf{i}/4)(\gamma^a \gamma^b - \gamma^b \gamma^a),$$

$$\tilde{\mathbf{S}}^{ab} := (\mathbf{i}/4)(\tilde{\gamma}^a \tilde{\gamma}^b - \tilde{\gamma}^b \tilde{\gamma}^a),$$

$$\{\mathbf{S}^{ab}, \tilde{\mathbf{S}}^{cd}\}_- = \mathbf{0}.$$

- $\tilde{\mathbf{S}}^{ab}$  define the equivalent representations with respect to  $\mathbf{S}^{ab}$ .

My recognition:

- If  $\gamma^a$  are used to describe **the spin and the charges of spinors**,  
 $\tilde{\gamma}^a$  can be used to describe families of spinors.

**Must be used!!**



- $S^{ab}$ , applied on the object  $B$ , extract **family members of spinors and determine their quantum numbers**,
- $\tilde{S}^{ab}$ , applied on the **spinors**, determine to **each family member the families** and their quantum numbers,
- $(S^{ab} + \tilde{S}^{ab})$ , applied on the object  $B$ , extract **vector, scalar and tensor** states and determine their quantum numbers.



A simple action for a **spinor** which carries in  $d = (13 + 1)$  only **two kinds of a spin** (no charges) and for **the gauge fields**

$$\mathbf{S} = \int d^d x E \mathcal{L}_f + \int d^d x E (\alpha R + \tilde{\alpha} \tilde{R})$$

$$\mathcal{L}_f = \frac{1}{2} (\bar{\psi} \gamma^a p_{0a} \psi) + h.c.$$

$$p_{0a} = f^\alpha{}_a p_{0\alpha} + \frac{1}{2E} \{p_\alpha, E f^\alpha{}_a\} -$$

$$\mathbf{p}_{0\alpha} = \mathbf{p}_\alpha - \frac{1}{2} \mathbf{S}^{ab} \omega_{ab\alpha} - \frac{1}{2} \tilde{\mathbf{S}}^{ab} \tilde{\omega}_{ab\alpha}$$

- The only internal degrees of freedom of **spinors fermions**) are the **two kinds of the spin**.
- The only **gauge fields** are the **gravitational ones** – **vielbeins and the two kinds of spin connections**.
- Either  $\gamma^a$  or  $\tilde{\gamma}^a$  transform as vectors in  $d$ ,

$$\gamma'^a = \Lambda^a_b \gamma^b, \quad \tilde{\gamma}'^a = \Lambda^a_b \tilde{\gamma}^b,$$

$$\delta\gamma^c = -\frac{i}{2} \alpha_{ab} S^{ab} \gamma^c = \alpha^c_a \gamma^a,$$

$$\delta\tilde{\gamma}^c = -\frac{i}{2} \alpha_{ab} \tilde{S}^{ab} \tilde{\gamma}^c = \alpha^c_a \tilde{\gamma}^a,$$

$$\delta A^{c\dots ef} = -\frac{i}{2} \alpha_{ab} S^{ab} A^{c\dots ef} = \alpha^e_a A^{c\dots af},$$

$$S^{ab} A^{c\dots e\dots f} = i(\eta^{ae} A^{c\dots b\dots f} - \eta^{be} A^{c\dots a\dots f})$$

and correspondingly also  $f^\alpha_a \omega_{bc\alpha}$  and  $f^\alpha_a \tilde{\omega}_{bc\alpha}$  transform as tensors with respect to the flat index  $a$ .



- The action for spinors seen from  $d=(3+1)$  and analyzed with respect to the standard model groups as subgroups of  $SO(1 + 13)$ , J.of Mod.Phys.**4(2013)823**:

$$\begin{aligned}
 \mathcal{L}_f = & \bar{\psi} \gamma^m (p_m - \sum_{A,i} g^A \tau^{Ai} A_m^{Ai}) \psi + \\
 & \left\{ \sum_{s=[7],[8]} \bar{\psi} \gamma^s p_{0s} \psi \right\} + \\
 & \left\{ \sum_{s=[5],[6]} \bar{\psi} \gamma^s p_{0s} \psi + \right. \\
 & \left. \sum_{t=[9],\dots[14]} \bar{\psi} \gamma^t p_{0t} \psi \right\}.
 \end{aligned}$$

## The action

$$p_{0m} = \{p_m - \sum_A g^A \vec{\tau}^A \vec{A}_m^A\}$$

$$m \in (0, 1, 2, 3),$$

$$p_{0s} = f_s^\sigma [p_\sigma - \sum_A g^A \vec{\tau}^A \vec{A}_\sigma^A - \sum_A \tilde{g}^A \vec{\tau}^A \vec{A}_\sigma^A],$$

$$s \in (7, 8),$$

$$p_{0s} = f_s^\sigma [p_\sigma - \sum_A g^A \vec{\tau}^A \vec{A}_\sigma^A - \sum_A \tilde{g}^A \vec{\tau}^A \vec{A}_\sigma^A],$$

$$s \in (5, 6),$$

$$p_{0t} = f_t^{\sigma'} (p_{\sigma'} - \sum_A g^A \vec{\tau}^A \vec{A}_{\sigma'}^A - \sum_A \tilde{g}^A \vec{\tau}^A \vec{A}_{\sigma'}^A),$$

$$t \in (9, 10, 11, \dots, 14),$$



## The action

$$\mathbf{A}_s^{\text{Ai}} = \sum_{a,b} \mathbf{c}_{ab}^{\text{Ai}} \omega_{abs} ,$$

$$\mathbf{A}_t^{\text{Ai}} = \sum_{a,b} \mathbf{c}_{ab}^{\text{Ai}} \omega_{abt} ,$$

$$\tilde{\mathbf{A}}_s^{\text{Ai}} = \sum_{a,b} \tilde{\mathbf{c}}_{ab}^{\text{Ai}} \tilde{\omega}_{abs} ,$$

$$\tilde{\mathbf{A}}_t^{\text{Ai}} = \sum_{a,b} \tilde{\mathbf{c}}_{ab}^{\text{Ai}} \tilde{\omega}_{abt} .$$

$$\tau^{Ai} = \sum_{a,b} c^{Ai}_{ab} \mathbf{S}^{ab},$$

$$\tilde{\tau}^{Ai} = \sum_{a,b} \tilde{c}^{Ai}_{ab} \tilde{\mathbf{S}}^{ab},$$

$$\{\tau^{Ai}, \tau^{Bj}\}_- = i\delta^{AB} f^{Aijk} \tau^{Ak},$$

$$\{\tilde{\tau}^{Ai}, \tilde{\tau}^{Bj}\}_- = i\delta^{AB} f^{Aijk} \tilde{\tau}^{Ak},$$

$$\{\tau^{Ai}, \tilde{\tau}^{Bj}\}_- = 0.$$

- $\tau^{Ai}$  represents the standard model charge groups, for the second  $SU(2)_I$ , for the "spinor" charge,
- $\tilde{\tau}^{Ai}$  denote the family quantum numbers.

$$\vec{N}_{(L,R)} := \frac{1}{2}(S^{23} \pm iS^{01}, S^{31} \pm iS^{02}, S^{12} \pm iS^{03}),$$

$$\vec{\tau}^{(1,2)} := \frac{1}{2}(S^{58} \mp S^{67}, S^{57} \pm S^{68}, S^{56} \mp S^{78}),$$

$$\vec{\tau}^3 := \frac{1}{2}\{S^{9\ 12} - S^{10\ 11}, S^{9\ 11} + S^{10\ 12}, S^{9\ 10} - S^{11\ 12}, \\ S^{9\ 14} - S^{10\ 13}, S^{9\ 13} + S^{10\ 14}, S^{11\ 14} - S^{12\ 13}, \\ S^{11\ 13} + S^{12\ 14}, \frac{1}{\sqrt{3}}(S^{9\ 10} + S^{11\ 12} - 2S^{13\ 14})\},$$

$$\tau^4 := -\frac{1}{3}(S^{9\ 10} + S^{11\ 12} + S^{13\ 14}), \quad Y := \tau^4 + \tau^{23},$$

$$Y' := -\tau^4 \tan^2 \vartheta_2 + \tau^{23}, \quad Q := \tau^{13} + Y, \quad Q' := -Y \tan^2 \vartheta_1 + \tau^{13},$$

and equivalently for  $\check{S}^{ab}$  and  $S^{ab}$ .



Breaks of symmetries when starting with the **massless spinors** (**fermions**), **vielbeins and two kinds of spin connection fields**



## Breaking the starting symmetry from:

- $SO(1, 13) \times \widetilde{SO}(1, 13)$  to  
 $SO(1, 7) \times \widetilde{SO}(1, 7) \times U(1)_{II} \times SU(3)$  (at  $E \geq 10^{16}$  GeV)

**O** makes the **spin** (the handedness) in  $d = (1 + 3)$  of two massless groups of four families of spinors connected with the **weak** and the **hyper** charge ,

- $SO(1, 7) \times \widetilde{SO}(1, 7) \times U(1)_{II} \times SU(3)$  to  
 $SO(1, 3) \times SU(2)_I \times SU(2)_{II} \times U(1)_{II} \times SU(3)$   
 $\widetilde{SO}(1, 3) \times \widetilde{SU}(2)_I \times \widetilde{SU}(2)_{II}$

**O** makes that each member of the two groups of four massless families manifests in  $d = (1 + 3)$  the **weak** ( $SU(2)_I$ ), the **hyper** ( $SU(2)_{II}$ ), the **colour** ( $SU(3)$ ) and the **"spin charge"** ( $U(1) = \tau^4$ ).



- Both breaks leave **eight families** ( $2^{8/2-1} = 8$ , determined by the symmetry of  $SO(1, 7)$ ) massless.
- **The appearance of the condensate of the two right handed neutrinos, coupled to spin 0**, makes all the boson fields
  - that is the scalar fields with the space index  $s \geq 5$
  - and the vector bosons,  $m \leq 3$ , with the charge which is the superposition of  $(SU(2)_{II})$  and  $U(1)_{III}$ , massive,
  - while the **colour, elm, weak and hyper** vector gauge fields remain massless.

- In Ref. [arXiv:1604.00675] it is proven the one-to-one correspondence between the **vielbeins in the Kaluza-Klein** theories, which represent **gauge fields** in ( $d=(3+1)$ ) after the isometry procedure, and the **spin connection fields** used in the *spin-charge-family* theory to describe the **vector gauge fields** in  $d = (3 + 1)$ .
- The **vielbeins**  $f^\sigma_m$  relation to the **spin connections**:

$$f^\sigma_m = -i \sum_A \tilde{A}_m^A \tilde{\tau}^{A\sigma} x^\tau,$$

$\vec{A}_m^A$  are the superposition of  $\omega^{st}_m$ ,  $A_m^{Ai} = c^{Ai}_{st} \omega^{st}_m$ , what demonstrates the symmetry of the space with  $s \geq 5$ .



- **At the electroweak break** from  $SO(1,3) \times SU(2)_I \times U(1)_I \times SU(3)$  to  $SO(1,3) \times U(1) \times SU(3)$  the scalar fields with the space index  $s = (7, 8)$  obtain nonzero vacuum expectation values,
  - breaking correspondingly the weak and the hyper charge and changing their own masses.
  - They leave massless only the colour and the elm gauge fields, while all eight massless families gain masses.

- **To the electroweak break** several scalar fields contribute, all with the **weak and the hyper charge** of the *standard model* Higgs, carrying besides the weak and the hyper charge either **the family members** quantum numbers **( $Q, Q', Y'$ )** or the **family quantum numbers**.



- Both,  $SO(n)$  and  $\widetilde{SO}(n)$  break simultaneously.
- We studied (with H.B. Nielsen, D. Lukman) on a toy model of  $d = (1 + 5)$  conditions which lead after breaking symmetries to massless spinors chirally coupled to the Kaluza-Klein-like gauge fields, New J.Phys.**13**(2011)103027,1-25.

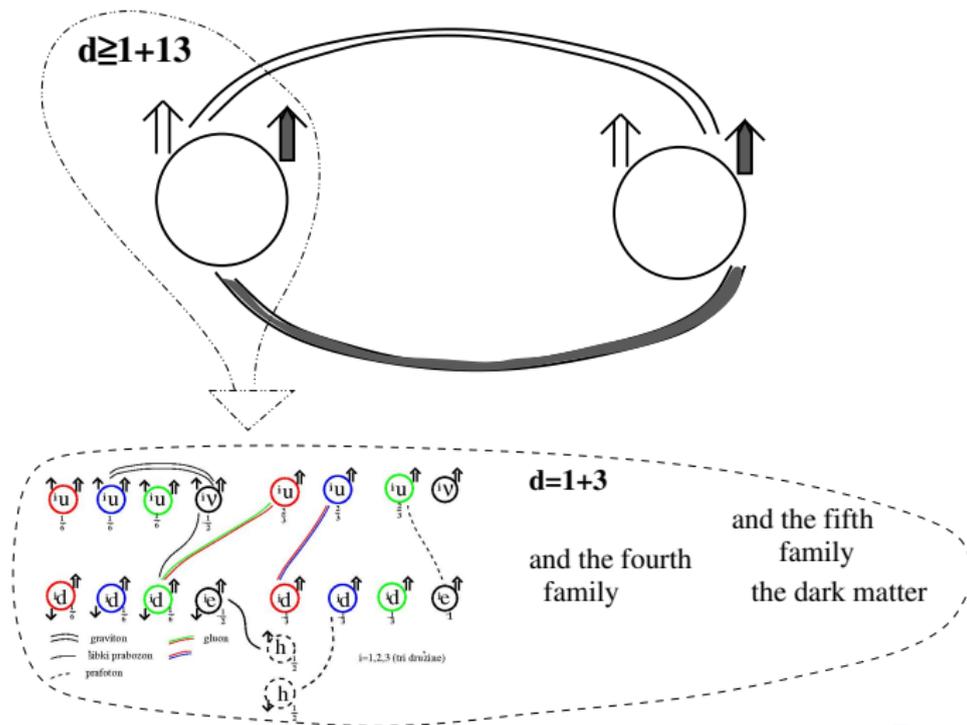


## ■ Is Nature elegant with simple laws

$$\mathbf{S} = \int d^d x E \mathcal{L}_f + \int d^d x E (\alpha R + \tilde{\alpha} \tilde{R}),$$

**Or it is complicated and only "from time to time" symmetries show up?**

The action





## Our technique to represent spinors is elegant.

- N. S. Mankoč Borštnik, *J. Math. Phys.* **34**, 3731 (1993),
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- *J. of High Ener. Phys.* **04** (2014) 165, arxiv:1212.2362v2, the last three with H.B. Nielsen.



$$\begin{aligned}
 \overset{\text{ab}}{(\pm \mathbf{i})} &:= \frac{1}{2}(\gamma^{\mathbf{a}} \mp \gamma^{\mathbf{b}}), \quad [\overset{\text{ab}}{\pm \mathbf{i}}] := \frac{1}{2}(1 \pm \gamma^{\mathbf{a}}\gamma^{\mathbf{b}}) \\
 &\text{for } \eta^{aa}\eta^{bb} = -1, \\
 \overset{\text{ab}}{(\pm)} &:= \frac{1}{2}(\gamma^{\mathbf{a}} \pm \mathbf{i}\gamma^{\mathbf{b}}), \quad [\overset{\text{ab}}{\pm}] := \frac{1}{2}(1 \pm i\gamma^{\mathbf{a}}\gamma^{\mathbf{b}}), \\
 &\text{for } \eta^{aa}\eta^{bb} = 1
 \end{aligned}$$

with  $\gamma^a$  which are the usual **Dirac operators**



## Our technique

$$\begin{aligned} \mathbf{S}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \mathbf{S}^{ab}[\mathbf{k}] &= \frac{k^{ab}}{2}[\mathbf{k}], \\ \tilde{\mathbf{S}}^{ab}(\mathbf{k}) &= \frac{k^{ab}}{2}(\mathbf{k}), & \tilde{\mathbf{S}}^{ab}[\mathbf{k}] &= -\frac{k^{ab}}{2}[\mathbf{k}]. \end{aligned}$$



$\gamma^a$  transforms  $\binom{ab}{k}$  into  $[-k]$ , never to  $\binom{ab}{k}$ .

$\tilde{\gamma}^a$  transforms  $\binom{ab}{k}$  into  $\binom{ab}{k}$ , never to  $[-k]$ .



- One Weyl representation of one family contains all the **family members** with the **right handed neutrinos included**. It includes also **antimembers**, reachable by  $\mathbb{C}_N \mathcal{P}_N$  on a **family member**.
- There are  $2^{(7+1)/2-1} = 8$  **families**, which decouple into twice four families, with the quantum numbers  $(\tilde{\tau}^{2i}, \tilde{N}_R^i)$  and  $(\tilde{\tau}^{1i}, \tilde{N}_L^i)$ , respectively.

$S^{ab}$  generate **all the members of one family**. The eightplet (the representation of  $SO(7, 1)$ ) of quarks of a particular colour charge

i		$ ^a \psi_i \rangle$	$\Gamma^{(3,1)}$	$S^{12}$	$\Gamma^{(4)}$	$\tau^{13}$	$\tau^{23}$	$Y$	$\tau^4$
		Octet, $\Gamma^{(7,1)} = 1$ , $\Gamma^{(6)} = -1$ , of quarks							
1	$u_R^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & (+)(+) &    & (+)(-) & (-) & (-) & \end{matrix}$	1	$\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
2	$u_R^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] &   & (+)(+) &    & (+)(-) & (-) & \end{matrix}$	1	$-\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{1}{6}$
3	$d_R^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & [-] & [-] &    & (+)(-) & (-) & \end{matrix}$	1	$\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
4	$d_R^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & [-] &   & [-] & [-] &    & (+)(-) & (-) \end{matrix}$	1	$-\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{1}{3}$	$\frac{1}{6}$
5	$d_L^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) &   & (+)(+) &    & (+)(-) & (-) & \end{matrix}$	-1	$\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
6	$d_L^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] &   & [-] & (+) &    & (+)(-) & (-) \end{matrix}$	-1	$-\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
7	$u_L^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i] & (+) &   & (+)[-] &    & (+)(-) & (-) & \end{matrix}$	-1	$\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$
8	$u_L^c 1$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i) & [-] &   & (+)[-] &    & (+)(-) & (-) & \end{matrix}$	-1	$-\frac{1}{2}$	-1	$\frac{1}{2}$	0	$\frac{1}{6}$	$\frac{1}{6}$

$\gamma^0 \gamma^7$  and  $\gamma^0 \gamma^8$  transform  $u_R$  of the 1<sup>st</sup> row into  $u_L$  of the 7<sup>th</sup> row, and  $d_R$  of the 4<sup>rd</sup> row into  $d_L$  of the 6<sup>th</sup> row, doing what the Higgs scalars and  $\gamma^0$  do in the Stan. model.



The **anti-eightplet** (the representation of  $SO(7, 1)$ ) of anti-quarks of the anti-colour charge, reachable by either  $S^{ab}$  or  $\mathbb{C}_N \mathcal{P}_N^{(d-1)}$ :

i		$ ^a \psi_i \rangle$	$\Gamma^{(3,1)}$	$S^{12}$	$\Gamma^{(4)}$	$\tau^{13}$	$\tau^{23}$	$Y$	$\tau^4$
		Antioctet, $\Gamma^{(7,1)} = -1$ , $\Gamma^{(6)} = 1$ , of antiquarks							
33	$\bar{d}_L^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i](+) &   & (+)(+) &    & [-] & [+ & [+ & \end{matrix}$	-1	$\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{1}{3}$	$-\frac{1}{6}$
34	$\bar{d}_L^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)[- &   & (+)(+) &    & [-] & [+ & [+ & \end{matrix}$	-1	$-\frac{1}{2}$	1	0	$\frac{1}{2}$	$\frac{1}{3}$	$-\frac{1}{6}$
35	$\bar{u}_L^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i](+) &   & [-] & [-] &    & [-] & [+ & [+ & \end{matrix}$	-1	$\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{2}{3}$	$-\frac{1}{6}$
36	$\bar{u}_L^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)[- &   & [-] & [-] &    & [-] & [+ & [+ & \end{matrix}$	-1	$-\frac{1}{2}$	1	0	$-\frac{1}{2}$	$-\frac{2}{3}$	$-\frac{1}{6}$
37	$\bar{d}_R^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & (+)[- &    & [-] & [+ & [+ & \end{matrix}$	1	$\frac{1}{2}$	-1	$\frac{1}{2}$	0	$-\frac{1}{6}$	$-\frac{1}{6}$
38	$\bar{d}_R^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i][- &   & (+)[- &    & [-] & [+ & [+ & \end{matrix}$	1	$-\frac{1}{2}$	-1	$\frac{1}{2}$	0	$-\frac{1}{6}$	$-\frac{1}{6}$
39	$\bar{u}_R^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ (+i)(+) &   & [-](+) &    & [-] & [+ & [+ & \end{matrix}$	1	$\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$-\frac{1}{6}$	$-\frac{1}{6}$
40	$\bar{u}_R^{\bar{c}1}$	$\begin{matrix} 03 & 12 & 56 & 78 & 9 & 1011 & 1213 & 14 \\ [-i][- &   & [-](+) &    & [-] & [+ & [+ & \end{matrix}$	1	$-\frac{1}{2}$	-1	$-\frac{1}{2}$	0	$-\frac{1}{6}$	$-\frac{1}{6}$

$\gamma^0 \gamma^7$  and  $\gamma^0 \gamma^8$  transform  $\bar{d}_L$  of the 1<sup>st</sup> row into  $\bar{d}_R$  of the 5<sup>th</sup> row, and  $\bar{u}_L$  of the 4<sup>rd</sup> row into  $\bar{u}_R$  of the 8<sup>th</sup> row. ↻ 🔍

- **All the vector gauge fields, manifesting at the observable energies, have all the properties assumed by the *standard model*.**

They carry **with respect to the space index**  $m \in (0, 1, 2, 3)$  the vector degrees of freedom while they have additional **internal degrees of freedom** ( $\tau^{Ai} = \sum_{st} c^{Aist}$ ) in the adjoint representations.

Analyzing all the indexes of the gauge fields, manifesting at low energy, with respect to  $\mathcal{S}^{ab}$ , where  $A_m^{Ai} = C^{Aist} \omega_{stm}$  and  $\mathcal{S}^{ab}$ , applies on index  $(s, t, m)$  as follows

$$\mathcal{S}^{ab} \omega_{stm\dots g} = i (\delta_s^a \omega_{tm\dots g}^b - \delta_s^b \omega_{tm\dots g}^a),$$

one finds that the weak, colour and hyper charge fields have just the properties required for them by the *standard model*.

- There are several **scalar gauge fields** - twice **three triplets** with respect to the **family** quantum numbers ( $\tilde{\tau}^{Ai} = \sum \tilde{c}^{Ai}_{ab} \tilde{S}^{ab}$ ) and **three singlets** with the quantum numbers **(Q,Q',Y')** - which manifest at the so far observable energies explaining the **Higgs's scalar** and the **Yukawa couplings**.

They all carry the weak charge and the hyper charge as required by the *standard model* for the Higg's scalar, while all the rest of quantum numbers are **in the adjoint representations**.

Their properties have to be analyzed with respect to the generators of the corresponding subgroups, expressible with  $S^{ab}$ .

The scalar condensate of two **right handed neutrinos** couple to all the scalar and vector gauge fields, except to the **weak charge  $SU(2)_I$** , the **hyper charge  $U(1)$** , and the **colour  $SU(3)$  charge gauge fields**, as well as the **gravity**, leaving them **massless**, J.of Mod.Phys.4(2013)823-847, J.of Mod.Phys.6(2015)2244-2247, Phys Rev.D 91(2015)6,065004.

state	$S^{03}$	$S^{12}$	$\tau^{13}$	$\tau^{23}$	$\tau^4$	$Y$	$Q$	$\tilde{\tau}^{13}$	$\tilde{\tau}^{23}$	$\tilde{Y}$	$\tilde{Q}$	$\tilde{N}_R^3$	$\tilde{N}_I^3$
$ \nu_{1R}^{VIII} >_1   \nu_{2R}^{VIII} >_2$	0	0	0	1	-1	0	0	0	1	0	0	1	0
$ \nu_{1R}^{VIII} >_1   e_{2R}^{VIII} >_2$	0	0	0	0	-1	-1	-1	0	1	0	0	1	0
$ e_{1R}^{VIII} >_1   e_{2R}^{VIII} >_2$	0	0	0	-1	-1	-2	-2	0	1	0	0	1	0

Before the appearance of the **condensate**, which breaks the CP symmetry,

scalars form

- **2 doublets**,  $s = (5, 6, 7, 8)$ , and
- a **triplet** and an **antitriplet**,  $s = (9, \dots, 14)$ .

**There are no additional scalars.**

All the scalars have the family and the family members quantum numbers in the **adjoint** representation.



The two doublets are:

	state	$\tau^{13}$	$\tau^{23} = Y$	spin	$\tau^4$	$Q$
$A_{78}^{Ai}$ (-)	$A_7^{Ai} + iA_8^{Ai}$	$+\frac{1}{2}$	$-\frac{1}{2}$	0	0	0
$A_{56}^{Ai}$ (-)	$A_5^{Ai} + iA_6^{Ai}$	$-\frac{1}{2}$	$-\frac{1}{2}$	0	0	-1
$A_{78}^{Ai}$ (+)	$A_7^{Ai} - iA_8^{Ai}$	$-\frac{1}{2}$	$+\frac{1}{2}$	0	0	0
$A_{56}^{Ai}$ (+)	$A_5^{Ai} - iA_6^{Ai}$	$+\frac{1}{2}$	$+\frac{1}{2}$	0	0	+1

There are  $A_{78}^{Ai}$  and  $A_{56}^{Ai}$  which gain a nonzero vacuum expectation values at the electroweak break.

Index  $Ai$  determine the family ( $\tilde{\tau}^{Ai}$ ) and the family members ( $Q, Q', Y'$ ) quantum numbers.



Scalars with  $\mathbf{s}=(7,8)$  gain nonzero vacuum expectation values breaking the weak and the hyper symmetry, and conserving the electromagnetic and colour charge.

$$\begin{aligned} \mathbf{A}_s^{\mathbf{A}i} &\supset (\mathbf{A}_s^{\mathbf{Q}}, \mathbf{A}_s^{\mathbf{Q}'}, \mathbf{A}_s^{\mathbf{Y}'}, \tilde{\mathbf{A}}_s^{\tilde{\mathbf{I}}}, \tilde{\mathbf{A}}_s^{\tilde{\mathbf{N}}_L}, \tilde{\mathbf{A}}_s^{\tilde{\mathbf{2}}}), \\ \tau^{\mathbf{A}i} &\supset (\mathbf{Q}, \mathbf{Q}', \mathbf{Y}', \tilde{\tau}^{\tilde{\mathbf{1}}}, \tilde{\mathbf{N}}_L), \\ \mathbf{s} &= (7,8). \end{aligned}$$

$\mathbf{A}i$  denotes family quantum numbers and  $(\mathbf{Q}, \mathbf{Q}', \mathbf{Y}')$ ,  $(\tilde{\tau}^{\tilde{\mathbf{1}}}, \tilde{\mathbf{N}}_L)$  quantum numbers of the first group of four families and  $(\tilde{\tau}^{\tilde{\mathbf{2}}}, \tilde{\mathbf{N}}_R)$  quantum numbers of the second group of four families.

The **mass term** in the **starting action** ( $p_s$ , when treating the lowest energy solutions, is left out) is

$$\mathcal{L}_M = \sum_{s=(7,8), Ai} \bar{\psi} \gamma^s (-\tau^{Ai} A_s^{Ai}) \psi =$$

$$-\bar{\psi} \left\{ \binom{78}{+} \tau^{Ai} (A_7^{Ai} - i A_8^{Ai}) + \binom{78}{-} \tau^{Ai} (A_7^{Ai} + i A_8^{Ai}) \right\} \psi ,$$

$$\binom{78}{\pm} = \frac{1}{2} (\gamma^7 \pm i \gamma^8), \quad A_{\binom{78}{\pm}}^{Ai} := (A_7^{Ai} \mp i A_8^{Ai}).$$

Operators  $Y$ ,  $Q$  and  $\tau^{13}$ , applied on  $(A_7^{Ai} \mp i A_8^{Ai})$

$$\tau^{13} (A_7^{Ai} \mp i A_8^{Ai}) = \pm \frac{1}{2} (A_7^{Ai} \mp i A_8^{Ai}),$$

$$Y (A_7^{Ai} \mp i A_8^{Ai}) = \mp \frac{1}{2} (A_7^{Ai} \mp i A_8^{Ai}),$$

$$Q (A_7^{Ai} \mp i A_8^{Ai}) = 0,$$

manifest that **all**  $(A_7^{Ai} \mp i A_8^{Ai})$  have quantum numbers of the **Higgs's scalar of the standard model**, "dressing", after **gaining nonzero expectation values**, the right handed members of a family with appropriate charges, so that they gain charges of the left handed partners:

$A_7^{Ai} + i A_8^{Ai}$  "dresses"  $u_R, \nu_R$  and  $A_7^{Ai} - i A_8^{Ai}$  "dresses"  $d_R, e_R$ , with quantum numbers of their left handed partners, just as required by the "standard model".



**A<sub>i</sub>** represents:

**O** either the **Q,Q',Y'** charges of the family members

**O** or transforms a family member of one family into the same family member of another family, within each of the **two groups of four families**,

manifesting in each group of four families  $\widetilde{SU}(2) \times \widetilde{SU}(2) \times U(1)$  symmetry.

## Family members and families

**Eight families** of  $u_R$  (spin 1/2, colour  $(\frac{1}{2}, \frac{1}{2\sqrt{3}})$ ) and of colourless  $\nu_R$  (spin 1/2). All have the weak charge

$\tau^{13} = 0$ ,  $\tau^{23} = \frac{1}{2}$ ,  $\tilde{\tau}^4 = -\frac{1}{2}$ . Quarks have "spinor" q.no.  $\tau^4 = \frac{1}{6}$  and leptons  $\tau^4 = -\frac{1}{2}$ . The first four families have  $\tilde{\tau}^{23} = 0$ ,  $\tilde{N}_R^3 = 0$ , the second four families have  $\tilde{\tau}^{13} = 0$ ,  $\tilde{N}_L^3 = 0$ .

		$\tilde{\tau}^{13}$	$\tilde{N}_L^3$
$u_{R1}^{c1}$	03 12 56 78 9 10 11 12 13 14 (+i) [+ ]   [+ ] (+)    (+) [- ] [- ]	$-\frac{1}{2}$	$-\frac{1}{2}$
$u_{R2}^{c1}$	03 12 56 78 9 10 11 12 13 14 [+i] (+)   [+ ] (+)    (+) [- ] [- ]	$-\frac{1}{2}$	$\frac{1}{2}$
$u_{R3}^{c1}$	03 12 56 78 9 10 11 12 13 14 (+i) [+ ]   (+) [+ ]    (+) [- ] [- ]	$\frac{1}{2}$	$-\frac{1}{2}$
$u_{R4}^{c1}$	03 12 56 78 9 10 11 12 13 14 [+i] (+)   (+) [+ ]    (+) [- ] [- ]	$\frac{1}{2}$	$\frac{1}{2}$
		$\tilde{\tau}^{23}$	$\tilde{N}_R^3$
$u_{R5}^{c1}$	03 12 56 78 9 10 11 12 13 14 (+i) (+)   (+) (+)    (+) [- ] [- ]	$-\frac{1}{2}$	$-\frac{1}{2}$
$u_{R6}^{c1}$	03 12 56 78 9 10 11 12 13 14 (+i) (+)   [+ ] [+ ]    (+) [- ] [- ]	$-\frac{1}{2}$	$\frac{1}{2}$
$u_{R7}^{c1}$	03 12 56 78 9 10 11 12 13 14 [+i] [+ ]   (+) (+)    (+) [- ] [- ]	$\frac{1}{2}$	$-\frac{1}{2}$
$u_{R8}^{c1}$	03 12 56 78 9 10 11 12 13 14 [+i] [+ ]   [+ ] [+ ]    (+) [- ] [- ]	$\frac{1}{2}$	$\frac{1}{2}$

Before the electroweak break all the families are mass protected and correspondingly massless.

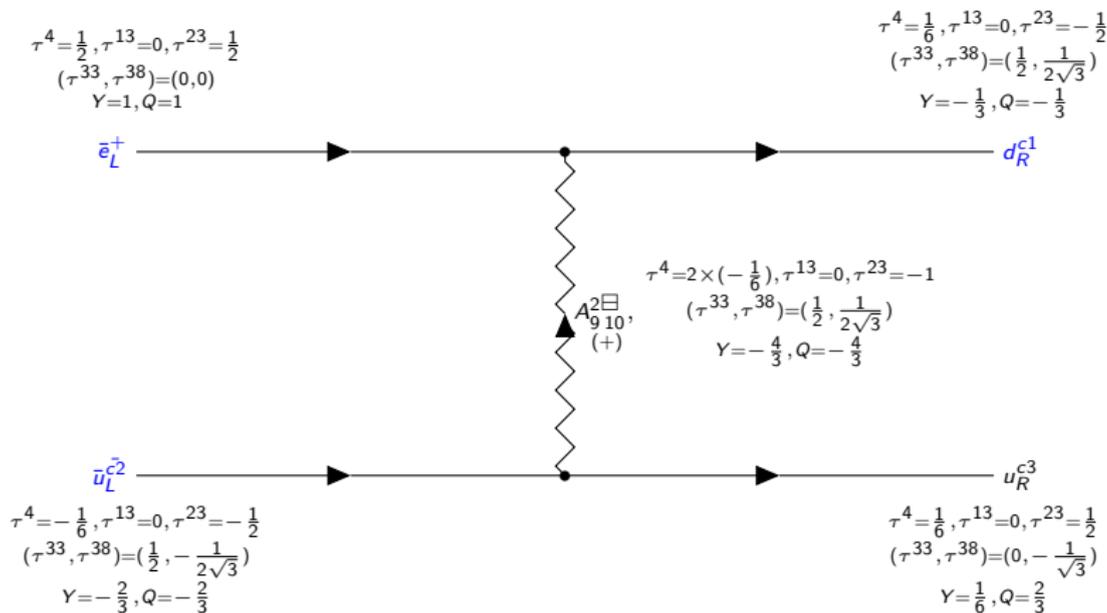
There are also **triplet** and **anti-triplet** scalars  $s = (9, \dots, d)$ :

	state	$\tau^{33}$	$\tau^{38}$	spin	$\tau^4$	$Q$
$A_{9\ 10}^{A_i}$ (+)	$A_9^{A_i} - iA_{10}^{A_i}$	$+\frac{1}{2}$	$\frac{1}{2\sqrt{3}}$	0	$-\frac{1}{3}$	$-\frac{1}{3}$
$A_{11\ 12}^{A_i}$ (+)	$A_{11}^{A_i} - iA_{12}^{A_i}$	$-\frac{1}{2}$	$\frac{1}{2\sqrt{3}}$	0	$-\frac{1}{3}$	$-\frac{1}{3}$
$A_{13\ 14}^{A_i}$ (+)	$A_{13}^{A_i} - iA_{14}^{A_i}$	0	$-\frac{1}{\sqrt{3}}$	0	$-\frac{1}{3}$	$-\frac{1}{3}$
$A_{9\ 10}^{A_i}$ (-)	$A_9^{A_i} + iA_{10}^{A_i}$	$-\frac{1}{2}$	$-\frac{1}{2\sqrt{3}}$	0	$+\frac{1}{3}$	$+\frac{1}{3}$
$A_{11\ 12}^{A_i}$ (-)	$A_{11}^{A_i} + iA_{12}^{A_i}$	$\frac{1}{2}$	$-\frac{1}{2\sqrt{3}}$	0	$+\frac{1}{3}$	$+\frac{1}{3}$
$A_{13\ 14}^{A_i}$ (-)	$A_{13}^{A_i} + iA_{14}^{A_i}$	0	$\frac{1}{\sqrt{3}}$	0	$+\frac{1}{3}$	$+\frac{1}{3}$

**They cause the transitions** of anti-leptons into quarks and anti-quarks into quarks and back, **transforming matter into antimatter and back**. **The condensate breaks CP symmetry**, offering the explanation for the matter-antimatter **asymmetry in the universe**.



Let us look at scalar triplets, causing the birth of a proton from the left handed positron, antiquark and quark:





These two quarks,  $d_R^{c1}$  and  $u_R^{c3}$  can bind (at low enough energy) together with  $u_R^{c2}$  into the colour **chargeless baryon - a proton**.

After the appearance of the **condensate** the **CP is broken**.

In the expanding universe, fulfilling the Sakharov request for appropriate nonthermal equilibrium, **these triplet scalars have a chance to explain the matter-antimatter asymmetry**.

The opposite transition makes the **proton decay**.

■ Due to

$$\tau^{1+} \tau^{1-} \mathbf{A}_{78(+)}^{\text{Ai}} = \mathbf{A}_{78(+)}^{\text{Ai}},$$

$$\tau^{1-} \tau^{1+} \mathbf{A}_{78(-)}^{\text{Ai}} = \mathbf{A}_{78(-)}^{\text{Ai}},$$

$$Q \mathbf{A}_{78(\mp)}^{\text{Ai}} = 0,$$

$$Q' \mathbf{A}_{78(\mp)}^{\text{Ai}} = \pm \frac{1}{2 \cos^2 \theta_1} \mathbf{A}_i^{\text{Ai}}{}_{78(\mp)},$$

the **vector gauge fields**  $A_m^{1\pm} (= W_m^\pm)$  and  $A_m^{Q'}$  ( $= Z_m$ )  
 $= \cos \theta_1 A_m^{13} - \sin \theta_1 A_m^Y$  become massive, while  $A_m^Q (= A_m)$   
 $= \sin \theta_2 A_m^{13} + \cos \theta_1 A_m^Y$  remain massless, if  $\frac{g_1}{g_Y} \tan \theta_1 = 1$ .



- Correspondingly the mass term of the **vector gauge bosons** is

$$\begin{aligned}
 & (p_{0m} A_{\mp}^{Ai})^\dagger (p_0^m A_{\mp}^{Ai}) \rightarrow \\
 & \left(\frac{1}{2}\right)^2 (g^1)^2 v^2 \left( \frac{1}{(\cos \theta_1)^2} Z_m^{Q'} Z^{Q' m} + 2 W_m^+ W^{-m} \right),
 \end{aligned}$$

$$\text{Tr}(\langle A_{\mp}^{Ai\dagger} \rangle \langle A_{\mp}^{vAi} \rangle) = \frac{v^2}{2}.$$

- It must be shown how can all the scalars **contribute so little to the heavy bosons mass.**

$$v^2 = \frac{m^2}{\Lambda}$$

- These scalars with the weak and the hyper charge  $(\mp\frac{1}{2}, \pm\frac{1}{2})$ , respectively, determine together with the **gauge vector fields** masses of all the members  $\alpha$  of the **lower four families**, and together with the **condensate also the masses** of the **upper four families**. **The group of the lower four families** manifest the  $\widetilde{SU}(2)_{\widetilde{SO}(1,3)} \times \widetilde{SU}(2)_{\widetilde{SO}(4)} \times U(1)$  **symmetry** (after all loop corrections, what we have shown, I believe), with  $(\mathbf{a}, \mathbf{a}_1, \mathbf{a}_2, \mathbf{e}, \mathbf{d}, \mathbf{b})$  as parameters:

$$\mathcal{M}^\alpha = \begin{pmatrix} -a_1 - a & e & d & b \\ e & -a_2 - a & b & d \\ d & b & a_2 - a & e \\ b & d & e & a_1 - a \end{pmatrix}^\alpha .$$

## Does the fourth family exist at all?

- No direct observation of the fourth family quarks with the masses below 1 TeV.
- The fourth family quarks with masses above 1 TeV contributions to the quark-gluon fusion production of higgs would be according to the *standard model* proportional to  $\frac{m_4^\alpha}{v}$ ,  $\alpha = u, d$ , and correspondingly  $\approx 10$  times too much in comparison with the observations.
- Similarly it goes also for the scalar field decay into two photons.
- Correspondingly the high energy physicists do not expect the existence of the fourth family members at all.



## Let us try to understand whether the observations really forbid the fourth family!

- In the *spin-charge-family theory* there are **two triplets** with the **family quantum numbers** and **three singlets** with the **family members** quantum numbers.
- All scalars carry the weak and the hyper charge like the higgs.
- Due to our calculations [arxiv:1412.5866] and the experimental observations to the masses of the **lower three families** mainly the **three singlets** with the **family members** quantum numbers contribute, causing the large differences in masses of the lower three families.



- To the masses of the **fourth family**, weakly coupled to the **observed three families**, again due to our calculation, mainly **two triplets** with the **family quantum numbers** contribute, causing that the fourth family quarks have comparable masses.
- Correspondingly the **three observed families** couple mostly to the **three singlets**, while the **fourth family** couple mostly to **two triplets**.
- Then to the **quark-gluon production of scalars with the family members** quantum numbers, as it is the higgs, mostly the **top quark** contributes, and so it also mainly contributes to the decay of the higgs into two photons, in agreement with the observations.

- $\mathcal{L}_{qm}$  for quarks mass term,  $k, j$  are the family index, (phases of the quarks states assures that fermions have the ordinary properties under the spin rotation and under  $\mathcal{C}_N \mathcal{P}_N$ ):

$$\begin{aligned}
 \mathcal{L}_{qm} = \frac{1}{2} \sum_{k,l} \{ & (u_L^{k\dagger} \gamma^0 \sum_{A,i,-}^{78} (-) \tau^{Ai} g^{Ai} A_-^{Ai} u_R^l) + \\
 & (u_R^{l\dagger} \gamma^0 \sum_{A,i,-} \tau^{Ai} (+)^{78} g^{Ai} A_+^{Ai} u_L^k) + \\
 & (d_L^{k\dagger} \gamma^0 \sum_{A,i,+}^{78} (+) \tau^{Ai} g^{Ai} A_+^{Ai} d_R^l) + \\
 & (d_R^{l\dagger} \gamma^0 \sum_{A,i,+} \tau^{Ai} (-)^{78} g^{Ai} A_+^{Ai} d_L^k)^\dagger \}.
 \end{aligned}$$



- The Hermiticity is assumed  $(A_{\pm}^{Ai})^{\dagger} = A_{\mp}^{Ai}$ .
- All the family operators commute with  $\gamma^0\{(\pm)\}^{78}$ :  
 $\{\gamma^0\{(\pm)\}^{78}, \tilde{\tau}^{Ai}\}_- = 0$ .
- The family members operators,  $\tau^{Ai} = (Q, Q', Y')$ , do not,  
 $\{(Q, Q', Y'), \gamma^0\{(\pm)\}^{78}\}_- \neq 0$ ,  
 however:  
 $\gamma^0(Q, Q', Y')\{(\pm)\}^{78} u_L^k = (Q_{Ru}, Q'_{Ru}, Y'_{Ru}) u_R^k$ ,  
 $\gamma^0(Q, Q', Y')\{(\pm)\}^{78} d_L^k = (Q_{Rd}, Q'_{Rd}, Y'_{Rd}) d_R^k$ .

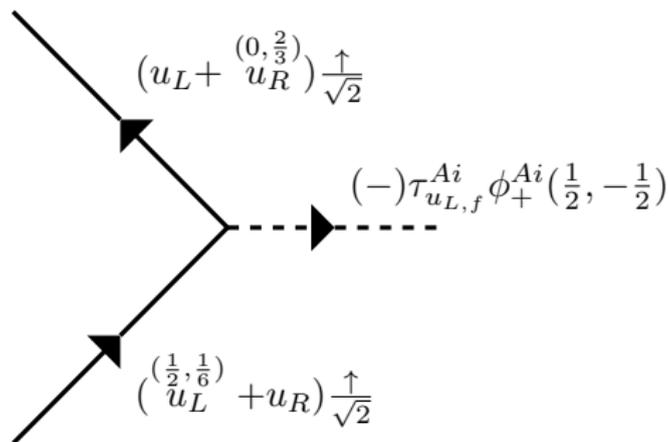


$$A_{78(\pm)}^{Ai} = v_{78(\pm)}^{Ai} + \Phi_{78(\pm)}^{Ai},$$

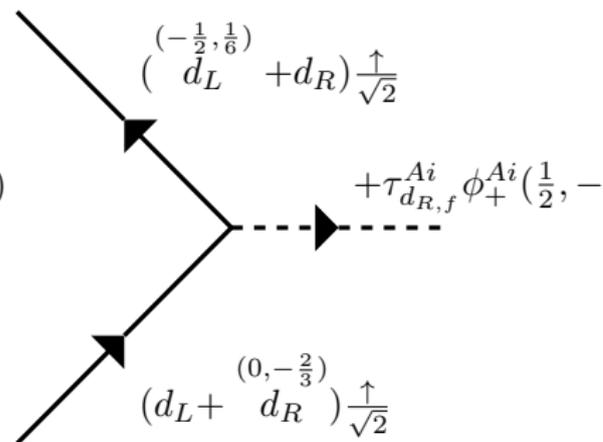
where  $A_{78(\pm)}^{Ai}$  represents scalars carrying either the family or the family members quantum numbers.



## Family members and families

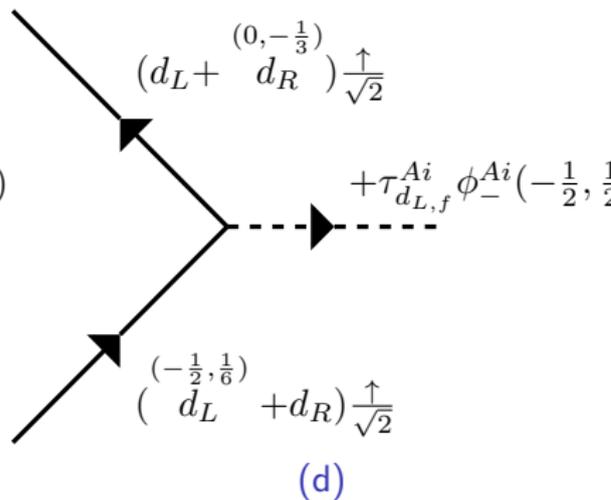
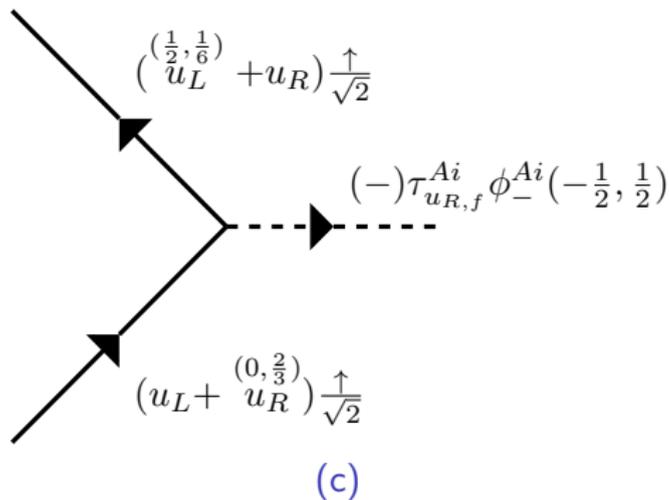


(a)



(b)

Family members and families





- One notices on Figs. (a,b,c,d) the opposite signs of the couplings of the scalar fields - the two triplets with the family quantum numbers to  $u^k$  with respect to  $d^k$ .

The two triplet scalars carrying the family quantum numbers do not distinguish between  $u^k$  and  $d^k$ .

- The three singlets carrying the family members quantum numbers do distinguish between  $u^k$  and  $d^k$ .
- Correspondingly the  $u^4$  and  $d^4$ , if having comparable masses, would contribute (very) little to either the quark-gluon fusion production of any scalar or to the decay to any scalar into two photons, which is consistent with the observations.

- However,  $u^4$  and  $d^4$ , having very little mixing matrix elements to the lower three families, if of not completely equal masses, do contribute to the quark-gluon fusion production of scalars carrying the family quantum numbers, as well as to the decay of such scalars into two photons.
- If the 750 GeV event on the LHC is the real one, could then a superpositions of scalars of the mass of  $\approx 750$  GeV be the first direct confirmation that there are several scalar fields, as predicted by the *spin-charge-family* theory?.

- Since the **decay** of this scalar would go stronger to two ( $W^+$ ,  $W^-$ ) and ( $Z^0$ ,  $Z^0$ ), what experiments have not observed, the two photons events then can not belong to the decay of this **scalar**.
- More probable is the **decay** of this scalar to two bosons - ( $W^+$ ,  $W^-$ ) and ( $Z^0$ ,  $Z^0$ ) (and also to two photons) – at the energy of about 1.8 TeV, if this observation is a real one. This would then be the first direct observation of the second scalar, among those, predicted by the *spin-charge-family* theory.  
The **indirect** signal of the existence of several scalars are the **Yukawa couplings**.

- Even if the phases of  $u^4$  and  $d^4$  can be washed away, still the existence of the fourth family is not so far in contradiction with the experiments.  
The fourth family quarks would in any case contribute very little to the production of the observed higgs in the quark-gluon fusion, since they mainly couple to the superposition of scalars with the family quantum numbers.
- I predict: **There is the fourth family**, with the weak mixing matrix elements to the lower four families.



- **Let us have a look on the explanations of the assumptions of the *standard model* and on predictions of the *spin-charge-family theory* to be able to notice whether Nature might be elegant and transparent in laws (in system with many degrees of freedom symmetries simplify effective laws).**

- **In the standard model** the **family members**, the **families**, the **gauge vector fields**, the **scalar Higgs**, the **Yukawa couplings**, exist by the **assumption**.
- **\*\*** In the **spin-charge-family theory** all these properties **follow from the simple starting action** with **two kinds of spins** and with **gravity only** .
  - \*\*** The theory offers the explanation for the **dark matter**, the stable of the upper four families does this.
  - \*\*** The theory offers the explanation for the **matter-antimatter asymmetry**, the condensate, breaking CP symmetry together with the massive triplet scalars do that.
  - \*\*** All the **scalar** and all the **vector** gauge fields are **directly or indirectly observable**.



## Concrete predictions:

- There are several scalar fields;
  - two triplets , ○ three singlets ,explaining higgs and Yukawa couplings, some of these scalars will be observed at the LHC, or one of these scalars might have 750 GeV, if the event is real.  
JMP 6 (2015) 2244,  
Phys. Rev. D 91 (2015) 6, 065004.
- There is the fourth family, (weakly) coupled to the observed three, which will be observed at the LHC, New J. of Phys. 10 (2008) 093002.



- There is the **dark matter**, with the predicted properties, Phys. Rev. D (2009) 80.083534.
- There is the ordinary **matter/antimatter asymmetry** explained and the **proton decay** predicted, Phys. Rev. D 91 (2015) 6, 065004.



With **G. Bregar** we **made calculations**, treating **quarks** and **leptons** in equivalent way, as required by the "spin-charge-family" theory.

- Any  **$(n-1) \times (n-1)$**  submatrix of an unitary  **$n \times n$**  matrix determines the  **$n \times n$**  matrix for  **$n \geq 4$**  uniquely.
- The measured mixing matrix elements of the  **$3 \times 3$**  submatrix are not accurate enough even for quarks to predict the masses  $m_4$  of the fourth family members.

**O** We can say only, if taking into account only mixing matrices and measured masses, that  $m_4$  quark masses might be any in the interval  **$(300 < m_4 < 1000)$**  GeV or even **above**.

- **Assuming** masses  $m_4$  we can predict mixing matrices.



## We recognize that:

- The last **data for mixing matrix of quarks** are in better agreement with our prediction for the  $3 \times 3$  **submatrix** elements of the  $4 \times 4$  **mixing matrix** than the previous ones.
- Our **fit** to the last data predicts how will the  $3 \times 3$  **submatrix elements change** in the next more accurate measurements.



Results are presented for two choices of  $m_{u_4} = m_{d_4}$ , [arxiv:1412.5866]:

- 1.  $m_{u_4} = 700$  GeV,  $m_{d_4} = 700$  GeV.....*new1*
- 2.  $m_{u_4} = 1\,200$  GeV,  $m_{d_4} = 1\,200$  GeV.....*new2*

$ V_{(ud)}  =$	<i>exp<sub>n</sub></i>	$0.97425 \pm 0.00022$	$0.2253 \pm 0.0008$	$0.00413 \pm 0.00049$	
	<i>new1</i>	0.97423(4)	0.22539(7)	0.00299	<b>0.00776(1)</b>
	<i>new2</i>	0.97423[5]	0.22538[42]	0.00299	<b>0.00793[466]</b>
	<i>exp<sub>n</sub></i>	$0.225 \pm 0.008$	$0.986 \pm 0.016$	$0.0411 \pm 0.0013$	
	<i>new1</i>	0.22534(3)	0.97335	0.04245(6)	<b>0.00349(60)</b>
	<i>new2</i>	0.22531[5]	0.97336[5]	0.04248	<b>0.00002[216]</b>
	<i>exp<sub>n</sub></i>	$0.0084 \pm 0.0006$	$0.0400 \pm 0.0027$	$1.021 \pm 0.032$	
	<i>new1</i>	0.00667(6)	0.04203(4)	0.99909	<b>0.00038</b>
	<i>new2</i>	0.00667	0.04206[5]	0.99909	<b>0.00024[21]</b>
	<i>new1</i>	<b>0.00677(60)</b>	<b>0.00517(26)</b>	<b>0.00020</b>	<b>0.99996</b>
	<i>new2</i>	<b>0.00773</b>	<b>0.00178</b>	<b>0.00022</b>	<b>0.99997[9]</b>

- The **matrix elements**  $V_{CKM}$  **depend strongly on the accuracy of the experimental  $3 \times 3$  submatrix.**
- Calculated  $3 \times 3$  submatrix of  $4 \times 4$   $V_{CKM}$  depends on the  $m_{4th}$  **family masses**, but not much.
- $V_{4i}, V_{i4}$  do not depend strongly on the  $m_{4th}$  family masses.
- $V_{u_i d_4}$  and of  $V_{d_i u_4}$  are obviously **very** small.



## Predictions from the calculated quark mixing matrix:

- $|V_{ud}|$  will stay or will slightly decrease.
- $|V_{us}|$  will continue slightly increasing.
- $|V_{cd}|$  will very slightly increase back towards  $exp_0$ .
- $|V_{cb}|$  will still increase.
- $|V_{ts}|$  will very slightly increase back towards  $exp_0$ .
- $|V_{ub}|$  will still decrease.
- $|V_{cs}|$  will still decrease.
- $|V_{td}|$  will decrease.
- $|V_{tb}|$  will decrease, approaching 1 from below.



- The higher are the fourth family members masses, the closer are the mass matrices to the **democratic matrices** for either quarks or leptons, as expected.
- **Mass matrices for quarks:**

$$\mathbf{M}_d^u / \text{MeV}/c^2 = (1.25, 620.1, 172\,000., 700\,000.),$$

$$\mathbf{M}_d^d / \text{MeV}/c^2 = (2.92, 54.8, 2\,899., 700\,000.),$$

## Mass matrices of quarks:

$m_{u_4} = 700 \text{ GeV}$  and  $m_{d_4} = 700 \text{ GeV}$ .

- $$M^u = \begin{pmatrix} 227623. & 131877. & 132239. & 217653. \\ 131877. & 222116. & 217653. & 132239. \\ 132239. & 217653. & 214195. & 131877. \\ 217653. & 132239. & 131877. & 208687. \end{pmatrix},$$

- $$M^d = \begin{pmatrix} 175797. & 174263. & 174288. & 175710. \\ 174263. & 175666. & 175710. & 174288. \\ 174288. & 175710. & 175813. & 174263. \\ 175710. & 174288. & 174263. & 175682. \end{pmatrix},$$



- Mass matrices for  $m_4 \geq 1 \text{ TeV}$  are closer to a **democratic** matrix, like  $M^d$  at 700 GeV.
- From values of the calculated mass matrix elements we try to extract some properties of the **two triplet and three singlet scalar fields** with the weak and the hyper charge of higgs:  $(\mp\frac{1}{2}, \pm\frac{1}{2})$ .

- The **upper four families** are **decoupled** from the **lower four families**.
- The **stable family** of the **upper four families** group is the candidate to form the **Dark Matter**.
- Their masses are influenced by:
  - the  $\widetilde{SU}(2)_{II\widetilde{SO}(3,1)} \times \widetilde{SU}(2)_{II\widetilde{SO}(4)}$  **scalar fields** with the corresponding family quantum numbers,
  - the **scalars**  $(A_{78}^Q, A_{78}^{Q'}, A_{78}^{Y'})$ , and
  - the **condensate** of the two  $\nu_R$  of the **upper four families**.
- With **G. Bregar** we investigate this possibility carefully.

hep-ph/0711.4681, p.189-194; *Phys. Rev. D* **80**, 083534 (2009).

- Masses of the **fifth family** lie **much above** the known three and the **predicted fourth family** masses.
- **Baryons** of the **fifth family** are heavy, forming small enough clusters with small enough scattering amplitude among themselves and with the ordinary matter to be the candidate for the **dark matter**.
- We make a rough estimation (with a Bohr like model) of properties of clusters of  $(u_5, d_5, \nu_5, e_5)$ , which interact with the same vectors gauge fields as the lower four family, here with **one gluon** (one weak and one hyper charge) exchange.

## We estimate:

- The behavior of such clusters in the **evolution** of the **Universe**.
- The behavior of such clusters when **hitting our Earth**, and in particular direct measurements - DAMA/NaI and DAMA-LIBRA and others.
- The elm. **neutral fifth family baryons** (neutrinos also contribute) form the **dark matter**.
- Direct measurements and cosmological evolution limit my **fifth family masses** to
 
$$10 \text{ TeV} < m_{q_5} c^2 < 10^4 \text{ TeV}.$$
- Dark matter baryons are opening an interesting new **"fifth family nuclear"** dynamics.



- The **spin-charge-family theory** is offering an explanation for the **hierarchy problem**:  
The mass matrices of the **two four families groups** are almost democratic, causing spreading of the **fermion masses** from  $10^{16}$  GeV to  $10^{-8}$  MeV.

## To Summarize:

- The spin-charge-family theory offers **the explanation** for:
  - the **origin of charges,**
  - the **origin of families,**
  - the **origin and properties of scalar fields,**
  - the **origin and properties of vector fields,**
  - the **properties of families,**
  - the **the hierarchy,**
- The spin-charge-family theory offers **the explanation** for:
  - the **origin of "ordinary" matter-antimatter asymmetry and the proton decay,**
  - the **origin of the dark matter.**



## The spin-charge-family theory **predicts:**

- **New families:**
  - **the fourth family** will be observed at the LHC,
  - **the fifth one forms** the **dark matter**.
- **New scalar fields**, one of them might be already observed at the LHC.
- The  $SU(2)_{II}$  vector gauge fields, too heavy to be directly observed.
- **New kind of the "nuclear force"** within the stable heavy family members.
- The direction in which the  $V_{CKM}$  will change.



- **o Fermionization** in any dimension might help to understand better if and why the *spin-charge-family* theory is a possible next step beyond the *standard model*.
- **o** The spin-charge-family theory is expected to have many a thing in common with other proposed theories, models, ideas.
- **o** More than I am working on the spin-charge-family theory more phenomenological, directly or indirectly observed, properties appear to be describable within this project.